## Optimizing the dispatch schedule of Product Y

## Bachelor Thesis

Industrial Engineering and Management

## Pedersen, J.E. (Jesper. Student B-IEM)

Supervisor 1: Dr Daniela Guericke (University of Twente)
Supervisor 2: Dr Derya Demirtas (University of Twente)
Supervisor 3: Erik Keppels (Company X)

## Preface

Dear reader,
This bachelor's thesis is the final part of the Bachelor of Industrial Engineering and Management programme at the University of Twente. This study was conducted for an anonymous Dutch mechanisation business. The study "Optimising the dispatch schedule of Product $Y$ " aids the business in integrating the product into the supply chain.

I would like to take this opportunity to thank the university staff and the company for their assistance with my research and thesis writing. My first supervisor, Daniela Guericke, deserves special recognition for helping me through this procedure. It was enjoyable working with you, and I sincerely hope that this won't be the last time. Erik Keppels, who is my company's supervisor, deserves a special mention as well. You assisted me in providing an overview of the business and the product. He helped me navigate the company and was always available to answer queries. I learned a lot from the wonderful experience.

Enjoy Reading,
Kind regards,

Jesper Pedersen
Enschede, September 2023

## Management Summary

## Introduction

Company X is a family-owned mechanisation company that produces metal processing machines and complete machine lines. It consists of two divisions. Company $X$ Machinery's first division manufactures Computer Numerical Control (CNC) machines for steel fabrication. Currently, the company produces 20 machines. The other division, Company X Construction, specialises in the design, production, and supply of steel projects, acting as a subcontractor that delivers steel to a project.

In September 2022, Company X presented a new sorting machine called Product Y. Company X desires to change material storage's disadvantages into a central plate handling advantage with digital inventory management. Where previously plates destinated for a beam were sorted manually, now Product Y can identify, store, and dispatch the plates in designated bins for a specific beam. The company recognises that there are problems with implementing Product $Y$ in the supply chain and wants to improve the flow of products towards the workplace. To improve this workflow, a distribution method should be created.

## Approach

In order to create a good distribution, the method Managerial Problem Solving Method (MPSM) guidelines were used. This methodological approach uses seven sequential phases to help solve the problem. These phases were followed through this research to find a solution to the company's problem. After first understanding the business and the current situation, it was time to find a possible solution via literature studies. There are three priority rules for the beam distribution over workplaces and three priority rules for bin distribution of product $Y$ from this literature study. This means there are nine different combinations of rules to be tested (Table below)

| Beam priority rules | Objective |
| :--- | :--- |
| Shortest Processing Time (SPT) | Distribute increasingly on the processing time of beams. |
| Longest Processing Time (LPT) | Distribute decreasingly on the processing time of beams. |
| Service in Random Order (SIRO) | Random distribution over welders. |
| Plate priority rules | Objective |
| Shortest Processing Time (SPT) | Distribute increasingly on the processing time of plates. |
| Earliest Due Date (EDD) | Sort on increasing the due date for bins. |
| Shortest Setup Time (SST) | Sort on increasing setup time for bins. |

## Simulation

Data provided by Company $X$ was prepared into experiments and set in the suitable template. The nine experiments were evaluated in a simulation model created in Tecnomatix Plant Simulation. From here, the most surprising experiment was set for a sensitivity analysis. A dispatching order from excel is imported directly into the simulation to evaluate the rule combinations.

## Results

The performance evaluation of the nine experiments gives results to be investigated. The three beam methods were first performed following the three plate rules on the beam order. In the evaluations, the distribution starting time was set at 06:00 AM with 50 bins in circulation.

| Beam priority rule: | Current situation | SPT | SPT | SPT | LPT | LPT | LPT | Random | Random | Random |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plate priority rule: | Current situation | SPT | EDD | SST | SPT | EDD | SST | SPT | EDD | SST |
| AvgWaitingTime: | 1:26:56.3 | 7:49.9 | 7:18.9 | 9:10.2 | 44:38.1 | 45:50.7 | 10:17.0 | 08:27 | 03:43.8 | 09:11.8 |
| TotalProcessTime: | 18:25:19.6 | 15:56:53.2 | 15:18:22.8 | 15:59:19.2 | 14:55:51.3 | 10:52:42.5 | 15:59:19.2 | 15:53:21.6 | 13:03:37.2 | 15:49:39.8 |
| TotalWorkingTime | 09:55:19.6 | 14:26:53.2 | 13:48:22.8 | 14:29:19.2 | 13:25:51.3 | 9:22:42.5 | 14:29:19.2 | 14:23:21.6 | 11:33:37.2 | 14:19:39.8 |
| Welder Working\% | 67.5 | 58.3 | 58.2 | 58.2 | 58.3 | 73.3 | 58.2 | 58.3 | 62.7 | 58.2 |
| Welder Walking\% | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 | 0.7 | 0.6 | 0.6 | 0.6 | 0.6 |
| Welder Waiting\% | 31.9 | 41.1 | 41.2 | 41.2 | 41.1 | 25.9 | 41.2 | 41.1 | 36.7 | 41.2 |

The most exciting outcome from these results was the LPT/EDD combinations, where the total working time resulted in only 9 hours and 22 minutes. So, after the execution of the nine experiments, the sensitivity analysis was performed on the LPT/EDD combination. Here the starting hour was changed to 05:00 AM and 07:00 AM. Also, the bin numbers were changed to $25,30,35,40,45,50,75$ and 100 .

| starting hour: 05:00 |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Number of bins | 25 | 30 | 35 | 40 | 45 | 50 | 75 | 100 |
| AvgWaitingTime: | $0: 50.1$ | $8: 42.7$ | $18: 34.1$ | $28: 53.0$ | $39: 41.5$ | $49: 47.8$ | $1: 32: 21.5$ | $1: 59: 24.8$ |
| TotalProcessTime: | $11: 38: 15.4$ | $11: 20: 41.7$ | $11: 13: 51.9$ | $11: 07: 45.4$ | $11: 06: 55.9$ | $11: 06: 55.9$ | $11: 06: 55.9$ | $11: 06: 55.9$ |
| TotalWorkingTime | $9: 08: 15.4$ | $8: 50: 41.7$ | $8: 43: 51.9$ | $8: 37: 45.4$ | $8: 36: 55.9$ | $8: 36: 55.9$ | $8: 36: 55.9$ | $8: 36: 55.9$ |
| Welder Working\% | 75.3 | 77.8 | 78.8 | 79.7 | 79.8 | 79.8 | 79.8 | 79.8 |
| Welder Walking\% | 0.7 | 0.8 | 0.8 | 0.8 | 0.7 | 0.7 | 0.7 | 0.7 |
| Welder Waiting\% | 24.0 | 21.5 | 20.4 | 19.5 | 19.3 | 19.3 | 19.3 | 19.3 |


| Starting hour: 06:00 |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Number of Bins | 25 | 30 | 35 | 40 | 45 | 50 | 75 | 100 |
| AvgWaitingTime: | $0: 50.7$ | $7: 59.7$ | $16: 30.6$ | $26: 46.9$ | $36: 26.7$ | $45: 50.7$ | $1: 25: 33.8$ | $1: 49: 48.9$ |
| TotalProcessTime: | $11: 20: 22.5$ | $11: 05: 14.4$ | $10: 59: 40.7$ | $10: 52: 42.5$ | $10: 52: 42.5$ | $10: 52: 42.5$ | $10: 52: 42.5$ | $10: 52: 42.5$ |
| TotalWorkingTime | $9: 50: 22.5$ | $9: 35: 14.5$ | $9: 29: 40.7$ | $9: 22: 42.5$ | $9: 22: 42.5$ | $9: 22: 42.5$ | $9: 22: 42.5$ | $9: 22: 42.5$ |
| Welder Working\% | 69.9 | 71.7 | 72.4 | 73.3 | 73.3 | 73.3 | 73.3 | 73.3 |
| Welder Walking\% | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 |
| Welder Waiting\% | 29.4 | 27.5 | 26.8 | 25.9 | 25.9 | 25.9 | 25.9 | 25.9 |


| starting hour: 07:00 |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Number of bins | 25 | 30 | 35 | 40 | 45 | 50 | 75 | 100 |
| AvgWaitingTime: | $0: 50.5$ | $7: 36.2$ | $16: 00.0$ | $26: 28.4$ | $35: 52.1$ | $44: 58.5$ | $1: 22: 29.5$ | $1: 22: 29.5$ |
| TotalProcessTime: | $11: 12: 14.4$ | $10: 58: 41.1$ | $10: 51: 44.5$ | $10: 46: 43.6$ | $10: 46: 43.6$ | $10: 46: 43.6$ | $10: 46: 43.6$ | $10: 46: 43.6$ |
| TotalWorkingTime | $10: 42: 14.4$ | $10: 28: 41.1$ | $10: 21: 44.5$ | $10: 16: 43.6$ | $10: 16: 43.6$ | $10: 16: 43.6$ | $10: 16: 43.6$ | $10: 16: 43.6$ |
| Welder Working\% | 64.3 | 65.6 | 66.4 | 66.9 | 66.9 | 66.9 | 66.9 | 66.9 |
| Welder Walking\% | 0.6 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 |
| Welder Waiting\% | 35.1 | 33.7 | 33,0 | 32.4 | 32.4 | 32.4 | 32.4 | 32.4 |

These results can be seen in the table above. Remarkable is that change in the number of bins can decrease the waiting time with more time and increases the total working time.

## Recommendations

The company wants to sell Product $Y$ globally, aiming to improve the efficiency and accuracy of plate sorting in welding. By implementing Product $Y$, the company can track the location of each plate and prevent missing plates, leading to increased efficiency for welders. However, after storage, there is still a need for a dispatch schedule to utilise the machine effectively. To address this, the recommendation is to invest in a beam ordering system, which would provide valuable information for planners on how to use the machine effectively. With a detailed schedule based on the time required for welders to work on a beam and tack weld a specific plate, Product $Y$ would greatly benefit.

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## 1. Introduction

The first chapter introduces the research company and briefly describes the problem in section 1.1 In section 1.2, the research objective and methodology.

### 1.1. Company \& Problem

### 1.1.1. Company $X$

Company $X$ is a family-owned business established in 1970 as a mechanisation company, producing metal processing machines and complete machine lines. In 1976, the Company expanded its services to include the design and construction of steel structures, leading to a decision in 1980 to split the Company into two separate entities: a construction company and a machinery company.

Company X Machinery focuses on manufacturing Computer Numerical Control (CNC) machines for steel fabrication. These machines are controlled by computer programs, which direct the movements and patterns applied to the processed material. The company currently produces 20 machines, categorised into four processing types: beam, plate, pipe, angle processing, and surface treatment. Additionally, the company offers a complete process creating the possibility for a completely automated production process by connecting all standalone machines (Figure 1).


Figure 1 Example of a complete process
The other division, Company X Construction, specialises in the design, production and supply of steel projects, acting as a subcontractor that delivers steel to a project. One significant advantage is that they can utilise and test the machines developed by Company X Machinery, enabling data collection and machine improvement.

### 1.1.2. Management Problem

Beams are distributed over all workplaces at the beginning of the day. The specifications of beams will differ for every project. This means that every beam will require different sets of plates to be attached. A combination of specific plates and beams is called an assembly. For every assembly, at least one bin is required for the plates to be transferred from Product $Y$ to the workplace. It is impossible to combine different assemblies for the instance that only a few plates need to be attached to the beam.

In September 2022, Company X presented a new sorting machine called Product Y. Company X desires to change material storage's disadvantages into a central plate handling advantage with digital inventory management. Previously, the plates would arrive from a plasma cutter in the production
hall. Here all the plates arrive and are stored together. In the next step all these plates are manually sorted into bins (Figure 2). Once a bin is filled with the required plates, they are stored in a designated area. When required, the bins are brought to the workplace. All the plates are tack-welded to the beams at these workplaces.


Figure 2 Current manual sorting situation
Company X Machinery is developing Product $Y$ (Figure 3). The machine is still a prototype, so there is room for improvement in different aspects. Company $X$ has a production hall close to the machinery office. Here Product $Y$ is stationed and used for testing new software and collecting data on different parts. The Company recognises that there are problems with implementing Product $Y$ in the supply chain and wants to improve the flow of products towards the workplace.


Figure 3 Render of Product $Y$
Company $X$ wants to focus on the next steps of the process. Testing different dispatching schedules for Product $Y$ is one part of that. There is no method for determining a dispatch schedule. Since the distribution time of a plate keeps improving with software updates, it is essential to keep updating the dispatching schedule for efficient usage of the machine.


Figure 4 Problem cluster
In Figure 4, an overview of the management problem in the problem cluster can be seen. The management problem of Company $X$ can be set into one general problem but originates from several smaller problems. Some of these problems are not influenced by Product $Y$ such as the inefficient transport of bins, the daily production planning, or the overviews system. multiple problems also occurred with the implementation of Product $Y$. To conclude this cluster, it can be said that the product flow towards the workplace is not efficient. From here, the management problem can be formulated:

Management Problem: The product flow from Product $Y$ towards the beam workplace is not optimised.

### 1.1.3. Problem Identification

As mentioned before, the problem with the distribution of Product Y is that Company X has not been working on a dispatch schedule. This means there is no knowledge of the order of bin dispatching or when the machine should start.

Product $Y$ should distribute bins filled with plates for the concerning beams at the right moment. To minimise the downtime of the welders, the filled bins should always be present at the beam when required. On the other hand, it should not be dispatched too early because more bins are required in circulation, and a larger storage area is needed as a buffer for filled bins.

All the beams need to be finished at the end of the day. There is no planning per specific beam where it should be placed and when it should be welded. If the bins can be dispatched at the right time and the beams can be planned on a beam-specific level, then a more efficient product flow can be coordinated. This can result in more control and better usage of Product Y .

To summarise the previous points into a central problem, it has been stated below:
Core problem: There is no dispatch planning for Product $Y$.

### 1.1.4. The gap between Norm and Reality

In the book Solving Managerial Problems Systematically (Heerkens \& van Winden, 2017), the discrepancy between the norm and reality should be stated to clarify the core problem. Once a core
problem is acquired from a cluster, there needs to be a variable in which the problem can be measured. A variable will not always be quantifiable, so this requires operationalisation. Here a measurable variable will be connected to the core problem. From this point, a norm and reality should be defined.

In the case of Company X, it is about the dispatch planning of the machine. No planning or heuristic exists to determine how the bins should be dispatched. This means that all the bins should be filled before the works begin. This will result in a significant number of bins in circulation and a large buffer area to store all these bins. This means there is a long time between the moment of dispatching and the moment of usage. The time between these moment reaches the largest possible since without a dispatch schedule all the bins are dispatched before the day starts. The beams processed at the beginning of the day will have a shorter waiting time, but the beams at the end will have a very long time. So, the reality can be seen as the maximum time in the current situation. The norm, which is the time between dispatching and usage is set to be half an hour before the requirement.

### 1.2. Research Question \& Problem-Solving Approach

### 1.2.1. Research Question

The main research question can be derived from the core problem. As mentioned earlier, with the implementation of Product $Y$ into the logistical process, the company is facing problems with the dispatching of plates, resulting in an inefficient process. The dispatch schedule requires input from the beams' schedule to work. Without this schedule, it is not known when which bin is required. To make a daily schedule for the beams, the process times of each beam is needed. With this schedule, it is possible to generate a distribution order for Product Y . From this point, one can calculate the influence of the proposed dispatch planning on the logistical process. The following research question can be derived:

Research Question: "How can Product Y improve the product flow towards the workplace?"

