Fast temperature changes for polymerase chain reaction (PCR) on a lab-on-a-chip (LoaC)

L.M.J. Nijsten

FACULTY OF SCIENCE AND TECHNOLOGY
Mesoscale Chemical Systems

Examination Committee:

Prof. dr. ir. H.J.M. ter Brake Energy, Materials & Systems
Prof. dr. J.G.E. Gardeniers Mesoscale Chemical Systems
Dr. ir. R.M. Tiggelaar Mesoscale Chemical Systems
B. B. Bruijns MSc Mesoscale Chemical Systems

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Summary
To obtain a DNA profile from a sample found on a crime scene, there are several steps that need to be executed. First the DNA has to be extracted from the sample, then the DNA has to be duplicated several times to get enough material to analyse, and finally the DNA profile has to be made. This research focuses on the DNA multiplication step.

The goal of this research is to find a chip design optimised for thermal cycling to perform the PCR reaction as fast and efficient as possible. This research is divided into two parts.

First, a literature study is done in search for an optimised chip design. Secondly, experimental research is performed to investigate the influence of adding a cooling element to the chip on the thermal cycle. Analytical and numerical calculations were made and an experimental setup was used to verify model results.

From the literature research a chip design is proposed for the fastest amplification time: a continuous droplet flow chip with an optimised length of the extension zone (i.e. adjusted to the velocity of the fluid, the cycle number, the speed of the polymerase and the length of the amplicon).

The materials of which this chip is composed should have low thermal conductivity, to make well separated temperature zones possible. As heating method thin element heaters in/near the fluid channel should be used, to localise the heat close to the fluid (for efficient heating with minimised losses).

Simulations showed that adding a cooling element between the denaturation and elongation zones improves the thermal cycling. For all simulated velocities in a channel with a cross section of 200 x 200 µm, the cooling element ensures a 20% decrease of the combined heating and cooling time (per cycle). Both smaller channels and the use of narrower denaturation heaters might be possibilities of further reducing the cycling time.

From simulations in combination with experiments (with PDMS/glass chips with external heating/cooling) it is concluded that the cooling element indeed reduces the temperature transition time between the denaturation and extension zone, thus making faster temperature transitions possible.
1 Introduction

The deoxyribonucleic acid (DNA) of every human is unique, except for identical twins [1]. Therefore it can be very useful to use in forensic investigations to identify suspects or victims. The first time DNA evidence used to identify an offender was in the late eighties of last century [2].

Since then, there obviously have been a lot of developments in the use of DNA as forensic evidence. But what lies ahead? A futuristic image would be a handheld device that, within minutes, could obtain a DNA profile from a sample and compare this with a database of DNA profiles to find suspects of the crime. Such a device combines several apparatus, used in a laboratory on one chip; a lab-on-a-chip.

A first step in the direction of such a system, which compares DNA profiles with a database, would be a handheld device that could indicate if there is human DNA present in a sample: a presumptive test. If human DNA is indeed found, the sample can be investigated further in the forensic laboratory, thereby reducing the number of samples to be investigated in detail, which saves costly time.

To obtain a DNA profile from a sample found on a crime scene, there are several steps that need to be executed. First the DNA has to be extracted from the sample, then the DNA has to be duplicated several times to get enough material to analyse, and finally the DNA profile has to be made.

This research focuses on the DNA multiplication step. To increase the amount of DNA from the sample, needed to obtain a DNA profile, the polymerase chain reaction (PCR) is used to duplicate specific parts of the DNA. The PCR reaction will be discussed in more detail in section 2.1. For now it is sufficient to know that for this reaction to take place, the sample needs to go through a temperature cycle several times.

The speed of the PCR reaction depends on several factors. One of them is the speed of an enzyme used to copy the DNA. Another factor is the speed and accuracy at which the different temperatures are reached. Not only the speed of the reaction increases with faster temperature rates, but also the specificity (the correct part of the DNA multiplied) and the efficiency (the yield of the PCR cycle) of the reaction is favoured by fast and accurate temperature changes [3-5].

Therefore, the goal of this research is to find a chip design optimised for thermal cycling to perform the PCR reaction as fast and efficient as possible. This research is divided into two parts.

First, a literature study is done in search for an optimised chip design. In this section the PCR reaction is treated in more detail including the theoretical limit of the PCR. Next an overview is given of chip design types, materials and cooling and heating methods mentioned in literature, leading to the design conclusion for the fastest chip.

Secondly, experimental research has been done to investigate the influence of adding a cooling element to the chip on the thermal cycle. Before actually fabricating the chip and doing practical experiments in the lab, analytical and numerical calculations are made. The analytical calculations are used to estimate the dimensions needed in the simulations. The numerical modelling will be compared to these calculations and will give an impression what the influence of the cooling element will be. Practical experiments will confirm whether a cooling element might decrease the time needed from sample to DNA detection.
2 Literature research

2.1 Polymerase Chain Reaction

2.1.1 General

The Polymerase Chain Reaction (PCR) is a reaction with which parts of DNA are duplicated by an enzyme called polymerase. The reaction can be divided in three main steps, denaturation, annealing and extension/elongation. These three steps have different optimal reaction temperatures. The temperature ranges commonly used for denaturation, annealing and extension are 90-95 °C, 50-70 °C and 70-75 °C, respectively [6-8] (see Figure 1).