### 1.2.2. Problem-Solving Approach

The Managerial Problem Solving Method (MPSM) guidelines are used in this research. This is a methodological approach based on seven sequential phases (Heerkens \& van Winden, 2017):

1. Defining the problem
2. Formulating the approach
3. Analysing the problem
4. Formulating (alternative) solutions
5. Choosing a solution
6. Implementing the solution
7. Evaluating the solution

These phases are visited throughout this report. Chapter 1 already defined the problem in section 1.1 and formulate an approach in section 1.2. The next phase will be executed in Chapter 2, where the problem is investigated. From this point, the solutions for the problem are formulated with a literature review in Chapter 3. To implement a solution, the setup for an experiment is required. This will be presented in Chapter 4. In Chapter 5, different solutions will be chosen and implemented. The solutions are evaluated in Chapter 6. Unfortunately, it is impossible to evaluate the solutions due to the length of the research.

### 1.2.3. Sub-questions

To divide the primary research question into smaller parts and make it easier to execute the research sub-questions are created. These will divide the thesis into smaller parts to understand it better in the parts and.

Sub-Question 1: How is the current beam production line organised?

- How does Company X plan its beam assembly?
- How are the plates sorted for assembly?
- How do the welders execute the daily production?

Sub-Question 2: What does the implementation of Product $Y$ change to the beam assembly?

- How does Product Y work?
- What changes for the logistical process?
- How should the beam and plates be planned?
- Which Key Performance Indicators are important for Product Y?

Sub-question 3: How can Product $Y$ be improved?

- What are the appropriate priority rules for the beam distribution?
- What are the appropriate priority rules for the bin distribution order?
- What is the best model to evaluate the combinations of priority rules?

Sub-Question 4: How can simulation help the distribution method of Product $Y$ ?

- Which data is required for the simulation?
- How do the beam and plate priority rules work?
- What kind of simulation is used?
- How does the simulation work?

Sub-Question 5: How do the applied priority rule combinations perform?
Sub-Question 6: What recommendations can be made on Product $Y$ with the evaluation of the simulation?

- What are the limitations of the simulation?
- How can the model help different company desires?


### 1.2.4. Deployment of the method

At the end of the research, a tool will create a dispatch schedule for the working Product Y . A simulation will determine how the dispatch schedules perform. The KPIs will be a result and determine if a particular schedule is good. Every Company has a different beam scheduling method, so that the input will differ. Therefore, it is also essential that the end user knows how to use the parameter and makes a well-working schedule for Product $Y$.

### 1.2.5. Assumptions

For this research, some assumptions need to be made. The final tool will have some assumptions because of external factors. Every stationed machine will have different output and input from both sides of the logistical process.

In the current situation at Company $X$, it is known that the plates are directly coming from the cutting hall and with the assumption that no plates are lost. The company cannot always know where their plates will be coming from. Hence, there must be an assumption on the input of Product Y's plates that this is always on time and complete.

Secondly, there is an assumption to be made about the layout of the bins. With the software now used, it is only possible to fit one assembly in the bin regardless of the number of assigned plates. This could change in the future, but it will not be reviewed since it can change the output process.

## 2.Problem Analysis

This chapter will provide insights into the current situation and how Product Y works. Here the first two sub-questions will be answered. First; "How is the current beam production line organised?" will be answered in section 2.1. The second question: "What does the implementation of Product $Y$ change to the beam assembly?" will be discussed in section 2.2.

### 2.1. Current Situation

Product $Y$ was launched to the market in September. The construction division tests the integration of the product into the supply chain. If the machine would be integrated into the current supply chain, it can not deliver the same throughput levels as the situation without Product Y . This means that in the current situation Product $Y$ is not used. To explain the current situation, a closer look into Figure 2 is required. The operation consists of three main elements. The Beams, plates, and the workplace. The beams and plates both come from a different origin. At the workplace they are welded together before the finished product can leave the production hall. In the following section, these three aspects will be explained in more detail for a better understanding of the whole operation.

### 2.1.1. Beams

Four phases of beams will be completed at the building site per day on average. Consider each phase as a truck loaded with beams and prepared for departure. This implies that as soon as the beams are completed, they will be put onto a truck and driven to their final location. Around 30 beams need to be processed on average during a phase. The beams have undergone several procedures to meet requirements before being set up on the job site. These processes include sawing, drilling, cutting, and painting. These processes will occur in the same production hall on the beamline. A beam is positioned alongside the others in a buffer area in the hall after it is prepared for welding.

### 2.1.2. Plates

The plates are delivered from another production facility. There, a large metal sheet is cut into multiple plates. After a batch is produced and given the unique specifications, they are moved to the production hall. First, all the plates are manually sorted into bins designated to specific bins. On an average day, Five fulltime-equivalents (FTE) work on 1050 plates. Once a bin is finished it is transferred to a storage area for filled bins. When required for welding, the bins are transported to the workplace where the beam is located. It is not always possible to arrange these plates in the proper order. The Company cannot build the plates in a way that will make them simple to sort since plate thickness varies. This implies that the manufacturing hall's buffer space will be significant.

### 2.1.3. Workplace

The beam and plates come together at the workplace. The day begins at 7:00 at Company X. The employees have 30 minutes to divide the beams over the 50 workplaces. These beams will be distributed at random because there is no beam-level planning. This implies that the location will be recognised when the employee starts on a specific beam.

50 Welders in pairs of two begin at 7:30, have two breaks of 30 minutes and work until 16:30 to complete the beams. The welder pairs have eight hours to complete the daily task. The production planner has created a timetable to ensure all work can be completed during this shift. These welders use a technique called tack welding to secure all the plates to the beams. Once a beam is finished, they start the next beam on the workplace. If all the beams on a workplace are done, they choose the next workplace randomly and start working there. This process goes on until all the beams are finished.

The second shift of welders begins at 16:30. These individuals will finish welding the plates to the beams. A beam will be moved from the workplace to the truck after it is done. The truck will start heading towards its ultimate destination once the phase is loaded.

### 2.2. Introduction of Product $Y$

The introduction of Product $Y$ removes the manual sorting of the bins and the problem of missing plates, as seen in Figure 5. The machine has two input conveyor belts and one output belt. The first input conveyor belt is for the plates. All the plates can be laid down on the belt. At the entrance of the machine, there is a 3D scanner camera. This inspects the plates and checks if they match those known to enter. If the plates match one from the database, they may continue the conveyor belt towards the storage towers. A plate will be rejected and travel an alternative route on the conveyor belt if the 3D scanner cannot identify it. All the rejected plates will be placed in a bin that is located on the conveyor belt's side.


Figure 5 New automated sorting situation
After being scanned and identified, the plate will move on to the magnetic arm (manipulator in Figure 6). The storage tower will simultaneously let down a drawer. The plate will be picked up and positioned in the drawer by the arm. The drawer will go back into the tower. During the storing of plates, the locations of plates will be stored in a database and used when required.

Product $Y$ can consist of up to three storage towers in total. Each of these towers has 145 drawers lined with rubber mats to prevent the plates from shifting while being stored. In addition to picking up plates to put them in a drawer, the arm can load plates into the bins. A double-tray method was developed to make this procedure more effective. It implies that the machine may initiate the second drawer while the first tray is descending since it already knows which drawer will be needed.

The bins are on the second input belt. Stacks of five bins can be placed on the conveyor belt. A single bin will continue to the magnetic arm with the help of an unstacking machine. Each bin will receive a
unique code that the machine can read. Plates destined for a specific beam will be filled from now on. A bin will move towards the output belt once it is complete.

Additionally, a stacking device can arrange the bins in stacks of up to five bins. These are manually taken off the belt and carried across to where the beam will be placed. The overview of Product Y can be seen in Figure 6.


Figure 6 Product Y layout
The introduction of Product Y creates a challenge for the company's planning schedule. The machine's output is set to a beam level. This indicates that a filled bin travelling down the conveyor belt is headed for a particular beam placed at a specific location. Each day, beam output is planned. As a result, there is a difference between the schedules' levels. Since virtually all businesses use phase-based daily planning, creating a dispatch schedule that distributes the filled bins appropriately is crucial. On the other hand, it is also critical to learn more about the location of the beams.

### 2.2.1. Beam planning

As was noted earlier, daily schedules are made to complete the beams. The sequence of the completed beams is not known at the start of the day, only which beams need to be completed. The production planner uses a forecasting tool that estimates the total duration. For this tool the specifications for the whole phase are used. Welders will establish a workspace and operate in pairs. About 120 beams will need to be completed. When one group is done, they move on to the following workplace, where another set of beams will be prepared for tack welding.

### 2.2.2. Plate planning

The beams are explicitly planned for each day. This is not a practical option for the planning of the plate. For a specific beam, Product $Y$ will send out a bin containing the required plates for the specific beam. This implies that Product $Y$ must understand when the plates are needed and, consequently, when they should be dispensed. The processing of the beams is now taking place in a random sequence. This means the location only becomes known when the welders start working on it. To make this work, all the bins must be delivered in the morning before the welders begin their job. This would need the use of product $Y$ every night, the need for several bins, and a sizable storage space for the full bins.

For product $Y$ to function efficiently, the two planning schedules must be on the same level. The beam scheduling has to be more exact since Product $Y^{\prime} s$ plate-specific level is fixed. This implies that the welders should have a timetable outlining the sequence in which the beams should be treated. When the beam's start time is known, the system can use a heuristic to ensure that all of the bins are sent
out at the appropriate moment. The difficult part of this scheduling part is the difference in time for a plate. Since the there are different drawers and different towers there are different times for every plates. On average a plate takes 19 seconds for a plate to be placed in the bin. There are 145 per tower so a difference in time for every specific plate.

### 2.3. Key performance indicators

Key performance indicators (KPIs) will be used to measure the performance of the dispatch method. They can indicate poor performance and improvement potential. There are KPIs from different perspectives, hence the difference in weight for one use versus the other. For the industry, it can be essential to have high overall equipment effectiveness (OEE) or minimally fixed or variable costs for the project's operation. For this research and scope, the following three KPIs have been chosen to indicate the performance of the plate sorter. It's good to know that they contradict each other.

### 2.3.1. Average waiting time for a bin

The average time a bin waits at the workplace is the first KPI for the method. This number will indicate if the total number of bins in circulation is excessively high or too low. With a long waiting time, there is a good indication of inefficient use of bins. With many bins, a big storage place is required for empty but filled bins. At the same time, a low waiting time could mean too few bins for an efficient process.

### 2.3.2. Total working time

The total working time tells how long it takes for the whole process. The chosen output method can significantly influence the order of dispatching for Product Y . This sometimes can take very long or be surprisingly short. With this KPI, an indication will be given about the efficiency of the output.

### 2.3.3. Welder pair efficiency

The welder pair efficiency indicates the worker distribution over the beams. With different schedules, some worker pairs must wait a long on the filled bins to arrive at the next beam, while others can immediately work on the next one. The efficiency percentage will indicate the productivity of the worker distribution among beams. The efficiency is calculated with the total working time of each pair and the total process time of a day.

### 2.4. Conclusion

The current beam production line is organised on a daily level. This means that which beams must be finished at the end of the day is only planned and not in which order. This is why the welders do not work in a specific order. The pairs work in random order. When a workplace is finished, they randomly pick a new workstation. All the plates destined for specific beams are manually sorted into designated bins. In the current system, this takes around 5 FTE to finish and is inefficient.

Product $Y$ is a sorting machine that optimises the product flow of plates towards the beam workplaces. With a two-input conveyor belt and one output, it is possible to store almost all the plates destined for beams and distribute them when required. There is less chance of missing plates since all the passing plates are scanned and stored in a cloud base inventory. For Product $Y$ to work efficiently, it is required to have a beam schedule. Without the knowledge of where and when which bin needs to be, the only possibility is to dispatch all the bins in the night before the welders start. This would make a very inefficient process.

To measure the performance of the overall system, there are three key performance indicators chosen:

- Average waiting time for a bin
- Total working time
- Welder pair efficiency

The next chapter will investigate planning methods from the literature.

## 3. Literature Review

The third sub-research question is answered in the following chapter: "How can Product $Y$ be improved?". Literature is reviewed to answer the three parts of this question and find a method for constructing a distribution method for Product Y. To establish a successful distribution strategy, a significant amount of data from Company $X$ must be examined and processed during the research. Some process decisions must be made to find a good distribution scheme. This will be divided into three different parts. The first part will discuss the order of beams that are used. Many businesses tend to use daily planning and are not beam-specific. A beam-specific plan cannot be made arbitrary; a priority rule for a parallel scheduling problem is required to create an order that makes sense. Second, a priority rule for the plates as a single machine scheduling problem is necessary. This is essential because the difference between a well-performing and a poorly performing distribution schedule can be made here. Finally, a model is needed to evaluate the priority rules for the operation. The production line needs to be recreated in a model to check the validity and reliability of the model.

### 3.1. Beam Planning as a parallel scheduling problem

It is required to know where all the beams will be located and when the welders will start working on a specific type. For a good distribution schedule for Product $Y$, the current daily schedule needs to be overhauled and made into a beam-level plan. Once this is created, there will be more details on the welders working schedule.

The company has indicated that beam planning is not the most critical part of the research. This is because this will be a machine that is sold to other companies. Every company will have a different way of planning their beams. With the preference the decisions are made to not apply a stochastic distribution on the process times on beams. The main focus will be on the scheduling problem of Product Y. From this information, only a few priority rules that are simple to work with and easy to calculate will be chosen.

The data provided by Company $X$ gave three main variables, the number of beams, the number of workers and the processing time of each beam. Using this as starting point, it is possible to use the approach of a parallel machine-scheduling. The book Planning and Scheduling (Pinedo, 2009), talks about jobs and machines for a parallel scheduling problem. there are M number of machines for J numbers of jobs. The machines can be seen as the welder pairs and the jobs are the beam assemblies. Every job can be assigned over each machine which makes it reasonably easy. Unfortunately, due to the lack of data, only a few priority rules can be chosen with the process times. In the book of Pinedo, there are several dispatching rules explained. Not all of them apply to this situation because not most of these priority rules require more variables used.

There are two priority rules based on processing time. The first would be the Shortest Processing Time (SPT). "This has been shown to minimise the average number of jobs waiting for processing" (Pinedo, 2009). This rule solely looks at the processing time. The welder pairs all have zero jobs assigned. Team number one or machine one takes the job with the lowest processing time. Then the second pair gets the next lowest. When all the pairs have one job assigned, the process starts again at team one. This goes on until all the jobs are assigned.

The opposite of the SPT rule would be the Longest Processing time (LPT). "This rule orders the jobs in decreasing order of processing times. When there are machines in parallel, this rule tends to balance the workload over the machines." (Pinedo, 2009). The smaller jobs can be kept for the final few in this method. Since these are shorter, it is easier to balance out the differences made by the longer jobs in
the beginning. The execution of this rule is like the SPT. All pairs start at zero jobs assigned. The first welders get the longest-taking job, and the second team will get the second-longest job. This process continues until all the jobs are equally assigned among the teams.

The Service In Random Order (SIRO) rule is the last priority rule applicable to this situation. This the rule that is used in the current system. Whenever a station is free, the next job will be assigned randomly. As mentioned earlier, this is a system that many companies use to plan the beams among workplaces. From this point of view, it will be a good experiment to compare the current dispatching system to the potential other rules.

### 3.2. Plate Planning as a single machine scheduling problem

The next step in the process would be to determine a dispatching order for Product Y. Where the beam scheduling problem was a parallel machine scheduling problem, the scheduling for Product $Y$ is a single machine problem. Here, only one machine needs to execute all the given jobs for one day. This schedule aims to make a dispatching schedule that makes the production day more efficient. Since there is only one machine, knowing how long each beam takes and when the welders start working on a particular beam is essential. It is known how long a particular beam takes to be processed. The setup time for product $Y$ can be calculated since it is known how many plates need to be drawn from the storage. Finally, it is now known when bins are required at the workplace. To summarise this, three variables can be used for applying priority rules to the dispatching: the processing time, the setup time and the due date of each beam.

The first priority rule is already used for the beam problem, the Shortest Processing Time rule (SPT). The order is evaluated on the processing time of the beams increasing from lowest to highest.

The second rule will be dependent on the due times off all beams. It is called the Earliest Due Date (EDD). The rule has the due date as an output value. For every beam, there will be a time when the bin is required. This means the first couple of bins will be required at time zero. Here the welders will start working, and the beams must be present. The due date for the next bin is when the pair is finished with the beam. They will start on the next beam, at that moment the next bin should be at the workplace. The EDD rule tends to minimise the maximum lateness among the welders waiting for a bin (Pinedo, 2009). This means the welders will not wait too long to go to the next bin.

The last rule applied to the plates will come from the last variable available, the setup time. The Shortest Setup Time (SST) will look at the time a bin takes to prepare. As mentioned earlier in the report, not all plates will fit in Product $Y$. This dispatching rule will maximise the early throughput of bins, so there is a large buffer of bins available at the beginning of the day.

### 3.3. Evaluation

After applying the different priority rules on beam and bins order, there are nine combinations of rules for the parallel and single machines scheduling problems. The outcome will be an order for Product Y. With only the order, there is nothing to say about it. It is impossible to say if the rule combination is better than the current situation or another combination. To process the stochasticity in plate moving and testing the rules, an evaluation of the performance is required. As mentioned earlier, the company provides data on a particular day. There is much variability with all the different calculations and orders in the data combining two different rules with a certain level of dependence. The components of the two will have a significant effect on each other.

The book, The Practise of Model Development and Use (Robinson, 2014) talks about how simulation models can model this complexity. To find out how the different Priority rules and stochasticity of picking up plates are performing, simulation research will be conducted. A simulation is defined as "experimentation with a simplified imitation (on a computer) of an operations system as it progresses through time, for better understanding and/or improving that system." (Robinson, 2014).

Company $X$ does not collect data on specific beam throughput. So, it is not possible to make a simulation model on the average. This means that data from the past will be used for the simulation. If the data for a specific day is given, it is possible to make a discrete-event simulation (Robinson, 2014). A discrete-event simulation works with states and events. The bins that need to be distributed at the beginning of the day are a collection of variables, all used at a specific moment. The data acquired from the beam and plate schedule makes evaluating this process in a simulation possible.

### 3.4. Conclusion

The literature review was required to find the answers for the three parts of sub-question 3. For Product $Y$ to function properly, a beam order is required. From literature, three Priority rules can be applied:

- Shortest Processing Time (SPT)
- Longest Processing Time (LPT)
- Service in Random Order (SIRO)

After finding the different beam rules, it was time to search for the appropriate rules for the single machine scheduling problem. With the data provided by the Company, it became clear that three variables can be used: Processing time, due date and setup time. With the possibility to use these three, there were three priority rules chosen from the literature:

- Shortest Processing Time (SPT)
- Earliest Due Date (EDD)
- Shortest Setup Time (SST)

A method was needed to evaluate these combinations of rules in the last part of the literature review. The book of Robinson showed that a simulation would be a good tool to try all the different priority rules combinations.

## 4.Simulation Model

The fourth research question will be addressed in Chapter 4: "How can a model help the distribution method of Product Y?" A simulation is required to identify improvements to the distribution system. Several strategies will be examined to determine which type of distribution can help enhance the performance of Product Y. This part will look at the input data, establish the model setup and various strategies that may be used to enhance the performance of Product Y .

### 4.1. Data preparation

The existing logistical process may be looked at with the aid of Company $X$ and the data provided. Quantitative data analysis has been used to prepare the data for importation into the model. It became evident throughout the company's daily throughput inspection that there is significant daily variety in demand. Every day will be different from the one before it. Because averages cannot be taken in such a specialised business, producing an "average day" will be exceedingly challenging.

As a result, it was challenging to decide whether to use an average with a wide range of values or a single day as a sample group and base the rest of the investigation on this sample. In agreement with the company's wishes, the decision has been taken to look at just one day of data and use the distribution method.

Table 1 Example of the bill of material


Microsoft Excel has been used to prepare the data. Table 1 shows an example with three beams (K37, K38 and K40) and all the plates (all letters P with a number behind) that need to be attached. The company prepares a bill of materials for the whole day that details the hours needed to finish the daily plan. Numerous beams in the data table were unrelated to Product $Y$ and the logistical processing of the beams. This filtering process was completed after the irrelevant beams had been manually removed. The drawers of Product $Y$ have specific dimensions. As a result, not all plates can be kept inside the tower.

Table 2 Number of plates per beam handled by Product $Y$

| e 100 | \#plates 100 Phase 101 | \#plates 101 | Phase 102 | \#plates 102 | Phase 103 | \#plates 103 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| K28 | 13 K231 | 50 | K14 |  | K7 | 33 |
| K37 | 15 K232 | 33 | K194 |  | K9 | 40 |
| K38 | 13 K 296 | 46 | K195 |  | K11 | 37 |
| K40 | 9 K 297 | 47 | K196 | 2 | K267 | 35 |
| K42 | 13 K 311 | 33 | K197 |  | K308 | 37 |
| K62 | 16 K 317 | 35 | K198 |  | K311 | 33 |
| K183 | 3 L4 |  | K199 |  | L4 | 3 |
| K184 | 3 L35 |  | 3 K 200 |  | L7 | 0 |
| K187 | 3 L36 |  | 5 K201 |  | L37 | 2 |
| K188 | 3 L37 | 2 | K237 |  | L41 | 3 |
| K192 | 2 L41 |  | K238 |  | L78 | 0 |
| K193 | 2 L 78 |  | K293 | 45 | L81 | 7 |
| K239 | 2 L158 |  | K294 | 44 | L158 | 0 |
| K257 | 2 L 217 |  | K310 | 32 | L188 | 3 |
| K290 | 4 L 221 | 4 | K312 | 34 | L216 | 4 |
| K291 | 4 L279 |  | K314 | 37 | L217 | 4 |
| K295 | 42 L280 |  | L7 |  | L220 | 4 |
| K306 | 33 L313 |  | L37 |  | L222 | 4 |
| L3 | 2 L318 |  | L78 |  | L280 | 0 |
| L8 | 0 L344 | 9 | L158 | 0 | L313 | 0 |
| L14 | 8 L347 |  | L161 |  | L314 | 0 |
| L16 | 4 L361 |  | L193 |  | L321 | 2 |
| L17 | 6 L367 |  | L195 |  | L322 | 2 |
| L18 | 6 L370 |  | L196 |  | L344 | 9 |
| L19 | 4 L372 |  | L216 |  | L370 | 3 |
| L23 | 0 L382 |  | L313 |  | L384 | 2 |
| L24 | 4 L390 |  | L315 |  | L393 | 3 |
| L80 | 7 L394 |  | 4 L345 |  | L416 | 5 |
| L147 | 16 L418 |  | L350 |  | L418 | 3 |
| L155 | 19 L419 |  | L370 |  | L419 | 3 |
| L159 | 0 L422 |  | L371 |  | L422 | 4 |
| L163 | 0 L440 |  | L392 |  | L440 | 3 |
| L164 | 0 L441 |  | L393 |  | L441 | 3 |
| L192 | 2 L 442 |  | L416 |  | L476 | 3 |
| L202 | 0 |  | L417 | 5 |  |  |
| L244 | 4 |  | L420 | 4 | , |  |
| L253 | 3 |  | L424 | 4 | 4 |  |
| L254 | 3 |  |  |  |  |  |
| L257 | 10 |  |  |  |  |  |
| L258 | 8 |  |  |  |  |  |
| L281 | 0 |  |  |  |  |  |
| L316 | 0 |  |  |  |  |  |
| L319 | 2 |  |  |  |  |  |
| L330 | 2 |  |  |  |  |  |
| L334 | 2 |  |  |  |  |  |
| L403 | 0 |  |  |  |  |  |

The large plates had to be removed to create a clean dataset with only the plates for Product $Y$ and determine the beams process time. To determine the sorting machine's and the beams' respective processing times, both types of data were necessary. The setup time for Product Y was determined using the data with just the plates, the process times for each beam were determined using the data set with all plates. Table 2 shows the number of plates per beam handled by the sorting machine. Some of these beams have zero plates. This means that all the plates are too big to handle by the machine. As a result of the data cleaning of the company, it was possible to calculate the average process time for a beam which can be used for the next part.

### 4.2. Conceptual model

A conceptual model is used to overview the process that needs to be integrated into the simulation. All the steps that are made during the simulation will be described in the model. Next, a general overview of the simulation also gives an idea of the different steps the user needs to go through to get to the final result of the simulation. Since different steps need to be made in the data cleansing part, a larger model is required with more than only the parts executed in the simulation. Figure 8 gives an overview of this process.


Figure 8 Conceptual framework

### 4.3. Scheduling algorithm

There are two different kinds of scheduling problems used in the simulation models. It is known how long each beam will process after the data for the beams has been collected. Two distinct priority rules are be applied from here to the beam order. As previously noted, the shortest process time and longest process time methods are employed for the beams. Additionally, beams are used in a random sequence. The order of the present beams can be regarded as random because it is not planned. It is, therefore, comparable to the actual scenario.

Table 3 Beam priority rules.

| Beam priority rules | Objective |
| :--- | :--- |
| Shortest Processing Time (SPT) | Distribute increasingly on the processing time of beams |
| Longest Processing Time (LPT) | Distribute decreasingly on the processing time of beams |
| Service in Random Order (SIRO) | Random distribution over welders |

The priority rules on the single machine scheduling problem are be applied to the plates once the beams are divided over all the workplaces. There will be a working order for the welders. From this moment, the bins filled with plates must be prepared for the beams. Here there will be three different priority rules applied towards the Product $Y$ distribution: shortest process time, shortest setup time and earliest due date. With these rules, it will be possible to evaluate the different strategies for the machine.

Table 4 Plate priority rules

| Plate priority rules | Objective |
| :--- | :--- |
| Shortest Processing Time (SPT) | Distribute increasingly on the processing time of plates |
| Earliest Due Date (EDD) | Sort on increasing due date for bins |
| Shortest Setup Time (SST) | Sort on increasing setup time for bins |

### 4.4. Discrete event simulation

A simulation is the chosen method for our experiments. It involves simulating processes by focusing on specific events and skipping the time between them instead of continuously simulating (Robinson, 2014). Each event triggers actions and can lead to the planning of future events. In this case events are used to represent the arrival of jobs at buffers, completion of jobs, filling of workstations, movement of jobs, and events for initialisation purposes. All the priority rules are applied in excel. This means that as an output from here, there is a good overview of where which beam should go. This has been transformed into a plant simulation input template. Here the evaluation in Plant Simulation starts.

First, the Excel template can be copied and inserted into the plant simulation (Figure 9). The DataTable, ProductDataBase and ProcessTimes are used for input. These will be read out to determine the beam process times, the number of plates that must be put in the bins and the destination.


Figure 9 Simulation Model
The simulation starts at 6:00 AM with the distribution of bins to the buffer area and a total of 50 bins in circulation. At 7:00, these bins will be divided over the workplaces. The welder pairs start working at 7:30. When welders are done with a workplace, they will head to the following workplace in the schedule to start working.

When the whole simulation is finished, the data of all the bins is stored in BinsData. Here the time leaving Product $Y$, arrival time at the workplace, leaving time at the workplace and waiting time at the workplace are stored. This table shows that the average waiting time of a bin at the workplace can be calculated, and the total simulation time is noted. The total simulation time is not equal to the total working time. The time between the start of distribution and the starting moment of the welder pair first needs to be subtracted from the total simulation time. Once this is calculated, the total working time is also acquired.

Lastly, the welder efficiency needs to be exported from the simulation model. This can be done via the WorkerEfficiency widget. The average working, waiting and walking time is exported into a pie chart. This whole process is stated in Figure 10, where the flow chart of the steps is put together.


Figure 10 Simulation Flow

### 4.5. Validation and verification

The validity of a simulation model depends on whether the model is a good representation of the actual system. By staying in touch with the company and making sure all the choices and presumptions were accurate, the validity was confirmed. The conceptual model and the simulation matched up against each other. These decisions and meetings ensured that it was possible to validate the model.

In this discrete event simulation, most data are a constant. From the data, the processing times are constant and will not change during the test. The same is true for the transportation speed of the Bins and workers. These will not change during the simulation and the replications. The only thing where a difference can occur is the dispatching speed of Product Y. On average, it will take between 14 and 24 seconds with a normal distribution to take out a plate from the drawer and place it into the bin. However, a plate can be placed in the top or bottom drawer, which can be a difference in the dispatching speed.

From this knowledge, the decision has been made to make five runs for every different combination of rules. This means that with nine different combinations of rules, there are 45 simulations to be executed and investigated for the data.

The verification of the model was more complex than the validation. Since the machine is not in use yet, comparing the simulation output to real-world data is challenging. It was only possible to get a sense of the real-world output by using a random beam order since that is also happening in real-time. Nevertheless, no factual verification is possible for the distribution of Product $Y$ in the real world since the machine has no real-time data about the performance.

### 4.6. Conclusion

In this chapter, the possibilities of the simulation model were investigated, and how it can help the distribution method of Product Y . With the data provided by Company X, it was possible to calculate the processing time for every beam. This meant a beam priority rule could be applied to the beams.

The beam scheduling problem is dependent on the processing time of a beam. Determining a beam schedule introduces two new variables in the data, setup time and due date. This created possibilities to make a new Product Y dispatch schedule.

This schedule can be implemented in the Plant simulation where the values are processed, and every beam gets its own process time and number of plates. Here the welders' pair will start working. Once the simulation is finished, the simulation will give values for the three KPIs.

## 5. Computational results and analysis

The outcomes of the various rule combinations are be analysed and compared with reality in this chapter. These outcomes will answer sub-question 5: "How do the applied priority rule combinations perform? The experiment's setup will be described in the first part, and the various phases will be added to get the outcome. Following the introduction, Section 5.2 will study and compare the outcome to the existing performance. The various rules combinations will be looked at and assessed in Section 5.3. In the last part, there will be a conclusion to this chapter.