![Figure 1 PCR reaction steps. Edited from [5]](image)

DNA consists of two bonded polymer strands: double stranded DNA (dsDNA). During the denaturation step the dsDNA template splits into single stranded DNA (ssDNA). After the temperature is lowered to the annealing temperature the ssDNA reacts with primers.

The primers are nucleotide sequences which form the starting point of a particular fragment of the DNA that will be amplified; the amplicon. By modifying the nucleotide sequence of the primer, the amplicon can be chosen to be human specific [9, 10]. It is critical not to undershoot the annealing temperature to prevent false annealing of the primers. This would decrease the specificity of the PCR [7, 11].

When the primers are attached, an enzyme called polymerase reacts with the DNA-primer complex and starts the extension of the primers by adding nucleotides to the ssDNA. By increasing the temperature, the annealing is diminished and the extension is favoured.

Finally the temperature is raised to the denaturation temperature again to denaturise all double stranded DNA followed by the next cycle of annealing and extension.

After every successful cycle the amount of target DNA sequence is doubled [12]. With this exponential increase, typically 20-40 cycles are needed to get a detectable amount of DNA resulting in a detection time varying from couple of hours for commercial PCR machines [7] to several minutes for lab-on-a-chip devices [13, 14].
Typical detection methods include fluorescence-based DNA detection and capillary electrophoresis [15]. With fluorescence-based detection the amount of DNA can be monitored in real time. Intercalator dyes, such as SYBR Green, bind to the DNA and the fluorescence signals from the interaction between the dye and the increasing amount DNA can be optically detected [15].

2.1.2 PCR methods
There are several ways of performing the PCR reaction. The conventional way is the three steps PCR. The three main steps are performed at their optimal temperatures. Alternatively, the three steps can be combined into an isothermal reaction or divided into two temperature regimes. Limiting the temperature regimes reduces the complexity of chips for PCR, since less thermal cycling is needed. However, performing steps at non-optimal temperatures can result in lower product yield, speed or specificity.

Isothermal PCR has been investigated in the MCS group [10], but although it would dramatically decrease the complexity of the chip, it is not specific enough for forensic purposes and/or need very complex enzymes [16]. Besides the complex enzymes, the amplification times of different isothermal techniques are in the range of 20 minutes [17] to more than an hour [13]; not even close to the fast amplification times that will be mentioned in 2.1.3.3.

The two step PCR reaction combines the annealing and extension step. The temperature at which the combination of these steps is performed is critical for the results because a lower temperature is favourable for annealing, while higher temperature benefits the extension. It has been shown that the product yield does not differ much from the three step reaction when the extension temperature is below 70 °C [7]. By using the two step PCR reaction, the efficiency of the available primers and the specificity of the reaction can even increase (compared to the three step reaction), because false priming occurs less when the annealing is done at higher temperatures [7, 11].

Overall, the two step reaction is proven to be time saving per cycle and it uses less reagents compared to the conventional three step reaction [18].

2.1.3 PCR speed
There are two definitions that one should pay attention to. First the cycle time: the time needed to complete one cycle. The second is the amplification or detection time: the time needed until a detectable amount of DNA is formed. A short cycle time could lead to a longer amplification time when the efficiency of the cycle is lower than a somewhat longer cycle time (and thus, more cycles are needed). So, besides the cycle time, the efficiency of the cycle should also be taken into account.

2.1.3.1 Cycle time limit
The different steps of the PCR cycle have different time limits. The denaturation and annealing occur much faster than the time needed for elongation [4, 19]. The time for denaturation and annealing has been claimed to occur instantaneously when the correct temperatures is reached [20], while the elongation depends on the length of the required product [2], polymerase speed and the diffusion time of primers and polymerase [14].

By using small volumes, for example nano litre droplets, the diffusion times are negligible compared to the time needed for the polymerase to extend the amplicon [4, 14, 21]. The most commonly used human specific polymerase is the Thermus Aquaticus (Tag) polymerase. The extension rate of Taq is
temperature dependent. At 55 °C the extension rate is 24 nucleotides per second and at optimum temperature of 72 °C it is around 60-100 nucleotides per second [22]. A faster polymerase found in literature is the Thermococcus Kodakaraensis (KOD) polymerase with an extension rate of 100-130 nucleotides per second at an optimum temperature of 75 °C [23, 24]. Theoretically for a 200 base pair (bp) amplicon (a typical length needed to identify human DNA [25]) this would result in a minimum elongation time of two seconds.

2.1.3.2 Cycle times in practice

Although the denaturation and annealing times are stated previously as negligible, there are experiments done were the denaturation needs to take at least 2 seconds and the annealing time has a minimum of about 5 seconds, to maintain significant yield [3, 26].

Also reports have been made on varying the elongation time with the cycle number to increase the yield [3, 27]. This is explained by the fact that in the beginning the amount of primer and polymerase is excessive compared to the amplicons, while after a couple of cycles this ratio is lowered and the elongation time has to be extended [12, 27]. Another reason can be the inhibition effect of the materials surrounding the reaction mixture. It has been shown [28] that surface adsorption of Taq polymerase (rather than DNA) is responsible for the inhibition.