### 5.1. Experiment setup

It was essential to design and conduct several tests to determine how well the chosen rule combinations performed. The chosen data was significant to start. The placement of the beams must be determined in the next step. Scheduling techniques can then be used to construct an order of dispatch for Product Y. As a result, there are now nine separate experiments that need to be conducted. The most effective combination will then be selected, and the logistical process's parameters will be tested with a sensitivity analysis.

### 5.1.1. Data set

Company $X$ provided data for this experiment. Since the daily output varies drastically, it is inaccurate to estimate an average day. Instead, an average number of beams with a matching number of plates as input is used. As was already explained, this experiment uses data from one particular day. The company has decided to look for a day with a workload equivalent to the preceding days. The information for March 10, 2023, has been gathered from this search. This equates to four phases of steel, with each phase being a truckload of beams.

### 5.1.2. Current Performance

The current performance of Product $Y$ is different compared evaluation of the machine. Within the current supply chain, the machine is not used. All the bins are manually sorted beforehand and delivered to the workplace when required. In reality, there is no data available for the waiting time of a bin or the total production time. The solution to this problem is to simulate the reality in the simulation.

To replicate the reality in the model, the most essential part is to prepare all the bins before the days start. To make this possible, the number of bins needed to be equal to the number of beams, and the starting time needed to be early enough so all the bins could be dispatched before 07:30 when the employees would start their shift. This meant the starting time of the simulation was set to 23:00 to recreate this situation. Since the beams are randomly ordered, the simulation was executed five times with a different order of randomly created beams.

Table 5 Current situation performance

| Key Performance Indicator | Output value $(\mathbf{n}=\mathbf{5})$ |
| :--- | :--- |
| Number of bins | 123 |
| Starting hour | $23: 00$ (a day earlier) |
| AvgWaitingTime | $1: 26: 56.3$ |
| TotalProcessTime | $18: 25: 19.6$ |
| TotalWorkingTime | $09: 55: 19.6$ |
| Welder Working (\%) | 67.5 |
| Welder Walking (\%) | 0.6 |
| Welder Waiting (\%) | 31.9 |

In Table 5, the performance of the current situation can be seen. Here the three most important values are the average waiting time, total working time and the percentage of time the welders work. This data indicates the upcoming experiments to understand better what these rule combinations will have to influence the total time.

### 5.1.3. Beam scheduling

As previously indicated, this experiment combines the parallel and single machine scheduling problems for two stages of the logistical process. The scheduling procedure will start with the beams. The processing time for each beam may be retracted from the data set. The shortest process time and longest process time method can be introduced based on this data.

Fifty workplaces must share 123 beams, meaning there are 23 workplaces with three beams and 27 with only two beams. This is from the perspective of the availability of workplaces. When considering the employees' sides, 25 pairs of two workers are available. This indicates that two groups will finish four beams, and 23 will work on five. A random distribution of beams has been created, as seen in Table 5 and Table 6.

The welder pair distribution is used to apply the priority rules on the next step. When a duo has finished at one location, they move on to the following location to work on the next allocated beam. The workplace distribution is a simulation of the 50 workplaces in real life.

The first rule applied on the beams was the shortest process time. This strategy rule states that all the jobs are divided over the workplaces, which increases processing time. Essentially, this means the data table is sorted and, from here, divided over the welders. This would put the welders in a position where they would work on the shortest beams first and switch to a new bin reasonably quickly. As a result, new bins should arrive soon enough for the welders to avoid waiting.

The second ordering approach makes use of the longest processing time. In this case, the first rule's reverse would be appropriate. The information is ordered in order of decreased processing times. Where the most extended beams are used to begin welding, this implies that while the welders are at work, Product Y can construct a type of buffer.

The last rule would be applicable in the current situation. As indicated in Chapter 2, the beams are now randomly distributed among the workstations between 07:00 and 07:30. To simulate this scenario. It was decided to randomly distribute the beams throughout the workspaces and see how this order would be carried out.

| Table 5 Workplace distribution 1 L334K238 L347 |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 11 \\ & 2 \end{aligned}$ | L334K |  | $\frac{\mathrm{L} 347}{\mathrm{~L} 361}$ | WelderPair | 1 | 2 | 3 | 4 | 5 |
| 3 | L382 L | L345 | L418 | 1 | L334 | K238 | L347 | L390 | L155 |
| 4 | L37 | L81 | L419 | 2 | L37 | L193 | L361 | L394 | K62 |
| 5 | L37 | L321L | L350 | 3 | L382 | L345 | L418 | L422 | K38 |
| 6 | L384 L | L322 L | L392 | 4 | L37 | L81 | L419 | L216 | K42 |
| 7 | K192 L | L370 L | L393 | 5 | L37 | L321 | L350 | L420 | K37 |
| 8 | K193 L | L372 | L41 | 6 | L384 | L322 | L392 | L424 | K310 |
| 10 | K257 L | L441 | L188 | 7 | K192 | L370 | L393 | L216 | K306 |
| 11 | L3 | L442 L | L393 | 8 | K193 | L372 | L4 | L217 | K232 |
| 12 | L80 L | L370 | L418 | 9 | K239 | L440 | L41 | L220 | K311 |
| 13 | L192 | L371 | L419 | 10 | K257 | L441 | L188 | L222 | K14 |
| 14 | L319 L | L370 L | L476 | 11 | L3 | L442 | L393 | L344 | K311 |
| 15 | L330 L | L440K |  | 12 | L80 | L370 | $\llcorner 418$ | L422 | K312 |
| 17 | K194 | K183 | L16 | 13 | L192 | L371 | L419 | L36 | K317 |
| 18 | K195 K | K184 | L19 | 14 | L319 | L370 | L476 | L367 | K7 |
| 19 | K196 K | K187 | L24 | 15 | L330 | L440 | K290 | L416 | K267 |
| 20 | K197 K | K188 | L244 | 16 | L318 | L441 | K291 | L417 | K314 |
| 21 | K198 L | L253 | L217 | 17 | K194 | K183 | L16 | L416 | K308 |
| 22 | K199 L | L254 | L221 | 18 | K195 | K184 | L19 | L14 | K11 |
| 24 | K201 | L35 |  | 19 | K196 | K187 | L24 | L17 | K295 |
| 25 K | K237 | L41 |  | 20 | K197 | K188 | L244 | L18 | K9 |
| 26 | L390 L | L155 |  | 21 | K198 | L253 | L217 | K28 | K294 |
| 27 | L394 | K62 |  | 22 | K199 | L254 | L221 | L257 | K293 |
| 28 L | L422 | K38 |  | 23 | K200 | L4 | L344 | L258 | K296 |
| 29 | L216 | K42 K 37 |  | 24 | K201 | L35 | K40 | K297 | K296 |
|  | L424 | K310 |  | 25 | K237 | L41 | L147 | K231 |  |

### 5.1.4. Plate Scheduling

From the three scenarios created in the previous section, the next step is applying the different methods on the bins destined for the beams. At every moment, there will be 25 pairs working on the beams. These pairs all start working at 07:30 AM. Because Product $Y$ can only dispatch one bin at a time, it is essential to create an ordering strategy. In the previous part, the order was created. This means the due date for every beam is known, and so is when every bin should be dispatched. Every bin also has a specific setup time. This is calculated with the number of plates dispatched from the sorting machine. For this day chosen there is a total of 930 plates to divided over the 123 beams. The dispatched time of one plate will take between 14 and 24 seconds with a normal distribution. From this number, it is also possible to consider the setup time for the priority rule. The following three priority rules have been applied to product $Y$ dispatched schedule from all this data. All these numbers are noted from the beam rules and placed into a table to determine the plate order. Table 7 is an example of this data.

Table 7 Data for plate priority rules

| BeamID | Due date(Seconds) - | Process time(Seconds) | Setup times(Seconds) |
| :---: | :---: | :---: | :---: |
| L384 | 2291 | 2291 | 0 |
| L382 | 2291 | 2291 | 0 |
| L37b | 2291 | 2291 | 0 |
| L37a | 2291 | 2291 | 0 |
| L37 | 2291 | 2291 | 0 |
| L334 | 2291 | 2291 | 0 |
| L442 | 5757 | 3447 | 0 |
| L441a | 5757 | 3447 | 0 |
| L441 | 5757 | 3447 | 0 |
| L440a | 5757 | 3447 | 0 |
| 1440 | 5757 | 3447 | 0 |
| L372 | 5757 | 3447 | 0 |
| L371 | 5757 | 3447 | 0 |
| L370b | 5757 | 3447 | 0 |
| L370a | 5757 | 3447 | 0 |
| L370 | 5757 | 3447 | 0 |
| K193 | 2310 | 2310 | 19 |
| K192 | 2310 | 2310 | 19 |
| L41 | 5776 | 3466 | 19 |
| L35 | 5776 | 3466 | 19 |
| L392 | 8068 | 3466 | 19 |
| L361 | 8068 | 3466 | 19 |
| L476 | 9223 | 3466 | 19 |
| L41a | 9223 | 3466 | 19 |
| L393a | 9223 | 3466 | 19 |
| L393 | 9223 | 3466 | 19 |
| L394 | 12688 | 4621 | 19 |
| L390 | 12688 | 4621 | 19 |
| L80 | 2310 | 2310 | 38 |
| L330 | 2310 | 2310 | 38 |
| L319 | 2310 | 2310 | 38 |
| L318 | 2310 | 2310 | 38 |
| L3 | 2310 | 2310 | 38 |
| L192 | 2310 | 2310 | 38 |
| K257 | 2310 | 2310 | 38 |
| K239 | 2310 | 2310 | 38 |
| K237 | 2310 | 2310 | 38 |
| K201 | 2310 | 2310 | 38 |
| K200 | 2310 | 2310 | 38 |
| K199 | 2310 | 2310 | 38 |
| K198 | 2310 | 2310 | 38 |
| K197 | 2310 | 2310 | 38 |
| K196 | 2310 | 2310 | 38 |
| K195 | 2310 | 2310 | 38 |
| K194 | 2310 | 2310 | 38 |
| L81 | 4602 | 2310 | 38 |
| L345 | 4602 | 2310 | 38 |

The first priority rule is based on the shortest process time. The beam scheduling already uses this rules, and the plate's principle is unchanged. All the beams are sorted in increasing process time, and the shortest processing times are chosen first. For this method the data acquired by the beam scheduling is not required.

Since the due date is available for every beam, the earliest due date method is also possible. The data is sorted on every due date, and the required bin is chosen and distributed.

Lastly, the shortest setup time for the bins is used for the order strategy. This rule uses the number of plates stored in the machine to calculate the setup time. This can differ per beam because sometimes there are plates which are too big for the machine but are considered for the total process time of the beams.

### 5.1.5. Parameters

Within the simulation, some parameters can be changed during the execution of the simulation. The primary essential parameters are the number of bins in circulation and the starting moment of distribution.

The number of bins can be changed in the simulation. This may influence the average waiting time for a bin at a station or welders at a workplace. The starting time for the sorting machine can also be adjusted. The earlier this starts, the more bins can be prepared before the welders start work. Of course, this moment also depends on the number of bins in circulation because the starting moment is very early. However, if there are not enough bins in circulation, this machine will stand still.

### 5.2. Experiment Results

In this section, the results of the different experiments will be discussed. First, the current situation of Company X will be evaluated, and after the different variants of methods. Once the best priority rule combinations are found, a small sensitivity analysis will be executed to determine how the parameter difference impacts the combination.

### 5.2.1. Evaluation of Scheduling rules

In this section, all the different priority rule combinations are be evaluated. During the nine experiments, the starting hour is fixed at 6:00 AM, and the number of bins in circulation is set to 50 . After these experiments, different values will be investigated with a sensitivity analysis where the values for the starting hour and the number of bins will be changed.

## Shortest Processing Time (SPT) beam order

The due dates of the first beams are zero. This is set to zero because the bins are required when the welders start working. If the clock hits 7:30 AM and the welders pair start working, the bins should already be stationed at the workplace. With this data acquired, applying the rule to the bins dispatched is possible. This resulted in the orders shown in Table 6.

Table 6 Plate priority rule performance values (SPT)

| Beam priority rule: | Current situation | Beam priority rule: | SPT | Beam priority rule: | SPT | Beam priority rule: | SPT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plate priority rule: | Current situation | Plate priority rule: | SPT | Plate priority rule: | EDD | Plate priority rule: | SST |
| AvgWaitingTime: | 1:26:56.3 | AvgWaitingTime: | 7:49.9 | AvgWaitingTime: | 7:18.9 | AvgWaitingTime: | 9:10.2 |
| TotalProcessTime: | 18:25:19.6 | TotalProcessTime: | 15:56:53.2 | TotalProcessTime: | 15:18:22.8 | TotalProcessTime: | 15:59:19.2 |
| TotalWorkingTime | 09:55:19.6 | TotalWorkingTime | 14:26:53.2 | TotalWorkingTime | 13:48:22.8 | TotalWorkingTime | 14:29:19.2 |
| Welder Working\% | 67.5 | Welder Working\% | 58.3 | Welder Working\% | 58.2 | Welder Working\% | 58.2 |
| Welder Walking\% | 0.6 | Welder Walking\% | 0.6 | Welder Walking\% | 0.6 | Welder Walking\% | 0.6 |
| Welder Waiting\% | 31.9 | Welder Waiting\% | 41.1 | Welder Waiting\% | 41.2 | Welder Waiting\% | 41.2 |

It can be seen from table 7 that the average waiting time for a bin drastically decreases with the implementation of SPT compared to the current situation. These values have decreased to around 8 minutes per bin, while previously, this time was around one and a half hours. On the other hand, the total time for production has increased by more than three to four hours for each plate rule. Moreover, for the last rule, the efficiency of the welders is the same. The percentage of time the welders are working has decreased by around 9 percent.

## Longest Processing Time (LPT) beam order

With the LPT beam rule, the three plates' rules were applied to the beams. This resulted in the performance in Table 9.

Table 7 Plate priority rule performance values (LPT)

| Beam priority rule: | Current situation | Beam priority rule: | LPT | Beam priority rule: | LPT | Beam priority rule: | LPT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plate priority rule: | Current situation | Plate priority rule: | SPT | Plate priority rule: | EDD | Plate priority rule: | SST |
| AvgWaitingTime: | 1:26:56.3 | AvgWaitingTime: | 44:38.1 | AvgWaitingTime: | 45:50.7 | AvgWaitingTime: | 10:17.0 |
| TotalProcessTime: | 18:25:19.6 | TotalProcessTime: | 14:55:51.3 | TotalProcessTime: | 10:52:42.5 | TotalProcessTime: | 15:59:19.2 |
| TotalWorkingTime | 09:55:19.6 | TotalWorkingTime | 13:25:51.3 | TotalWorkingTime | 9:22:42.5 | TotalWorkingTime | 14:29:19.2 |
| Welder Working\% | 67.5 | Welder Working\% | 58.3 | Welder Working\% | 73.3 | Welder Working\% | 58.2 |
| Welder Walking\% | 0.6 | Welder Walking\% | 0.6 | Welder Walking\% | 0.7 | Welder Walking\% | 0.6 |
| Welder Waiting\% | 31.9 | Welder Waiting\% | 41.1 | Welder Waiting\% | 25.9 | Welder Waiting\% | 41.2 |

The table shows that the average waiting time decreases halves for SPT and EDD, and the SST decreases to only approximately 10 minutes per bin. For the total working time, it can be seen that for SPT and SST, the value increases by at least three and a half hours. While for the earliest due date rule, the total working time decreases. The main surprise is the welder efficiency for the EDD method. Here an increase of around 6 percent can be seen compared to the current situation.