There have been attempts to approach the theoretical limit of the PCR. Cycle times as short as 5.2 seconds for a 500 bp amplicon using Taq polymerase have been reported with a continuous flow device [7]. Assuming the speed of Taq polymerase to be 100 nucleotides per second, this is very close to the theoretical limit.

2.1.3.3 Shortest amplification time

The fastest PCR chip has a cycle time of 4.5 seconds [8], resulting in an amplification time of just 90 seconds. This was achieved for an amplicon of 176 bp, so it did not approach the Taq polymerase limit of 1.8 seconds per cycle.

The PCR reaction approaching the theoretical limit of the polymerase, as mentioned above, was just a little slower with an amplification time of 1.7 minutes for 20 cycles [7].

Compared to commercial thermal cyclers (with detection times in the order of hours as mentioned in 2.1.1) the efficiency of is latter PCR chip was significantly lower: with a fluid velocity of 1 mm s⁻¹ the efficiency was only 25% [7]. This efficiency decreased even further with increasing velocity. Reasons for this low efficiency could be inhibition of the Taq polymerase because of the high surface-to-volume ratio and/or the non-optimised duration in the different temperature zones [7].
2.2 PCR in microfluidic systems

In search for the fastest PCR reaction on chip the main requirement for the design is fast and precise temperature cycling. The chip types, materials and heating and cooling methods can all be selected based on this requirement.

Secondary requirements that can be taken into account for a handheld DNA-profile producing device, are compatibility with pre- and post-processes, small footprint (size of device) and low power consumption. At the end of each section a table is given which summarises the section with values ranging from ‘- -’, via ‘-’, ‘+/−’, ‘+’ to ‘++’. These values are rather subjectively chosen, however, it is just intended to give a clear overview of the possibilities.

2.2.1 Chip designs

There are several chip designs reported for DNA multiplication. Roughly the designs can be divided into ‘chamber based’ and ‘continuous flow’.

2.2.1.1 Chamber based

In a chamber or well based design, the PCR solution stays in a reaction chamber (no flow/ static) while the temperature is cycled [29] (Figure 2). This design allows small reaction volumes to be cycled rapidly through the different temperature because of the small thermal mass of the mixture. Besides small reaction volumes, fast temperature changes can be accomplished with materials of high thermal conductivity and low thermal capacity: they can be heated and cooled fast.

In combination with thin film heaters (see section 2.2.4.1) a heating rate of 175 °C s\(^{-1}\) and a cooling rate of 125 °C s\(^{-1}\) of a 100 nL sample was realised [3]. This resulted in a cycle time for an amplicon of 82 base pairs of 8.5 seconds [3].

Disadvantages of this design include the absence of high throughput possibilities and risk of cross contamination between experiments [30, 31].

![Figure 2 Simplified chamber based chip](image)

2.2.1.2 Continuous flow

The fastest cycle and amplification times are, as mentioned in section 2.1.3, 2.1.3.2, achieved with continuous flow designs.

The sample in a continuous flow PCR device is moved through fixed temperature zones (indicated with different colours in Figure 3). Not the complete reaction chamber has to be heated and cooled repeatedly, but only the reaction mixture has to change temperature. Compared to a chamber based chip this provides simplified temperature control, low energy consumption and it greatly decreases thermal transition times which on its turn reduces the cycling time [7, 14, 26, 27, 31, 32].

To ensure that the different temperature zones are well insulated, materials with low thermal conductivity [7] or air gaps [33] can be used [30]. In case of materials with low thermal conductivity, it is easier to establish different fixed temperature zones in parallel in comparison with high thermal conductivity materials. For example, the use of silicon with different temperature zones leads to a
high power consumption device with hard to separate temperature zones, leading to low PCR yield [34]. This latter is due to the fact that heat from the heated denaturation zone easily flows to the cooling zone, resulting in a cooler denaturation zone and a hotter cooling zone.

The continuous flow design can be subdivided into designs with fixed and adjustable cycle numbers. With a fixed-loop (Figure 3A) design the number of cycles is determined the design of the chip [15, 32], while with closed-loop (Figure 3B) and oscillatory devices (Figure 3C) the cycle number is adjustable [35, 36].

Adjustable cycle numbers are convenient when the amount of DNA per sample differs. Extra cycles can be added for lower concentrations of DNA in a sample. The complexity of (fabrication and control of) the device however will increase compared to a fixed-loop design.

2.2.1.3 Virtual reaction chamber
For both chamber based and continuous flow devices a way to increase the rate of change of temperature is by reducing the thermal mass of the sample.

A decreased sample volume will increase the surface-to-volume ratio. Thus, more sample is in contact with the surrounding material, which is preferable for faster temperature changes. However, a higher surface to volume ratio also increases the inhibition effect (as mentioned in section 2.1.3.2) by the surrounding materials on the PCR [15, 28, 37, 38]. To prevent contact between the sample and the surrounding material, oil can be used to form virtual reaction chambers; nano litre droplets of sample in oil.

The use of droplets of sample in oil adds an advantage for fast temperature changes. Oil has a lower thermal mass than water and thus can respond more rapidly to the surrounding temperature and thus will reach the operating temperatures more quickly [26].