## Random beam order

For the last experiment, the current situation of beam division is investigated. In a typical situation, the beams are randomly distributed over the workplace. With this experiment, the goal is to keep this system. Nevertheless, the difference now applies a method to the plate dispatched and sees the influence. For this experiment, five different beam orders are used. The three plate rules are applied, and an average is taken for the output values. The order and values for processing time and the due date can be seen for one of the five experiments in Appendix $C$ to indicate the randomiser's influence on the data.

Table 8 Plate priority rule performance values (random $n=5$ )

| Beam priority rule: | Current situation | Beam priority rule: | Random | Beam priority rule: | Random | Beam priority rule: | Random |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plate priority rule: | Current situation | Plate priority rule: | SPT | Plate priority rule: | EDD | Plate priority rule: | SST |
| AvgWaitingTime: | 1:26:56.3 | AvgWaitingTime: | 08:27 | AvgWaitingTime: | 03:43.8 | AvgWaitingTime: | 09:11.8 |
| TotalProcessTime: | 18:25:19.6 | TotalProcessTime: | 15:53:21.6 | TotalProcessTime: | 13:03:37.2 | TotalProcessTime: | 15:49:39.8 |
| TotalWorkingTime | 09:55:19.6 | TotalWorkingTime | 14:23:21.6 | TotalWorkingTime | 11:33:37.2 | TotalWorkingTime | 14:19:39.8 |
| Welder Working\% | 67.5 | Welder Working\% | 58.3 | Welder Working\% | 62.7 | Welder Working\% | 58.2 |
| Welder Walking\% | 0.6 | Welder Walking\% | 0.6 | Welder Walking\% | 0.6 | Welder Walking\% | 0.6 |
| Welder Waiting\% | 31.9 | Welder Waiting\% | 41.1 | Welder Waiting\% | 36.7 | Welder Waiting\% | 41.2 |

The results (Table 10) show that the waiting times for bins have dropped below ten minutes for all combinations. For the total production times, EDD performs the best of the three, with 11 hours and 33 minutes. This also is the case for efficiency, where EDD is the only one reaching a percentage over 60 percent.

### 5.2.2. Sensitivity analysis

One priority rule combination gave a remarkable outcome from the nine different experiments outcomes. All the combinations resulted in a higher total working time except the longest processing time with the earliest due date.

This resulted in the decision for sensitivity analysis with different parameter values for the Starting time and the number of bins in circulation. The starting time values are set to 05:00 AM, 06:00 and 07:00. These were chosen because the spread in time can significantly influence the number of bins that can be prepared before the welders start their shift. The other parameter is the number of bins in circulation. The values $25,30,35,40,45,50,75$ and 100 are chosen for this parameter.

| starting hour: 05:00 |  |  |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: |
| Number of bins | 25 | 30 | 35 | 40 | 45 | 50 | 75 | 100 |  |  |  |
| AvgWaitingTime: | $0: 50.1$ | $8: 42.7$ | $18: 34.1$ | $28: 53.0$ | $39: 41.5$ | $49: 47.8$ | $1: 32: 21.5$ | $1: 59: 24.8$ |  |  |  |
| TotalProcessTime: | $11: 38: 15.4$ | $11: 20: 41.7$ | $11: 13: 51.9$ | $11: 07: 45.4$ | $11: 06: 55.9$ | $11: 06: 55.9$ | $11: 06: 55.9$ | $11: 06: 55.9$ |  |  |  |
| TotalWorkingTime | $9: 08: 15.4$ | $8: 50: 41.7$ | $8: 43: 51.9$ | $8: 37: 45.4$ | $8: 36: 55.9$ | $8: 36: 55.9$ | $8: 36: 55.9$ | $8: 36: 55.9$ |  |  |  |
| Welder Working\% | 75.3 | 77.8 | 78.8 | 79.7 | 79.8 | 79.8 | 79.8 | 79.8 |  |  |  |
| Welder Walking\% | 0.7 | 0.8 | 0.8 | 0.8 | 0.7 | 0.7 | 0.7 | 0.7 |  |  |  |
| Welder Waiting\% | 24.0 | 21.5 | 20.4 | 19.5 | 19.3 | 19.3 | 19.3 | 19.3 |  |  |  |


|  |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| Starting hour: 06:00 |  |  |  |  |  |  |  |  |  |
| Number of Bins | 25 | 30 | 35 | 40 | 45 | 50 | 75 | 100 |  |
| AvgWaitingTime: | $0: 50.7$ | $7: 59.7$ | $16: 30.6$ | $26: 46.9$ | $36: 26.7$ | $45: 50.7$ | $1: 25: 33.8$ | $1: 49: 48.9$ |  |
| TotalProcessTime: | $11: 20: 22.5$ | $11: 05: 14.4$ | $10: 59: 40.7$ | $10: 52: 42.5$ | $10: 52: 42.5$ | $10: 52: 42.5$ | $10: 52: 42.5$ | $10: 52: 42.5$ |  |
| TotalWorkingTime | $9: 50: 22.5$ | $9: 35: 14.5$ | $9: 29: 40.7$ | $9: 22: 42.5$ | $9: 22: 42.5$ | $9: 22: 42.5$ | $9: 22: 42.5$ | $9: 22: 42.5$ |  |
| Welder Working\% | 69.9 | 71.7 | 72.4 | 73.3 | 73.3 | 73.3 | 73.3 | 73.3 |  |
| Welder Walking\% | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 |  |
| Welder Waiting\% | 29.4 | 27.5 | 26.8 | 25.9 | 25.9 | 25.9 | 25.9 | 25.9 |  |


| starting hour: 07:00 |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Number of bins | 25 | 30 | 35 | 40 | 45 | 50 | 75 | 100 |
| AvgWaitingTime: | $0: 50.5$ | $7: 36.2$ | $16: 00.0$ | $26: 28.4$ | $35: 52.1$ | $44: 58.5$ | $1: 22: 29.5$ | $1: 22: 29.5$ |
| TotalProcessTime: | $11: 12: 14.4$ | $10: 58: 41.1$ | $10: 51: 44.5$ | $10: 46: 43.6$ | $10: 46: 43.6$ | $10: 46: 43.6$ | $10: 46: 43.6$ | $10: 46: 43.6$ |
| TotalWorkingTime | $10: 42: 14.4$ | $10: 28: 41.1$ | $10: 21: 44.5$ | $10: 16: 43.6$ | $10: 16: 43.6$ | $10: 16: 43.6$ | $10: 16: 43.6$ | $10: 16: 43.6$ |
| Welder Working\% | 64.3 | 65.6 | 66.4 | 66.9 | 66.9 | 66.9 | 66.9 | 66.9 |
| Welder Walking\% | 0.6 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 | 0.7 |
| Welder Waiting\% | 35.1 | 33.7 | 33,0 | 32.4 | 32.4 | 32.4 | 32.4 | 32.4 |

The results in Table 11 indicate the impact of the number of bins and the starting hour. The number of bins drastically influences the average waiting time when the number of bins is between 25 and 50 . Here the ratio of bins per welder becomes more critical. With 50 bins in circulation, would be two bins available for every worker. This means the following bins will be available for the welders when the jobs are finished. Between 25 and 50 bins, a moment comes when the bins will not arrive on time. This influences the total working time, as can be seen between 35 and 30 bins.

The starting moment of the distribution also is essential. When the bin starts distributing at 5:00, there is enough time to dispatch all the plates in the bins and get the shortest total process time. On the other hand, the earlier the distribution start, the higher the waiting time will be.

### 5.3. Conclusion

This research aims to answer the question: "How can Product Y improve the product flow towards the workplace?" This question should be answered differently to keep it interesting for various companies.

The first perspective would be the Company with no beam-specific planning. This would be the case for most of the companies. Five experiments were run for this beam order, each with a completely random beam order. From this situation, there were three results due to the randomisation of the beams. Some long beams are at the beginning, and some are at the end. The same can be said for the short-taking beams. This causes a very balanced order of beams. Hence, the beams have a short waiting time for every bin order. So that means the total working time would be looked at. From this result, the EDD was the best by far. Looking at the due date for every beam was very important to create an efficient process.

To conclude the answer to the research question from this perspective, the product flow from Product $Y$ towards the workplaces can be improved by applying the Earliest due date rule to the random order of beams.

The next step would be to look at companies planning their beams depending on some priority rule. If a company already does this, it can adjust this to an LPT or SPT rule. If there were to be chosen an priority rule combination, then that would be the LPT/EDD combinations. These were the only combinations where the total working time was lower than the current situation. After that, from the sensitivity analysis, the average waiting time for a bin could be lowered to a minimum of around eight minutes.

To answer the main research question from the beam planning company perspective. The product flow from Product $Y$ towards the workplace can be improved with the longest process time and earliest due date combinations. In this situation, the welders can start with the longer-taking beams and divide the last shorter-taking beams to balance the work. The decision can also be made to start earlier or later with distributing plates into bins. Starting at 5:00 AM, a total working time of 8 hours and 50 minutes can be achieved with only 30 beams in circulation. The side note to this solution would be that employees need to start earlier in this system which can cost more money. Also, if the machine starts earlier with the distribution of bins, more bins will be filled before the welders can start. This means a larger buffer area is required, which will also cost more space in the layout of a production hall.

## 6. Conclusion and recommendations

The main goal of this research is to help Company $X$ integrate Product $Y$ into the supply chain, not only for the Company's construction division but also to help other companies which acquire the sorting machine. In the last chapter of this research, the main findings of the experiments will be discussed, the recommendations for distribution methods, the limitations of the research, and future research on the subject.

### 6.1. Conclusion

In this research the goal was to answer the main research question: "How can Product $Y$ improve the product flow towards the workplace?". Through out the research different sub research question have been answered to come to an answered.

The first step of the research was to identify the main problem of Product Y. After investigating different problems of the machine, the core problem became clear; there is no dispatching strategy for the machine which causes a decrease in efficiency for the supply chain. The next step was the analyse this problem and see how it can be processed. The problem consists of three different parts: the beams, the bins and the place where these to come together, the workplace.

The beams have no detailed planning system which leads into no knowledge about beams specific working schedule for welders. Hence it is not possible to know when which plates are required at the workplace to be used.

The literature review research was done to find applicable order methods for the data provided by the company. For the beams a method for a parallel machine scheduling problem was needed where the only variable known is the process time. From the literature came two different priority rules. The longest and shortest process time. Next to these two a decision was made to also use a randomizer in beam order. With a beam schedule acquired the next problem to investigate was the dispatching of plates. This could be seen as a single machine scheduling problem. with the new variables due date and setup time there were three priority rules chosen: earliest due date, shortest setup time and shortest process time.

These methods required a form of evaluation. From the literature came the solution to use a discrete event simulation where the combinations of priority rules for both problems could be investigated. In the chapter 4 the simulation model is introduced and explained that evaluates these combinations.

All the priority rule combinations have given different outputs in Chapter 5 . Some of the results were similar, and some were very different. With nine combinations and a sensitivity analysis of the LPT/EDD combinations, some exciting findings must be made. There are different points of view for different companies, to be made. That is why the following sections discuss results from other perspectives.

### 6.2. Limitations

The setup of the simulation model and experiments were discussed in chapters 4 and 5 . To make a working simulation, some assumptions needed to be made and processed into the execution. This led to a couple of limitations in the research.

- The processing time of beams was calculated via the bill of material, and the hours it calculated to process the four phases. This was done by taking averages of the plates. Each plate was seen as equal and had certain times for the processing time. In this way, the total process time for
a beam was calculated. Of course, there would be differences between certain plates and how long they take to weld.
- The priority rule combinations were only applied to one daily production for this research. Due to the high variability in daily production, it was decided in agreement with the construction employees to look for an "average day". With this data, the priority rules would be executed and evaluated.
- A simulation model always brings limitations compared to reality. Product $Y$ used a normal distribution to simulate the difference in plate dispatched, but there will always be a difference. The same is true for the process times of beams. In this research, the decision was made to keep the processing time fixed and not let a distribution change the times per run. This was done because the focus was not on the beam schedule. Every Company has a unique way of planning the beams, which should be used as input to evaluate Product Y .


### 6.3. Recommendations

The gap between norm and reality has not precisely been filled. Although some reasonable beginning steps have been made, there are still some recommendations for progress. Company X wants to sell Product $Y$ worldwide to make the sorting process of plates more efficient and less influenced by human mistakes.

The implementation of Product $Y$ gives the advantage of a database with all the plates locations. When a plate did not yet arrive to the machine it will also be known, so employee can search in previous locations of the supply chain. This will increase the efficiency of welders since the problem of missing plates at the workplace will not occur anymore. If other companies want efficient machine usage, a dispatching order is required. The machine can be used as perfect storage. However, without a dispatch schedule, all the beams still need to be stored in a different area because there is no knowledge about when the bins are required.

The recommendation would be to invest in a beam ordering system. Implementing this schedule will create much knowledge for planners and how to use the machine. A detailed schedule can be made if it is known how long a sure welder works on a beam and how long a specific plate takes to be tack welded. Moreover, that is what Product $Y$ would benefit from.

### 6.4. Future Research

Product Y is a new product in the market with few competitors. Future research in the machine could create an even more efficient product flow towards the workplace and maximise the use of towers as storage areas. For this, future research should be done on more single and parallel machine scheduling problems. For this research, only three are used for product $Y$ while there are many more.

As mentioned in the limitations, this research has been executed on only one dataset for one day. It would be better to execute the research on multiple daily data sets and not one to better understand the rule combination.

In the sensitivity analysis, there was a small amount of research towards the number of bins in circulations at the starting time for the distribution of bins. The results showed that the influence of the value changes is quite significant average waiting time could be decreased from 50 minutes to around 8 minutes while the total working time only increased to around 15 minutes. A more in-depth analysis of the number of bins per working pair should give exciting results.

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## Appendices

## Appendix A: Deliverables

During this research, several preparation, calculations, and evaluation are needed. There will also be extra files for the research to give a better understanding compared to the tables and figures mentioned in the chapters and the appendix.

- Phase

From the Company, there is a daily production schedule. In this file, all the details of the beams and attachments are given. Some of the data does not apply to the research, so there is a straightforward overview of which parts are used and which are not.

- Beam and plate distribution

With the data provided by the Company, there are distributions to be made with the chosen methods. This file gives a clear overview of all the orders and the input for the simulation.

- Simulation model

A simulation model was set up in Tecnomatix Plant Simulation 16.1 to evaluate the used methods.

- Report

The report contains the different results for the evaluations that have been executed. Together with this, the overall structure of the research will be explained.

## Appendix B: Current Situation Performance

Table 10 Reality experiments

| Number of bins | 123 | Number of bins | 123 |
| :---: | :---: | :---: | :---: |
| Starting hour | 23:00 | Starting hour | 23:00 |
| AugW'aitingTime: | 55:45.99125549052 | AugWaitingTime: | 1:48:39.53016244442 |
| TotalProcessTime: | 18:40:10.4855693333 | TotalProcessTime: | 18:33:04.9402979999 |
| Total WorkingTime | 10:10:10.4855693333 | Total WorkingTime | 10:03:04.9402979999 |
| Welder Working\% | 67.6 | Welder Working\% | 68,4 |
| Welder Walking\% | 0,6 | Welder Walking\% | 0.7 |
| Welder Waiting\% | 31.8 | Welder W/aiting\% | 30,9 |
| Number of bins | 123 | Number of bins | 123 |
| Startinghour | 23:00 | Starting hour | 23:00 |
| Aug'VaitingTime: | 1:08:19.6469525149 | AugW/aitingTime: | 1:39:42.66261692835 |
| TotalProcessTime: | 18:23:07.428357 | TotalProcessTime: | 18:04:13.9044769999 |
| TotalWorkingTime | 9:53:10.4855693333 | Total WorkingTime | 9:34:13.9044769999 |
| Welder Working\% | 67,6 | Welder Working\% | 70,9 |
| Welder Walking\% | 0.6 | Welder Walking\% | 0,7 |
| Welder Waiting\% | 31.8 | Welder W/aiting\% | 28,4 |
| Number of bins | 123 | Number of bins: | 123 |
| Starting hour | 23:00 | Starting hour(hh:mm): | 23:00 |
| Aug'/aitingTime: | 1:40:19.69511415716 | Aug'WaitingTime(hh:mm:ss) | 1:26:56.333 |
| TotalProcessTime: | 18:26:02.1283589998 | TotalProcessTime(hh:mm: | 18:25:19.6 |
| TotalWorkingTime | 9:56:10.4855693333 | TotalWorkingTime(hh:mm: | 09:55:19.6 |
| Welder Working\% | 63,1 | Welder Working(\%) | 67.5 |
| Welder Walking\% | 0,3 | Welder Walking(\%) | 0,6 |
| Welder Waiting\% | 36,6 | Welder W/aiting(\%) | 31,9 |

Appendix C: Beam priority rule SPT Evaluation
Table 11 Welder pair distribution SPT

| WelderPair | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | L334 | L321 | K184 | K290 | L155 |
| 2 | L37 | L322 | K187 | K291 | K62 |
| 3 | L37a | L330 | K188 | L16 | K38 |
| 4 | L37b | L345 | L188 | L19 | K42 |
| 5 | L382 | L80 | L253 | L216 | K37 |
| 6 | L384 | L81 | L254 | L216a | K310 |
| 7 | K192 | L370 | L347 | L24 | K14 |
| 8 | K193 | L370a | L350 | L244 | K232 |
| 9 | K194 | L370b | L4 | L344 | K306 |
| 10 | K195 | L371 | L4a | L344a | K311 |
| 11 | K196 | L372 | L418 | L422 | K311a |
| 12 | K197 | 1440 | L418a | L422a | K312 |
| 13 | K198 | 1440 | 1419 | L36 | K7 |
| 14 | K199 | L441 | L419a | L367 | K267 |
| 15 | K200 | L441 | L390 | 1416 | K317 |
| 16 | K201 | L442 | L394 | L416a | K308 |
| 17 | K237 | L35 | L217 | 1417 | K314 |
| 18 | K238 | L361 | L217a | L14 | K11 |
| 19 | K239 | L392 | L220 | L17 | K295 |
| 20 | K257 | L393 | L221 | L18 | K9 |
| 21 | L192 | L393a | L222 | K28 | K294 |
| 22 | L193 | L41 | L420 | L257 | K293 |
| 23 | L3 | L41a | L424 | L258 | K296 |
| 24 | L318 | L476 | K40 | K297 |  |
| 25 | L319 | K183 | L147 | K231 |  |

Table 12 Process times and Due dates of beams SPT

| process time |  |  |  |  | due date |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2291 | 2310 | 3466 | 4621 | 11552 | 0 | 2291 | 4602 | 8068 | 12688 |
| 2291 | 2310 | 3466 | 4621 | 13863 | 0 | 2291 | 4602 | 8068 | 12688 |
| 2291 | 2310 | 3466 | 4621 | 15018 | 0 | 2291 | 4602 | 8068 | 12688 |
| 2291 | 2310 | 3466 | 4621 | 15018 | 0 | 2291 | 4602 | 8068 | 12688 |
| 2291 | 2310 | 3466 | 4621 | 17328 | 0 | 2291 | 4602 | 8068 | 12688 |
| 2291 | 2310 | 3466 | 4621 | 32346 | 0 | 2291 | 4602 | 8068 | 12688 |
| 2310 | 3447 | 3466 | 4621 | 33501 | 0 | 2310 | 5757 | 9223 | 13844 |
| 2310 | 3447 | 3466 | 4621 | 33501 | 0 | 2310 | 5757 | 9223 | 13844 |
| 2310 | 3447 | 3466 | 4621 | 33501 | 0 | 2310 | 5757 | 9223 | 13844 |
| 2310 | 3447 | 3466 | 4621 | 33501 | 0 | 2310 | 5757 | 9223 | 13844 |
| 2310 | 3447 | 3466 | 4621 | 33501 | 0 | 2310 | 5757 | 9223 | 13844 |
| 2310 | 3447 | 3466 | 4621 | 34657 | 0 | 2310 | 5757 | 9223 | 13844 |
| 2310 | 3447 | 3466 | 5776 | 35812 | 0 | 2310 | 5757 | 9223 | 14999 |
| 2310 | 3447 | 3466 | 5776 | 35812 | 0 | 2310 | 5757 | 9223 | 14999 |
| 2310 | 3447 | 4621 | 5776 | 35812 | 0 | 2310 | 5757 | 10378 | 16154 |
| 2310 | 3447 | 4621 | 5776 | 38122 | 0 | 2310 | 5757 | 10378 | 16154 |
| 2310 | 3466 | 4621 | 5776 | 38122 | 0 | 2310 | 5776 | 10397 | 16173 |
| 2310 | 3466 | 4621 | 6931 | 40433 | 0 | 2310 | 5776 | 10397 | 17328 |
| 2310 | 3466 | 4621 | 6931 | 42743 | 0 | 2310 | 5776 | 10397 | 17328 |
| 2310 | 3466 | 4621 | 6931 | 43899 | 0 | 2310 | 5776 | 10397 | 17328 |
| 2310 | 3466 | 4621 | 9242 | 45054 | 0 | 2310 | 5776 | 10397 | 19639 |
| 2310 | 3466 | 4621 | 9242 | 46209 | 0 | 2310 | 5776 | 10397 | 19639 |
| 2310 | 3466 | 4621 | 9242 | 47364 | 0 | 2310 | 5776 | 10397 | 19639 |
| 2310 | 3466 | 10397 | 48519 |  | 0 | 2310 | 5776 | 16173 |  |
| 2310 | 3466 | 10397 | 51985 |  | 0 | 2310 | 5776 | 16173 |  |

Table 13 Bin dispatch order (SPT)

| umber | Destination | SPT | EDD | SST |  |  | SPT | EDD | SST |  |  | SPT | EDD | STT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | workplace1.Beam1 | L334 | L334 | L334 | 42 | workplace17.Beam50 | K183 | K183 | L318 | 83 | workplace35.Beam92 | L344a | L244 | L216a |
| 2 | workplace2.Beam4 | L37 | L37 | L37 | 43 | workplace18.Beam53 | L35 | L35 | L319 | 84 | workplace36.Beam94 | L422 | L344 | L344a |
| 3 | workplace3.Beam7 | L37a | L37a | L37a | 44 | workplace19.Beam56 | L361 | L361 | L330 | 85 | workplace37.Beam96 | L422a | L344a | L422a |
| 4 | workplace4. Beam10 | L37b | L37b | L37b | 45 | workplace20.Beam59 | L392 | L392 | L80 | 86 | workplace38.Beam98 | L36 | L422 | L36 |
| 5 | workplace5. Beam13 | L382 | L382 | L382 | 46 | workplace21.Beam62 | L393 | L393 | K238 | 87 | workplace39.Beam100 | L367 | L422a | L367 |
| 6 | workplace6.Beam16 | L384 | L384 | L384 | 47 | workplace22.Beam65 | L393a | L393a | L193 | 88 | workplace40.Beam 102 | L416 | L36 | L416 |
| 7 | workplace7. Beam19 | K192 | K192 | L370 | 48 | workplace23.Beam68 | L41 | L41 | L321 | 89 | workplace41.Beam104 | L416a | L367 | L417 |
| 8 | workplace8.Beam22 | K193 | K193 | L370a | 49 | workplace24.Beam71 | L41a | L41a | L322 | 90 | workplace42.Beam 106 | L417 | L416 | L416a |
| 9 | workplace9.Beam25 | K194 | K194 | L370b | 50 | workplace25.Beam73 | L476 | L476 | L345 | 91 | workplace43.Beam108 | L14 | L416a | L14 |
| 10 | workplace10.Beam28 | K195 | K195 | L371 | 51 | workplace1.Beam3 | K184 | K184 | L81 | 92 | workplace44.Beam110 | L17 | L417 | 17 |
| 11 | workplace11.Beam31 | K196 | K196 | L372 | 52 | workplace2.Beam6 | K187 | K187 | K183 | 93 | workplace45.Beam112 | L18 | L14 | 18 |
| 12 | workplace12. Beam34 | K197 | K197 | L440 | 53 | workplace3.Beam9 | K188 | K188 | K184 | 94 | workplace46. Beam114 | K28 | L17 | K28 |
| 13 | workplace13.Beam37 | K198 | K198 | L440a | 54 | workplace4.Beam12 | L188 | L188 | K187 | 95 | workplace47.Beam116 | L257 | L18 | L257 |
| 14 | workplace14.Beam40 | K199 | K199 | L441 | 55 | workplace5.Beam15 | L253 | L253 | K188 | 96 | workplace48.Beam118 | L258 | K28 | L258 |
| 15 | workplace15.Beam43 | K200 | K200 | L441a | 56 | workplace6. Beam18 | L254 | L254 | L217 | 97 | workplace49.Beam120 | K40 | L257 | K40 |
| 16 | workplace16.Beam46 | K201 | K201 | L442 | 57 | workplace 7. Beam21 | L347 | L347 | L221 | 98 | workplace50.Beam122 | L147 | L258 | L147 |
| 17 | workplace17.Beam49 | K237 | K237 | K192 | 58 | workplace8.Beam24 | L350 | L350 | L420 | 99 | workplace26.Beam75 | L155 | L155 | L155 |
| 18 | workplace18.Beam52 | K238 | K238 | K193 | 59 | workplace ${ }^{\text {S }}$ Beam27 | L4 | L4 | L424 | 100 | workplace27.Beam77 | K62 | K62 | K62 |
| 19 | workplace19.Beam55 | K239 | K239 | L35 | 60 | workplace10.Beam30 | L418 | L418 | L217a | 101 | workplace28.Beam79 | K38 | K38 | K38 |
| 20 | workplace20.Beam58 | K257 | K257 | L41 | 61 | workplace11.Beam33 | L418a | L418a | L220 | 102 | workplace29.Beam81 | K42 | K42 | K42 |
| 21 | workplace21. Beam61 | L192 | L192 | L361 | 62 | workplace12.Beam36 | L419 | L419 | L222 | 103 | workplace30.Beam83 | K37 | K37 | 37 |
| 22 | workplace22.Beam64 | L193 | L193 | L392 | 63 | workplace13.Beam39 | L419a | L419a | L253 | 104 | workplace31.Beam85 | K310 | K310 | K310 |
| 23 | workplace23.Beam67 | L3 | L3 | L393 | 64 | workplace14.Beam42 | L4a | L4a | L254 | 105 | workplace32.Beam87 | K14 | K14 | 14 |
| 24 | workplace24.Beam70 | L318 | L318 | L393 | 65 | workplace15.Beam45 | L390 | L390 | L4 | 106 | workplace33.Beam89 | K232 | K232 | K232 |
| 25 | workplace25.Beam72 | L319 | L319 | L41a | 66 | workplace16.Beam48 | L394 | L394 | L347 | 107 | workplace34.Beam91 | K306 | K306 | K306 |
| 26 | workplace1.Beam2 | L321 | L321 | L476 | 67 | workplace17.Beam51 | L217 | L217 | L350 | 108 | workplace35.Beam93 | K311 | K311 | <311 |
| 27 | workplace2.Beam5 | L322 | L322 | L390 | 68 | workplace18.Beam54 | L217a | L217a | L418 | 109 | workplace36.Beam95 | K311a | K311a | K311a |
| 28 | workplace3.Beam8 | L330 | L330 | L394 | 69 | workplace19.Beam57 | L220 | L220 | L419 | 110 | workplace37.Beam97 | K312 | K312 | K312 |
| 29 | workplace4.Beami1 | L345 | L345 | K194 | 70 | workplace20.Beam60 | L221 | L221 | L188 | 111 | workplace38.Beam99 | K267 | K267 | K7 |
| 30 | workplace5. Beam 14 | L80 | L80 | K195 | 71 | workplace21.Beam63 | L222 | L222 | L4a | 112 | workplace39.Beam101 | K7 | K7 | K317 |
| 31 | workplace6.Beam17 | L81 | L81 | K196 | 72 | workplace22.Beam66 | L420 | L420 | L418a | 113 | workplace40.Beam 103 | K317 | K317 | K267 |
| 32 | workplace7. Beam20 | L370 | L370 | K197 | 73 | workplace23.Beam69 | L424 | L424 | L419a | 114 | workplace41.Beam 105 | K308 | K308 | K314 |
| 33 | workplace8.Beam23 | L370a | L370a | K198 | 74 | workplace26.Beam74 | K290 | K40 | K290 | 115 | workplace42.Beam107 | K314 | K314 | K308 |
| 34 | workplace9.Beam26 | L370b | L370b | K199 | 75 | workplace27.Beam76 | K291 | L147 | K291 | 116 | workplace43.Beam109 | K11 | K297 | K11 |
| 35 | workplace10.Beam29 | L371 | L371 | K200 | 76 | workplace28.Beam78 | L16 | K290 | L16 | 117 | workplace44.Beam111 | K295 | K231 | K295 |
| 36 | workplace11.Beam32 | L372 | L372 | K201 | 77 | workplace29.Beam80 | L19 | K291 | L19 | 118 | workplace45. Beam113 | K9 | K11 | K9 |
| 37 | workplace12.Beam35 | L440 | L440 | K237 | 78 | workplace30.Beam82 | L216 | L16 | L24 | 119 | workplace46.Beam115 | K294 | K295 | K294 |
| 38 | workplace13.Beam38 | L440a | L440a | K239 | 79 | workplace31.Beam84 | L216a | L19 | L244 | 120 | workplace47.Beam117 | K293 | K9 | K293 |
| 39 | workplace14.Beam41 | L441 | L441 | K257 | 80 | workplace32.Beam86 | L24 | L216 | L344 | 121 | workplace48.Beam119 | K296 | K294 | K296 |
| 40 | workplace15.Beam44 | L441a | L441a | L192 | 81 | workplace33.Beam88 | L244 | L216a | L216 | 122 | workplace49. Beam121 | K297 | K293 | K297 |
| 41 | workplace16.Beam47 | L442 | L442 | L3 | 82 | workplace34.Beam90 | L344 | L24 | L422 | 123 | workplace50.Beam123 | K231 | K296 | K231 |