Besides the prevention of inhibition and increasing temperature rates, droplet-based systems also avoid cross contamination and diffusional dilution while running many PCR assays simultaneously [26, 37, 39].
Finally, droplets in a continuous flow chip enable fast mixing because the droplets experience a dipolar, circulating flow, as can be seen in Figure 4. Fast mixing of the PCR sample (DNA, polymerase and primers) enables more efficient PCR.

![Figure 4 Mixing due to a dipolar, circulating flow experienced by droplets in a micro channel [40]](image)

### 2.2.1.4 Summarising table

Table 1 Overview of chip designs

<table>
<thead>
<tr>
<th>Chip designs</th>
<th>Temperature cycling</th>
<th>Pre/post compatibility</th>
<th>Device footprint</th>
<th>Ease of fabrication</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chamber (no flow)</td>
<td>++</td>
<td>-</td>
<td>+</td>
<td>-</td>
</tr>
<tr>
<td>Continuous flow fixed loop</td>
<td>+</td>
<td>+</td>
<td>+</td>
<td>+</td>
</tr>
<tr>
<td>Continuous flow closed loop</td>
<td>+</td>
<td>-</td>
<td>+/-</td>
<td>-</td>
</tr>
<tr>
<td>Droplet flow</td>
<td>++</td>
<td>+/-</td>
<td>+/-</td>
<td>+/-</td>
</tr>
</tbody>
</table>

### 2.2.2 Materials

In literature there are several materials mentioned to be used for a microfluidic lab-on-a-chip device. Roughly the materials can be divided in conventional materials and polymers. Depending on the chip design the best suitable material or combination of materials can be chosen.

#### 2.2.2.1 Conventional materials

The conventional materials are glass and silicon. Most of the PCR micro chambers/channels mentioned in literature are made of silicon [30]. There are several reasons for using silicon. First, the techniques to fabricate complex chip structures are well known [41]. Secondly silicon has a high (temperature dependent) thermal conductivity [42] which is favourable for fast temperature ramping in a chamber based chip. Thirdly the mechanical strength ensures robust designs [3].

Disadvantages include the silicon surface properties: it has to be covered with a coating to make PCR possible, since Si and SiO₂ inhibit the PCR [30, 43]. There is also a downside to the high thermal conductivity: silicon requires thermal insulation to prevent heat loss (and thus high energy
consumption) resulting in more complex designs [15]. Furthermore silicon cannot be easily used in combination with optical detection techniques (like the fluorescence-based DNA detection mentioned in section 2.1.1) because of its opacity [15].

The use of glass circumvents this opacity problem because of its superior optical transparency [30]. Other properties are the well-defined surface chemistries (which allows coating methods to prevent inhibition) [30] and the lower thermal conductivity of glass in comparison to silicon. The latter ensures that no additional insulation is required on chip [30], but does not perform as well as silicon in a chamber based design.

### 2.2.2.2 Polymers

A promising alternative for the conventional materials are polymers. There is a wide range of polymers used for PCR chips, including polydimethylsiloxane (PDMS), polymethyldiacrylate (PMMA) and polycarbonate (PC) [15, 28]. Overall these materials are cheaper than glass and silicon, and have lower thermal conductivities, which is favourable in combination with steady state temperature zones.

PDMS is one of the most commonly used polymers because of its optical transparency, flexibility, ease of fabrication and biocompatibility [15, 38, 44, 45]. Disadvantages include possible loss of sample because of the high permeability [15, 38, 46].

Another example of an inexpensive and versatile polymer is PMMA. PCR chips of this material can be fabricated in minutes using a CO$_2$ laser for ablation (removal of material from the surface) [47]. It can be used in combination with optical detection techniques [15] because of relatively low amounts of auto fluorescence [48]. Combined with low adsorption interaction of single-stranded DNA with PMMA [48] it seems a good material to use. The relatively low glass transition temperature ($T_g$), however, might cause problems when used as material for a PCR chip, although no deformation was observed in earlier research for short (<40 min) application [49].

A polymer that does not have the disadvantage of low glass transition temperature is polycarbonate. This material can withstand the high temperatures of a PCR cycle [15]. Besides high $T_g$, the low thermal capacitance makes polycarbonate chips less sensitive to thermal disturbances when used in steady state [50].

A disadvantage of the use of polycarbonate can be the significant amount of auto fluorescence that it generates. When fluorescence readout techniques are used, this could lower the detection limit [51]. This effect can be enhanced by the large levels of nonspecific adsorption to the PC [52].

The properties of polyimide [53] make this material also suitable for use in a DNA multiplication chip. It has a high $T_g$ (350°C) and optical transmission in range in which IR mediated thermo cycling (see section 2.2.4.2) can be done [53].

### 2.2.2.3 Other materials

Besides silicon, glass and the polymers mentioned above, there are several other materials used for PCR devices. Among them are ceramics, aluminium, 317 stainless steel, LiNbO3 and some special polymers like perfluoroalkoxy-modified polytetrafluoroethylene (PFA) and cyclic olefin copolymer (COC). Because their properties are not as favourable compared to the materials mentioned in
section 2.2.2.1 and 2.2.2.2, they are not widely used [30] and will not be taken into account in this work.