Appendix D: Beam priority rule LPT Evaluation
Table 14 Welder pair distribution LPT

| WelderPair | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | K231 | K40 | L244 | L4 | K198 |
| 2 | K297 | L147 | L344 | L4a | K199 |
| 3 | K296 | K28 | L344a | L41 | K200 |
| 4 | K293 | L257 | L390 | L41a | K201 |
| 5 | K294 | L258 | L394 | L418 | K237 |
| 6 | K9 | L14 | L420 | L418a | K238 |
| 7 | K295 | L17 | 1422 | 1419 | K239 |
| 8 | K11 | L18 | L422a | L419a | K257 |
| 9 | K308 | L36 | L424 | L476 | L192 |
| 10 | K314 | L367 | K183 | L370 | L193 |
| 11 | K267 | L416 | K184 | L370a | L3 |
| 12 | K317 | L416a | K187 | L370b | L318 |
| 13 | K7 | 1417 | K188 | L371 | L319 |
| 14 | K312 | K290 | L188 | L372 | L321 |
| 15 | K14 | K291 | L253 | 1440 | L322 |
| 16 | K232 | L16 | L254 | L440a | L330 |
| 17 | K306 | L19 | L347 | L441 | L345 |
| 18 | K311 | L216 | L35 | L441a | L80 |
| 19 | K311a | L216a | L350 | L442 | L81 |
| 20 | K310 | L217 | L361 | K192 | L334 |
| 21 | K37 | L217a | L392 | K193 | L37 |
| 22 | K38 | L220 | L393 | K194 | L37a |
| 23 | K42 | L221 | L393a | K195 | L37b |
| 24 | K62 | L222 | K196 | L382 |  |
| 25 | L155 | L24 | K197 | L384 |  |

Table 15 Process time and due date of Beams LPT

| process time |  |  |  |  | due date |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 51985 | 10397 | 4621 | 3466 | 2310 | 0 | 51985 | 62382 | 67003 | 70469 |
| 48519 | 10397 | 4621 | 3466 | 2310 | 0 | 48519 | 58916 | 63537 | 67003 |
| 47364 | 9242 | 4621 | 3466 | 2310 | 0 | 47364 | 56606 | 61227 | 64693 |
| 46209 | 9242 | 4621 | 3466 | 2310 | 0 | 46209 | 55451 | 60072 | 63537 |
| 45054 | 9242 | 4621 | 3466 | 2310 | 0 | 45054 | 54296 | 58916 | 62382 |
| 43899 | 6931 | 4621 | 3466 | 2310 | 0 | 43899 | 50830 | 55451 | 58916 |
| 42743 | 6931 | 4621 | 3466 | 2310 | 0 | 42743 | 49675 | 54296 | 57761 |
| 40433 | 6931 | 4621 | 3466 | 2310 | 0 | 40433 | 47364 | 51985 | 55451 |
| 38122 | 5776 | 4621 | 3466 | 2310 | 0 | 38122 | 43899 | 48519 | 51985 |
| 38122 | 5776 | 3466 | 3447 | 2310 | 0 | 38122 | 43899 | 47364 | 50811 |
| 35812 | 5776 | 3466 | 3447 | 2310 | 0 | 35812 | 41588 | 45054 | 48500 |
| 35812 | 5776 | 3466 | 3447 | 2310 | 0 | 35812 | 41588 | 45054 | 48500 |
| 35812 | 5776 | 3466 | 3447 | 2310 | 0 | 35812 | 41588 | 45054 | 48500 |
| 34657 | 4621 | 3466 | 3447 | 2310 | 0 | 34657 | 39278 | 42743 | 46190 |
| 33501 | 4621 | 3466 | 3447 | 2310 | 0 | 33501 | 38122 | 41588 | 45035 |
| 33501 | 4621 | 3466 | 3447 | 2310 | 0 | 33501 | 38122 | 41588 | 45035 |
| 33501 | 4621 | 3466 | 3447 | 2310 | 0 | 33501 | 38122 | 41588 | 45035 |
| 33501 | 4621 | 3466 | 3447 | 2310 | 0 | 33501 | 38122 | 41588 | 45035 |
| 33501 | 4621 | 3466 | 3447 | 2310 | 0 | 33501 | 38122 | 41588 | 45035 |
| 32346 | 4621 | 3466 | 2310 | 2291 | 0 | 32346 | 36967 | 40433 | 42743 |
| 17328 | 4621 | 3466 | 2310 | 2291 | 0 | 17328 | 21949 | 25415 | 27725 |
| 15018 | 4621 | 3466 | 2310 | 2291 | 0 | 15018 | 19639 | 23104 | 25415 |
| 15018 | 4621 | 3466 | 2310 | 2291 | 0 | 15018 | 19639 | 23104 | 25415 |
| 13863 | 4621 | 2310 | 2291 |  | 0 | 13863 | 18484 | 20794 |  |
| 11552 | 4621 | 2310 | 2291 |  | 0 | 11552 | 16173 | 18484 |  |


| Number | Destination | SPT | EDD | SST |  |  | SPT | EDD | SST |  |  | SPT | EDD | SST |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | workplace1.Be | L384 | K231 | L384 | 42 | workplace17.Beam50 | L393 | L37b | L330 | 83 | workplace35.Beam92 | L344a | L81 | L422a |
| 2 | workplace2.Beam4 | L382 | K297 | L382 | 43 | workplace18.Beam53 | L393a | L37 | L345 | 84 | workplace36.Beam94 | L344 | L258 | L422 |
| 3 | workplace3.Beam7 | L37a | K296 | L37a | 44 | workplace19.Beam56 | L392 | L217 | L80 | 85 | workplace37.Beam96 | L244 | L370a | L344a |
| 4 | workplace4.Beam10 | L37b | K293 | L37b | 45 | workplace20.Beam59 | L361 | K291 | L81 | 86 | workplace38.Beam98 | L36 | L370b | L344 |
| 5 | workplace5.Beam13 | L37 | K294 | L37 | 46 | workplace21.Beam62 | L35 | L16 | K183 | 87 | workplace39.Beam100 | L367 | L371 | L244 |
| 6 | workplace6.Beam16 | L334 | K9 | L334 | 47 | workplace22.Beam65 | L476 | L19 | L321 | 88 | workplace40.Beam102 | L416 | L321 | L416 |
| 7 | workplace7.Beam19 | K193 | K295 | L440 | 48 | workplace23.Beam68 | L41a | L216 | L424 | 89 | workplace41.Beam104 | L416a | L257 | L416a |
| 8 | workplace8. Beam22 | K192 | K11 | L440a | 49 | workplace24.Beam71 | L41 | L216a | L3 | 90 | workplace42.Beam106 | L417 | K28 | L417 |
| 9 | workplace9.Beam25 | K197 | K308 | L441 | 50 | workplace25.Beam73 | K184 | K290 | L318 | 91 | workplace43.Beam108 | L18 | L422a | L18 |
| 10 | workplace10.Beam28 | K196 | K314 | L441a | 51 | workplace1.Beam3 | K187 | L416 | L319 | 92 | workplace44.Beam110 | L17 | L370 | L17 |
| 11 | workplace11. Beam31 | K194 | K267 | L442 | 52 | workplace2.Beam6 | K188 | L416a | L193 | 93 | workplace45.Beam112 | L14 | L3 | L14 |
| 12 | workplace12.Beam34 | K195 | K317 | L372 | 53 | workplace3.Beam9 | K183 | L417 | L192 | 94 | workplace46.Beam114 | L258 | L318 | L258 |
| 13 | workplace13.Beam37 | L322 | K7 | L370a | 54 | workplace4.Beam12 | L253 | L361 | L420 | 95 | workplace47. Beam116 | L257 | L319 | L257 |
| 14 | workplace14.Beam40 | L330 | K312 | L370b | 55 | workplace5. Beam15 | L254 | L36 | K257 | 96 | workplace48.Beam118 | K28 | L147 | K28 |
| 15 | workplace15.Beam43 | L345 | K14 | L371 | 56 | workplace6. Beam18 | L347 | L367 | K239 | 97 | workplace49.Beam 120 | L147 | L476 | L147 |
| 16 | workplace16.Beam46 | L80 | K232 | L370 | 57 | workplace7. Beam21 | L350 | L253 | K238 | 98 | workplace50.Beam122 | K40 | L422 | K40 |
| 17 | workplace17.Beam49 | L81 | K306 | L393 | 58 | workplace8.Beam24 | L188 | L254 | K237 | 99 | workplace26.Beam75 | L155 | L193 | L155 |
| 18 | workplace18.Beam52 | L321 | K311 | L393a | 59 | workplace3.Beam27 | L419a | L347 | K201 | 100 | workplace27.Beam77 | K62 | L420 | K62 |
| 19 | workplace19.Beam55 | L3 | K311a | L392 | 60 | workplace10.Beam30 | L419 | L35 | K200 | 101 | workplace28.Beam79 | K38 | K40 | K38 |
| 20 | workplace20.Beam58 | L318 | K310 | K193 | 61 | workplace11.Beam33 | L418a | L350 | K199 | 102 | workplace29.Beam81 | K42 | L419a | K42 |
| 21 | workplace21. Beam61 | L319 | K37 | L361 | 62 | workplace12.Beam36 | L418 | L188 | K198 | 103 | workplace30.Beam83 | K37 | L192 | K37 |
| 22 | workplace22.Beam64 | L193 | K38 | L35 | 63 | workplace13.Beam39 | L4a | L18 | K291 | 104 | workplace31.Beam85 | K310 | L394 | K310 |
| 23 | workplace23.Beam67 | L192 | K42 | K192 | 64 | workplace14.Beam42 | L4 | K192 | K290 | 105 | workplace32.Beam87 | K14 | L419 | K14 |
| 24 | workplace24.Beam70 | K257 | K62 | L476 | 65 | workplace15.Beam45 | L394 | K184 | L253 | 106 | workplace33.Beam89 | K232 | L390 | K232 |
| 25 | workplace25.Beam72 | K239 | L155 | L394 | 66 | workplace16.Beam48 | L390 | K187 | L254 | 107 | workplace34.Beam91 | K306 | K257 | K306 |
| 26 | workplace1.Beam2 | K238 | L24 | L390 | 67 | workplace17.Beam51 | L222 | K188 | L347 | 108 | workplace35.Beam93 | K311 | L418a | K311 |
| 27 | workplace2.Beam5 | K237 | L222 | L41a | 68 | workplace18.Beam54 | L220 | L440 | L350 | 109 | workplace36.Beam95 | K311a | L344a | K311a |
| 28 | workplace3.Beam8 | K201 | L220 | L41 | 69 | workplace19.Beam57 | L221 | L440a | L188 | 110 | workplace37.Beam97 | K312 | K239 | K312 |
| 29 | workplace4.Beam11 | K200 | L221 | K197 | 70 | workplace20.Beam60 | L217a | L441 | L419a | 111 | workplace38.Beam99 | K7 | L418 | K7 |
| 30 | workplace5. Beam14 | K199 | K197 | L222 | 71 | workplace21.Beam63 | L217 | L441a | L419 | 112 | workplace39.Beam101 | K267 | L344 | K267 |
| 31 | workplace6.Beam17 | K198 | L217a | L220 | 72 | workplace22.Beam66 | L424 | L442 | L418a | 113 | workplace40.Beam103 | K317 | K238 | K317 |
| 32 | workplace7. Beam20 | L440 | K196 | L221 | 73 | workplace23.Beam69 | L420 | L17 | L418 | 114 | workplace41.Beam105 | K308 | L41a | K308 |
| 33 | workplace8. Beam23 | L440a | L384 | K196 | 74 | workplace26.Beam74 | K291 | L372 | L4a | 115 | workplace42.Beam107 | K314 | L41 | K314 |
| 34 | workplace9.Beam26 | L441 | L393 | L217a | 75 | workplace27.Beam76 | K290 | L334 | L4 | 116 | workplace43.Beam109 | K11 | K237 | K11 |
| 35 | workplace10.Beam29 | L441a | L393a | K194 | 76 | workplace28.Beam78 | L24 | L14 | L24 | 117 | workplace44.Beam111 | K295 | L244 | K295 |
| 36 | workplace11.Beam32 | L442 | L382 | K195 | 77 | workplace29.Beam80 | L16 | L424 | L16 | 118 | workplace45. Beam113 | K9 | K201 | K9 |
| 37 | workplace12.Beam35 | L372 | L392 | L217 | 78 | workplace30.Beam82 | L19 | K183 | L19 | 119 | workplace46.Beam 115 | K294 | L4a | K294 |
| 38 | workplace13.Beam38 | L370a | K194 | K184 | 79 | workplace31.Beam84 | L216 | L322 | L216 | 120 | workplace47.Beam117 | K293 | K200 | K293 |
| 39 | workplace14.Beam41 | L370b | K195 | K187 | 80 | workplace32.Beam86 | L216a | L330 | L216a | 121 | workplace48.Beam119 | K296 | L4 | K296 |
| 40 | workplace15.Beam44 | L371 | K193 | K188 | 81 | workplace33.Beam88 | L422a | L345 | L36 | 122 | workplace49.Beam121 | K297 | K199 | K297 |
| 41 | workplace16.Beam47 | L370 | L37a | L322 | 82 | workplace34.Beam90 | L422 | L80 | L367 | 123 | workplace50.Beam123 | K231 | K198 | K231 |

Table 16 Welder pair distribution Random

| WelderPair | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | K197 | L4 | K295 | L36 | K237 |
| 2 | K40 | L440a | K199 | L37 | L419a |
| 3 | L19 | K14 | K192 | L216 | L222 |
| 4 | K187 | L334 | K37 | L319 | L417 |
| 5 | L394 | K62 | L24 | L41 | L441 |
| 6 | L254 | K311 | L14 | L416a | L422 |
| 7 | L18 | L371 | L384 | L4a | L37a |
| 8 | 1419 | K238 | K310 | K196 | K9 |
| 9 | K314 | L188 | L253 | K232 | L416 |
| 10 | L390 | K184 | K290 | L17 | K306 |
| 11 | K193 | L361 | L81 | L350 | K231 |
| 12 | L16 | K296 | L155 | 1440 | L35 |
| 13 | K183 | K188 | L192 | K194 | L216a |
| 14 | K11 | K312 | L318 | L37b | K297 |
| 15 | L372 | L41a | K291 | L344 | K201 |
| 16 | L321 | L80 | L370b | L322 | K311a |
| 17 | L147 | L258 | 1420 | K317 | K257 |
| 18 | L344a | L370a | L347 | L418 | L393 |
| 19 | L345 | L3 | K267 | L217 | K38 |
| 20 | L330 | L393a | L244 | L221 | L257 |
| 21 | L367 | L370 | K42 | L442 | K294 |
| 22 | L422a | K200 | K198 | L382 | K239 |
| 23 | K7 | L392 | K293 | L220 | L424 |
| 24 | L441a | L217a | 1476 | K195 |  |
| 25 | K28 | L418a | L193 | K308 |  |