2.2.2.4 Coating
Almost every material that is used for PCR devices has to be coated to prevent inhibition of the reaction and improve the signal-to-noise ratio [38]. The inhibition effect can be weakened by treating the surface with dichlorodimethylsilane (DCDMS) or bovine serum albumin (BSA), thereby improving the PCR efficiency [28, 38].

The improved results come to a cost of extra fabrication of modification steps. The BSA treatment is faster and easier to perform compared to treatment with DCDMS, but the results show large variation and the BSA may interact problematic with a fluorescent dye, used for temperature sensing [15].

2.2.2.5 Summarising table

Table 2 Overview of materials used for PCR chips

<table>
<thead>
<tr>
<th>Materials</th>
<th>Thermal conductivity</th>
<th>Optical Transparancy</th>
<th>PCR compatibility (inhibition)</th>
<th>Ease of fabrication</th>
<th>Costs</th>
</tr>
</thead>
<tbody>
<tr>
<td>Glass</td>
<td>-</td>
<td>++</td>
<td>-</td>
<td>-</td>
<td>+/-</td>
</tr>
<tr>
<td>Silicon</td>
<td>++</td>
<td>--</td>
<td>-</td>
<td>+/-</td>
<td>--</td>
</tr>
<tr>
<td>PDMS</td>
<td>--</td>
<td>+</td>
<td>+/-</td>
<td>++</td>
<td>+</td>
</tr>
</tbody>
</table>

2.2.3 Cooling
Between the denaturation and annealing step, the temperature of the PCR mixture has to drop 30-40 °C, depending on which PCR technique is used. This temperature decrease can be accomplished either actively or passively.

2.2.3.1 Passive cooling
Passive cooling can be done by using a chip design with a high surface to volume ratio. In this way heat is dissipated by convection to the surroundings, which is quite effective [3, 7, 41]. To improve this dissipation, polycarbonate can be used to form a fin [50] or a copper block can be attached to dissipate heat from the micro-channel to the surroundings. When the chip uses small reaction volumes, this cooling method is sufficient to achieve fast cycling [3].
2.2.3.2 Active cooling

To increase the cooling rates, active cooling can be used. Active cooling is not widely used though. Most active cooling systems increase the size of the chip, the device consumes more power, and it complicates the design [6, 7, 41].

To make PCR cycling faster for somewhat larger reaction volumes (μL instead of nL) or high fluid velocities in a continuous flow chip [7], active cooling seems necessary [7]. To increase cooling rates there are several options.

First, compressed air or nitrogen gas can be blown over the chip to actively increase the dissipation of heat [6, 54].

Secondly, endothermic processes, like the evaporation of acetone, can be used in a heat exchanger to cool a micro channel [54]. Parallel to the channel containing the PCR fluid, a channel can be made to flow through acetone. By varying the flow rate, the evaporation of acetone can be influenced and thus the cooling effect can be adjusted. The power consumption is very low as an exception to most active cooling techniques because vacuum is used as the driving force [54]. In case of using gas-permeable PDMS the cooling effect is strengthened because the acetone vaporises through the material, and temperature ramps of about 1 °C s⁻¹ were obtained [54]. Besides these low temperature rates, the possible leakage of a chip, caused by PDMS dissolving and swelling in acetone [55], needs to be taken into account. A simpler solution could be to use water as the fluid for the heat exchanger.

Thirdly, thermoelectric elements are able to generate a heat difference between the two sides of the device based on the Peltier Effect [56], as can be seen in Figure 5. By switching the polarity the elements can both be used for cooling and heating [46, 57]. A cooling rate of 1 °C s⁻¹ was obtained in previous work using a single chamber PDMS chip [9]. Peltier coolers have the advantage of a compact and robust construction, because of the lack of mechanically moving parts [58, 59] and (at the cost of power consumption) can generate high cooling capacities.

![Figure 5 Cross section of a typical thermo electric cooler](image-url)
2.2.3.3 Summarising table

Table 3 Overview of cooling techniques used for PCR chips

<table>
<thead>
<tr>
<th>Cooling method</th>
<th>Cooling capacity</th>
<th>Ease of fabrication</th>
<th>Device footprint</th>
<th>Power consumption</th>
</tr>
</thead>
<tbody>
<tr>
<td>Compressed air</td>
<td>+/-</td>
<td>+</td>
<td>-</td>
<td>+/-</td>
</tr>
<tr>
<td>Heat exchangers</td>
<td>+/-</td>
<td>+/-</td>
<td>-</td>
<td>+/-</td>
</tr>
<tr>
<td>Thermoelectric cooler (Peltier)</td>
<td>+</td>
<td>+</td>
<td>+/-</td>
<td>-</td>
</tr>
<tr>
<td>Passively</td>
<td>-</td>
<td>+</td>
<td>+</td>
<td>++</td>
</tr>
</tbody>
</table>

2.2.4 Heating

The heating methods mentioned in literature can be divided into contact and non-contact heating methods.

2.2.4.1 Contact heating methods

One aspect that contact heating methods have in common is that they add a certain amount of thermal mass to the chip. This reduces the thermal response of the chip when a chamber design is used [15].

The simplest form of contact heating uses metallic heating blocks, heated by resistors. The “large” thermal mass results in lower temperature ramping rates and high power consumption [30]. Nevertheless, it is especially a reliable technique for precise thermal cycling performance [30, 60]. When used in combination with a continuous flow PCR chip with steady state temperature zones, this can be very effective.

A method that complicates the chip design a bit more is heating with thin film heating elements [61]. The heaters are built in the chip located in/near the micro channels, thus in close contact with the PCR mixture. On the one hand, with a more complex design the fabrication methods are costly and reconfiguring the design is not easy [31, 62]. On the other hand, the heating rates, as mentioned in 2.2.1.1, can be very high because of the direct contact with the PCR mixture and the low thermal mass of the heaters [3, 15]. An example of a material used for thin film heaters is indium-tin-oxide (ITO). ITO heaters can be integrated in silicon and/or glass [44] and because it is a transparent material fluorescent monitoring of the DNA multiplication can be used [44].

By adding metallic powder to a PDRM pre-polymer, the PDMS chip itself can be used for heating [45]. This unconventional technique has the advantages that it is cheap and it makes rapid prototyping
possible. Due to the fact that the PDMS micro heater gradually degrades in time, especially at high temperatures, it seems only of value when fixed temperature zones are used [45].

2.2.4.2 Non-contact heating methods
Non-contact heating methods do not add additional thermal mass to the chip and can be used for disposable chips because the heating system is separate from the actual chip.

One way to heat the PCR mixture without direct contact is by using infrared (IR) light. A tungsten lamp can be used to create the IR waves [6]. For a more focused beam, with better power and wavelength control, a laser can be used [30, 63]. The IR heating can be divided into direct and indirect heating of the PCR mixture.

Direct heating means that the IR beam specifically heats the liquid and not the surroundings. By selecting the correct wavelength (in the range of 1-4 μm [64]) the excitation of vibrational bands heats the water. Heating and cooling rates of a 160 nL sample of 65 °C s⁻¹ and 20 °C s⁻¹, respectively, have been reported [64].

A wavelength of 1,460 μm is used [39, 63] for the heating of stationary water droplets in oil. With this wavelength mainly the water and not the oil is heated, resulting in a low power consuming device [63].

The direct IR heating technique has also been used in continuous flow devices [65], but for lower temperatures than required for PCR.

With indirect heating the IR beam heats an absorbing target above the reaction channel. This technique has been used in a continuous flow design [66]. The indirect heating method is preferable when chip materials are used that are not optical transparent for the chosen wavelength.

Other non-contact heating methods include hot air/water cycling, which increases the footprint of the chip, and induction and microwave based heating. Induction based heating has the advantages of low power consumption and it is not necessary to position the PCR mixture very accurate with respect to the heat source [67]. Finally, microwave heating is promising because the PCR efficiency reached almost 70% of conventional PCR while the temperature ramping was shortened and uniform field densities can be delivered by modern microwave cavities [68].
### 2.2.4.3 Summarising table

Table 4 Overview of heating techniques used for PCR chips

<table>
<thead>
<tr>
<th>Heating method</th>
<th>Heating capacity</th>
<th>Ease of fabrication</th>
<th>Device footprint</th>
<th>Power efficiency</th>
</tr>
</thead>
<tbody>
<tr>
<td>IR laser</td>
<td>++</td>
<td>-</td>
<td>-</td>
<td>++</td>
</tr>
<tr>
<td>Hot air</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>--</td>
</tr>
<tr>
<td>External heater</td>
<td>+</td>
<td>++</td>
<td>-</td>
<td>--</td>
</tr>
<tr>
<td>Thin film</td>
<td>++</td>
<td>-</td>
<td>++</td>
<td>+</td>
</tr>
<tr>
<td>Microwave</td>
<td>++</td>
<td>+/-</td>
<td>?</td>
<td>+</td>
</tr>
</tbody>
</table>

### 2.3 Discussion

The most efficient way of heating the PCR sample seems to be the non-contact IR technique, because only the sample and not the surrounding material is heated. However, in recent literature the heating and cooling rates were not impressive: 7 °C s⁻¹ and 2 °C s⁻¹ respectively [6], and even the shortest cycling time mentioned in a recent review [13] was 12 seconds per cycle for a 500 bp amplicon with a total amplification time for 15 cycles of just under four minutes [53].

The chamber based design has impressive heating and cooling rates [3], but the cycle time of 8.5 seconds and an amplification time of 5 minutes and 40 seconds is not even close to the fastest design found in literature: continuous flow with a rather complicated configuration of thin film heaters, insulating air pockets and passive cooling [7]. This design resulted, as mentioned before, in a cycle time 5.2 seconds for a 500 bp amplicon, approaching the kinetic limit of Taq polymerase. Because of the limiting speed of the polymerase the cycle time cannot be shortened by much. A way to get detectable amounts of DNA faster, is by increasing the efficiency of the PCR to get the same yield in fewer cycles.