Appendix E: Beam priority rule Random Evaluation
Table 17 Example of Process time and due date of Beams random

| process time |  |  |  |  | due date |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2310 | 3466 | 42743 | 5776 | 2310 | 0 | 2310 | 5776 | 48519 | 54296 |
| 10397 | 3447 | 2310 | 2291 | 3466 | 0 | 10397 | 13844 | 16154 | 18446 |
| 4621 | 33501 | 2310 | 4621 | 4621 | 0 | 4621 | 38122 | 40433 | 45054 |
| 3466 | 2291 | 17328 | 2310 | 5776 | 0 | 3466 | 5757 | 23085 | 25396 |
| 4621 | 13863 | 4621 | 3466 | 3447 | 0 | 4621 | 18484 | 23104 | 26570 |
| 3466 | 33501 | 6931 | 5776 | 4621 | 0 | 3466 | 36967 | 43899 | 49675 |
| 6931 | 3447 | 2291 | 3466 | 2291 | 0 | 6931 | 10378 | 12669 | 16135 |
| 3466 | 2310 | 32346 | 2310 | 43899 | 0 | 3466 | 5776 | 38122 | 40433 |
| 38122 | 3466 | 3466 | 33501 | 5776 | 0 | 38122 | 41588 | 45054 | 78555 |
| 4621 | 3466 | 4621 | 6931 | 33501 | 0 | 4621 | 8087 | 12707 | 19639 |
| 2310 | 3466 | 2310 | 3466 | 51985 | 0 | 2310 | 5776 | 8087 | 11552 |
| 4621 | 47364 | 11552 | 3447 | 3466 | 0 | 4621 | 51985 | 63537 | 66984 |
| 3466 | 3466 | 2310 | 2310 | 4621 | 0 | 3466 | 6931 | 9242 | 11552 |
| 40433 | 34657 | 2310 | 2291 | 48519 | 0 | 40433 | 75090 | 77400 | 79691 |
| 3447 | 3466 | 4621 | 4621 | 2310 | 0 | 3447 | 6912 | 11533 | 16154 |
| 2310 | 2310 | 3447 | 2310 | 33501 | 0 | 2310 | 4621 | 8068 | 10378 |
| 10397 | 9242 | 4621 | 35812 | 2310 | 0 | 10397 | 19639 | 24260 | 60072 |
| 4621 | 3447 | 3466 | 3466 | 3466 | 0 | 4621 | 8068 | 11533 | 14999 |
| 2310 | 2310 | 35812 | 4621 | 15018 | 0 | 2310 | 4621 | 40433 | 45054 |
| 2310 | 3466 | 4621 | 4621 | 9242 | 0 | 2310 | 5776 | 10397 | 15018 |
| 5776 | 3447 | 15018 | 3447 | 45054 | 0 | 5776 | 9223 | 24241 | 27687 |
| 4621 | 2310 | 2310 | 2291 | 2310 | 0 | 4621 | 6931 | 9242 | 11533 |
| 35812 | 3466 | 46209 | 4621 | 4621 | 0 | 35812 | 39278 | 85487 | 90107 |
| 3447 | 4621 | 3466 | 2310 |  | 0 | 3447 | 8068 | 11533 |  |
| 9242 | 3466 | 2310 | 38122 |  | 0 | 9242 | 12707 | 15018 |  |

Table 18 Example of bin dispatched order (Random)

| Number | Destination | SPT | EDD | SST |  |  | SPT | EDD | SST |  |  | SPT | EDD | SST |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | workplace1.Beam1 | L334 | K308 | L384 | 42 | workplace17.Beam50 | L393a | L222 | K196 | 83 | workplace35.Beam92 | L24 | L192 | L422a |
| 2 | workplace2.Beam4 | L384 | L347 | L382 | 43 | workplace18.Beam53 | L188 | K193 | K194 | 84 | workplace36.Beam94 | L221 | K294 | L344 |
| 3 | workplace3.Beam7 | L382 | L16 | L37a | 44 | workplace19.Beam56 | K184 | L155 | L193 | 85 | workplace37.Beam96 | L344a | L80 | L216a |
| 4 | workplace4.Beam10 | L37b | L18 | L37b | 45 | workplace20.Beam59 | L253 | L334 | K201 | 86 | workplace38.Beam98 | L416 | L217a | L36 |
| 5 | workplace5. Beam13 | L37 | L393a | L37 | 46 | workplace21. Beam62 | L419a | L4a | L318 | 87 | workplace39. Beam 100 | L416a | K200 | L367 |
| 6 | workplace6.Beam16 | L37a | L422 | L334 | 47 | workplace22.Beam65 | L419 | K257 | L319 | 88 | workplace40. Beam 102 | L417 | K297 | L417 |
| 7 | workplace7. Beam19 | K193 | L370b | L370a | 48 | workplace23.Beam68 | L392 | K314 | L81 | 89 | workplace41. Beam104 | L36 | K197 | L416 |
| 8 | workplace8.Beam22 | L318 | L344a | L442 | 49 | workplace24.Beam71 | 41a | K28 | L330 | 90 | workplace42. Beam 106 | . 367 | L440 | L416a |
| 9 | workplace9.Beam25 | L192 | K11 | L440a | 50 | workplace25.Beam73 | L418a | L318 | L322 | 91 | workplace43.Beam 108 | 14 | L345 | 17 |
| 10 | workplace10.Beam28 | K239 | L371 | L371 | 51 | workplace1.Beam3 | K188 | L37a | K199 | 92 | workplace44.Beam110 | L17 | L147 | L14 |
| 11 | workplace11.Beam31 | L81 | L319 | L440 | 52 | workplace2.Beam6 | L418 | L416a | K184 | 93 | workplace45.Beam112 | L18 | K239 | L18 |
| 12 | workplace12.Beam34 | K198 | K192 | L370b | 53 | workplace3.Beam9 | L4a | L419 | K187 | 94 | workplace46.Beam114 | L258 | K184 | K28 |
| 13 | workplace13.Beam37 | K196 | L384 | L441a | 54 | workplace4. Beam 12 | L476 | L424 | K183 | 95 | workplace47.Beam116 | 257 | L361 | L258 |
| 14 | workplace14.Beam40 | K197 | L36 | L370 | 55 | workplace5. Beam15 | L393 | L442 | K188 | 96 | workplace48.Beam118 | K28 | L17 | L257 |
| 15 | workplace15.Beam43 | K195 | L244 | L372 | 56 | workplace6. Beam18 | L35 | K183 | L217 | 97 | workplace49.Beam120 | K40 | K291 | L147 |
| 16 | workplace16.Beam46 | K238 | L330 | L441 | 57 | workplace7. Beam21 | L347 | L420 | L420 | 98 | workplace50.Beam122 | L147 | L393 | K40 |
| 17 | workplace17.Beam49 | K200 | K196 | K192 | 58 | workplace8.Beam24 | K187 | L350 | L424 | 99 | workplace26.Beam75 | -155 | K37 | L155 |
| 18 | workplace18.Beam52 | L345 | K310 | K193 | 59 | workplace9.Beam27 | L350 | K295 | L221 | 100 | workplace27.Beam77 | K62 | K232 | K62 |
| 19 | workplace19.Beam55 | K201 | L188 | L41 | 60 | workplace10.Beam30 | L4 | L216a | L222 | 101 | workplace28.Beam79 | K42 | L257 | K42 |
| 20 | workplace20.Beam58 | L321 | L476 | L393 | 61 | workplace11.Beam33 | K183 | K199 | L220 | 102 | workplace29.Beam8 | K38 | L221 | K38 |
| 21 | workplace21.Beam61 | K237 | L370a | L361 | 62 | workplace12.Beam36 | L361 | L392 | L217a | 103 | workplace30.Beam83 | K37 | K14 | K37 |
| 22 | workplace22. Beam64 | L80 | L14 | L41a | 63 | workplace13.Beam39 | L41 | K7 | L254 | 104 | workplace31.Beam85 | K310 | K293 | K310 |
| 23 | workplace23. Beam67 | L330 | K198 | L393a | 64 | workplace14.Beam42 | L254 | K306 | L350 | 105 | workplace32. Beam87 | <232 | K62 | K14 |
| 24 | workplace24.Beam70 | L319 | L367 | L392 | 65 | workplace15.Beam45 | L217a | L422a | L253 | 106 | workplace33.Beam89 | K306 | L418a | K306 |
| 25 | workplace25.Beam72 | K192 | K195 | L476 | 66 | workplace16.Beam48 | L217 | L37b | L418a | 107 | workplace34.Beam9 | K14 | K238 | K311a |
| 26 | workplace1.Beam2 | K257 | K194 | L35 | 67 | workplace17.Beam51 | L420 | K311 | L4 | 108 | workplace35.Beam93 | K311a | L394 | K232 |
| 27 | workplace2. Beam5 | K194 | L344 | L394 | 68 | workplace18.Beam54 | L394 | K42 | L419 | 109 | workplace36.Beam95 | K311 | L24 | K311 |
| 28 | workplace3.Beam8 | L193 | L440a | L390 | 69 | workplace19.Beam57 | L244 | L35 | L4a | 110 | workplace37.Beam97 | K312 | L41 | K312 |
| 29 | workplace4.Beam11 | L3 | K231 | K238 | 70 | workplace20.Beam60 | K291 | L253 | L419a | 111 | workplace38.Beam99 | K267 | L416 | K7 |
| 30 | workplace5.Beam14 | K199 | K296 | L345 | 71 | workplace21.Beam63 | L216 | K311a | L418 | 112 | workplace39.Beam101 | K317 | L418 | K267 |
| 31 | workplace6.Beam17 | L322 | L417 | K257 | 72 | workplace22.Beam66 | L344 | L41a | L347 | 113 | workplace40. Beam 103 | K7 | L322 | K317 |
| 32 | workplace7. Beam20 | L441a | K312 | K200 | 73 | workplace23.Beam69 | K290 | L419a | L188 | 114 | workplace41.Beam 105 | <314 | L390 | K314 |
| 33 | workplace8.Beam23 | L441 | L37 | L80 | 74 | workplace26.Beam74 | L222 | L441a | K291 | 115 | workplace42. Beam 107 | <308 | L217 | K308 |
| 34 | workplace ${ }^{\text {S }}$. Beam26 | L370 | L441 | L3 | 75 | workplace27.Beam76 | L19 | L370 | K290 | 116 | workplace43.Beam 109 | K11 | L258 | K11 |
| 35 | workplace10.Beam29 | L442 | L254 | K239 | 76 | workplace28.Beam78 | L390 | K187 | L19 | 117 | workplace44.Beam111 | K295 | L193 | K295 |
| 36 | workplace11.Beam32 | L370a | K290 | K198 | 77 | workplace29.Beam80 | L422 | L216 | L216 | 118 | workplace45.Beam113 | K9 | L382 | K9 |
| 37 | workplace12.Beam35 | L440a | L372 | L321 | 78 | workplace30.Beam82 | L422a | K188 | L244 | 119 | workplace46.Beam115 | K294 | K40 | K294 |
| 38 | workplace13.Beam38 | L372 | K38 | K237 | 79 | workplace31.Beam84 | L220 | L4 | L24 | 120 | workplace47.Beam117 | K293 | L3 | K293 |
| 39 | workplace14.Beam41 | L371 | K9 | K197 | 80 | workplace32.Beam86 | L216a | L19 | L422 | 121 | workplace48.Beam119 | K296 | K237 | K296 |
| 40 | workplace15.Beam44 | L440 | L81 | L192 | 81 | workplace33.Beam88 | L424 | K267 | L344a | 122 | workplace49.Beam121 | K297 | K201 | K297 |
| 41 | workplace16.Beam47 | L370b | L321 | K195 | 82 | workplace34.Beam90 | L16 | K317 | L16 | 123 | workplace50. Beam123 | K231 | L220 | K231 |

Table 19 Random Beam priority rule 5 experiment results

| Beam Heurestic: | Random |  | Beam Heurestic: | Random |  | Beam Heurestic: | Random |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Plate Heuristios: | SPT |  | Plate Heuristios: | EDD |  | Plate Heuristics: |  |
| 1 AugWaitingTime: | 8:42.233315187465 |  | AugW/aitingTime: | 4:36.648228310786 |  | AugWaitingTime: | 9:10.195410787876 |
| 1 TotalProcessTime: | 15:52:26.6884027931 |  | TotalProcessTime: | 12:39:56.1372515075 |  | TotalProcessTim | 15:59:19.2301318852 |
| Welder Working\% | 58,5 |  | Welder Working\% | 63,0 |  | Welder Working* | 58,2 |
| Welder W/alking\% | 0,6 |  | Welder Walking\% | 0,6 |  | Welder Walking\% | 0,6 |
| Welder Waiting\% | 40,9 |  | Welder W/aiting\% | 36,4 |  | Welder Waiting\% | 41,2 |
| 2 AugWaitingTime: | 9:11.320286071473 | 2 | AugWaitingTime: | 1:14.0823550596172 |  | AugWaitingTime: | 9:14.250564428214 |
| 2 TotalProcessTime: | 15:50:45.4491809163 | 2 | TotalProcessTime: | 12:43:15.4518972765 | 2 | TotalProcessTim | 15:11:03.4491728094 |
| Welder Working\% | 58,5 |  | Welder Working\% | 63,0 |  | Welder Working* | 58,2 |
| Welder Walking\% | 0.6 |  | Welder Walking\% | 0,6 |  | Welder Walking\% | 0,6 |
| Welder Waiting\% | 40,9 |  | Welder Waiting\% | 36,4 |  | Welder Waiting\% | 41,2 |
| 3 AugWaitingTime: | 8:08.855186979143 | 3 | AugWaitingTime: | 4:55.338275964164 |  | AugWaitingTime: | 9:10.195410787876 |
| 3 TotalProcessTime: | 15:54:13.9146675455 | 3 | TotalProcessTime: | 12:58:47.060939578! | 3 | TotalProcessTim | 15:59:19.2301318852 |
| Welder Working\% | 58,4 |  | Welder Working\% | 62,9 |  | Welder Working* | 58,2 |
| Welder Walking\% | 0,6 |  | Welder Walking\% | 0,6 |  | Welder Walking\% | 0,6 |
| Welder Waiting\% | 41.0 |  | Welder Waiting\% | 36,5 |  | Welder Waiting\% | 41,2 |
| 4 AugWaitingTime: | 8:09.181074232294 | 4 | AugW/aitingTime: | 4:48.892135270756 |  | AugW/aitingTime: | 9:10.195410787876 |
| 4 TotalProcessTime: | 15:54:09.3565959565 | 4 | TotalProcessTime: | 14:10:52.6210066404 |  | TotalProcessTim | 15:59:19.2301318852 |
| Welder Working\% | 58,4 |  | Welder Working\% | 61.7 |  | Welder Working* | 58,2 |
| Welder Walking\% | 0,6 |  | Welder Walking\% | 0,6 |  | Welder Walking\% | 0,6 |
| Welder Waiting\% | 41,0 |  | Welder W/aiting\% | 37.7 |  | Welder Waiting\% | 41,2 |
| 5 AugW/aitingTime: | 8:05.174731827744 | 5 | AugW/aitingTime: | 3:04.351559497462 |  | AugW/aitingTime: | 9:10.195410787876 |
| 5 TotalProcessTime: | 15:55:11.903559396 | 5 | TotalProcessTime: | 12:45:14.5574165792 | 5 | TotalProcessTim | 15:59:19.2301318852 |
| Welder Working\% | 58,4 |  | Welder Working\% | 63,0 |  | Welder Working* | 58,2 |
| Welder Walking\% | 0.6 |  | Welder Walking\% | 0,6 |  | Welder Walking\% | 0,6 |
| Welder Waiting\% | 41,0 |  | Welder W'aiting\% | 36,4 |  | Welder Waiting\% | 41,2 |