To be able to detect even the smallest amount of DNA, it would be ideal to have adjustable cycle numbers with real time DNA detection. The cycling can be stopped when DNA is detected or the number of cycles can be increased when there is no DNA detected. However, a close loop design does have the disadvantages of more complex fabrication and control.
2.4 Conclusions

The fastest design seems to be a continuous flow chip with an optimised length of the extension zone (i.e. adjusted to the velocity of the fluid, the cycle number, the speed of the polymerase and the length of the amplicon). On top of that a droplet based design should be used to prevent inhibition and increase the reaction speed of the sample to temperature changes.

The materials should have low thermal conductivity, or insulating materials or air gaps should be used, to make well separated temperature zones possible. Therefore glass or polymers like PDMS are favourable over silicon.

For the heating method thin element heaters in/near the channel should be used to localise the heat as close to the fluid as possible: making efficient heating possible (with minimised losses). This is especially the case for the denaturation zone, where only a small heating zone is required. The extension zone could be heated with an easier to fabricate heating element.

In this work, the focus will be on a PDMS fixed-loop continuous droplet flow chip (on a glass slide), due to ease of fabrication. Heating will be done with thick film heaters and cooling with Peltier elements, as will be discussed in the next section.
3 Experimental research

As mentioned in the introduction, the heating and cooling of the PCR mixture has great influence on the efficiency and specificity of the product. For efficient PCR the denaturation and annealing/extension temperatures have to be reached fast, because transition times after denaturation do not contribute to higher yield [4]. The specificity can be increased by cooling rapidly after denaturation. Then the primer annealing will start instead of formation of non-specific by-products. However, undershooting the annealing temperature could nullify this increased specificity because of false annealing of the primers at lower temperatures (as mentioned in section 2.1.1).

The hypothesis is that by adding an active cooling element the temperature transition from the denaturation to the annealing/extension could go faster thereby increasing the efficiency. In this case ‘cooling’ means the addition of a temperature zone below the temperature of the annealing/extension zone (not necessarily below room temperature).

In this experimental research the effect of adding an active cooling element to a continuous flow chip is investigated. The goal is to increase the cooling rate to increase the efficiency of the PCR with a cycle time towards the kinetic limit of the polymerase.

3.1 Configuration of the PCR chip

The design used in this research is a PDMS/glass hybrid continuous flow chip. The cooling and heating is done using a Peltier element and resistor heaters, respectively.

PDMS is chosen because of the ease of manufacturing, low costs and low thermal conductivity. The latter also holds for glass which is used to support the PDMS. PDMS/glass is proven to maintain a more uniform temperature than pure PDMS chips [69].

The Peltier element and resistor heaters are attached to aluminium blocks placed on the glass side of the chip. With this configuration uniform temperature zones can be established with precise temperature control as well as ease of manufacturing.

The cross section, side and top view of the chip can be seen in Figure 6. The channel width and height are 200 µm. The channel length is adjusted to ensure a duration time of approximately two seconds at the extension temperature when a maximum flow speed (see for more information section 3.3.3) of 5 mm s⁻¹ is used. With the denaturation heater and cooling element width of 2.5 mm (ease of fabrication), this results in a 1:1:2 ratio of denaturation, cooling and extension.
Figure 6 Chip configuration. A: Cross section of part of the test design configuration (not to scale). Dotted lines represent lines of symmetry. B: side view (not to scale). C: top view (drawn to scale)
3.2 Analytical calculations

3.2.1 Heating block temperatures

For heating of the channel, resistive heaters in combination with aluminium blocks are used. To estimate the temperature of the aluminium block, needed to heat the middle of the channel up to the denaturation (or extension) temperature, a first approximation is used based on steady state conduction in 1D (only heat transfer in the x direction) through a composite wall of glass, mineral oil and PDMS.

With similar densities of mineral oil (0.8 g cm\(^{-3}\) [70]) and the PCR mixture (approximately 1 g cm\(^{-3}\)), the aqueous phase droplets will flow in the middle of the channel. Because of the large surface to volume ratio of the droplets (6·10\(^4\) and 1.2·10\(^5\) for droplets with a diameter of 100 and 50 \(\mu\)m respectively) they will respond very quickly to temperature changes of the oil [26]. Therefore the temperature in the middle of the channel calculated with only one oil phase, will be approximately the same as the droplet temperature.

The solution to this problem can be found using an example from chapter 3 of the book ‘Fundamentals of heat transfer’ by Frank P. Incropera [71]. In this example, an equivalent thermal circuit for the steady state conduction through a composite wall is used. In this approximation the liquid is assumed to be stationary and the contact resistances between the surfaces are not taken into account. Also, in the x direction the temperatures of the neighbouring temperature zones are not taken into account.

The one dimensional heat transfer (q\(_z\) in Watt) may be expressed as

\[
q_z = \frac{\text{overall temperature difference}}{\text{sum over thermal resistances}} = \frac{T_1 - T_\infty}{\sum R_t} \tag{1}
\]

For the configuration as can be seen in Figure 7 this results in:

\[
q_z = \frac{T_1 - T_\infty}{\left( \frac{L_a}{k_aA} \right) + \left( \frac{L_b}{k_bA} \right) + \left( \frac{L_c}{k_cA} \right) + \left( \frac{L_d}{k_dA} \right) + \left( \frac{1}{hA} \right)} \tag{2}
\]

The heat transfer coefficient can also be expressed over each element of the wall as follows:

\[
q_z = \frac{T_1 - T_2}{\left( \frac{L_a}{k_aA} \right)} = \frac{T_2 - T_3}{\left( \frac{L_b}{k_bA} \right)} = \frac{T_3 - T_4}{\left( \frac{L_c}{k_cA} \right)} = \frac{T_4 - T_5}{\left( \frac{L_d}{k_dA} \right)} = \frac{T_5 - T_\infty}{\left( \frac{1}{hA} \right)} \tag{3}
\]

Because of the linear temperature variation in the elements of the wall, the temperature in the middle of the channel is:

\[
T_{\text{channel}} = \frac{T_3 - T_4}{2} \tag{4}
\]
By combining these equations the temperature in the middle of the aluminium block (=\(T_1\)) can be calculated. The middle of the aluminium block is taken, because in the practical experiments the thermocouple will be placed here.

Using the values listed in Table 5 and \(T_{\text{channel}} = 94\) °C for the denaturation temperature, and 25 °C for the surrounding air \((T_{\infty})\), \(T_1\) is 94.8 °C. This is only slightly above \(T_{\text{channel}}\) because of the thin glass plate and the insulating capacity of the PDMS layer. For the combined annealing and extension zone a temperature of \(T_{\text{channel}} = 65\) °C, \(T_1\) should be about 65.5 °C.

Table 5 composite wall characteristics [26, 29, 72-74]

<table>
<thead>
<tr>
<th>Section</th>
<th>material</th>
<th>L: thickness of the layer (µm)</th>
<th>(k): thermal conductivity (W m(^{-1}) K(^{-1}))</th>
<th>(h): heat transfer coefficient (W m(^{-2}) K(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>aluminium</td>
<td>2500</td>
<td>200</td>
<td>-</td>
</tr>
<tr>
<td>b</td>
<td>glass</td>
<td>500</td>
<td>0.75</td>
<td>-</td>
</tr>
<tr>
<td>c</td>
<td>mineral oil</td>
<td>3000</td>
<td>0.17</td>
<td>-</td>
</tr>
<tr>
<td>d</td>
<td>PDMS</td>
<td>-</td>
<td>0.21</td>
<td></td>
</tr>
<tr>
<td>e</td>
<td>air</td>
<td>-</td>
<td>-</td>
<td>10 [72, 73]</td>
</tr>
</tbody>
</table>

Figure 7 Composite wall conduction

3.2.2 Heating/cooling length

To estimate the length needed to heat the middle of the channel from 65 °C to 94 °C (and cool the other way around) an analytical solution is applied, using the simplifications that i) all the heat from the heater goes through the glass into the liquid and ii) assuming the channel is insulated because of the thick layer of PDMS with low thermal conductivity. This latter assumption is justified (see verification in appendix I).

Derived from the equation used in chapter 8 of the book ‘Fundamentals of heat transfer’ by Frank P. Incropera [71], the heat transfer from the glass sheet to the oil can be expressed as
\[ q = h \, w \, dx (T_w - T_{oil}(x)) = \dot{m} c_p dT_{oil} \]  

(5)

where \( h \) is the heat transfer coefficient of the channel, \( w \) the width of the channel, \( x \) the distance traveled through the channel, \( T_w \) the wall temperature on the bottom of the channel, \( T_{average} \) the average oil temperature in the channel as a function of \( x \), \( \dot{m} \) the mass flow in \( \text{kg s}^{-1} \) (calculated using \( \dot{m} = A v \rho \), \( A \) being the channel cross section, \( v \) the mean oil velocity and \( \rho \) the density of the oil) and \( c_p \) the specific heat of the used mineral oil.

Equation 5 can be solved for \( T_{oil} \) (derivation can be found in appendix I):

\[ T_{average}(x) = (T_w - T_{in}) \exp\left(-\frac{h \, w \, x}{\dot{m} c_p}\right) + T_w \]  

(6)

![Figure 8 Simplified channel used for the analytical calculation of the length needed for heating/cooling](image)

**Table 6 variables used in the calculation**

<table>
<thead>
<tr>
<th>expression</th>
<th>value</th>
<th>unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \rho ) density</td>
<td>916</td>
<td>Kg m(^{-3})</td>
</tr>
<tr>
<td>( \text{Nu} ) Nusselt number</td>
<td>2.98 [75]</td>
<td>-</td>
</tr>
<tr>
<td>( k ) thermal conductivity</td>
<td>0.17</td>
<td>W m(^{-1}) K(^{-1})</td>
</tr>
<tr>
<td>( c_p ) specific heat</td>
<td>2000</td>
<td>J kg(^{-1}) K(^{-1})</td>
</tr>
<tr>
<td>( w ) width/height of the channel</td>
<td>200 \cdot 10(^{-6})</td>
<td>m</td>
</tr>
<tr>
<td>( v ) average fluid velocity</td>
<td>5 \cdot 10(^{-3})</td>
<td>m/s</td>
</tr>
<tr>
<td>( P ) wetted perimeter</td>
<td>4( w )</td>
<td>-</td>
</tr>
<tr>
<td>( A ) channel cross section</td>
<td>( w \cdot w )</td>
<td>-</td>
</tr>
<tr>
<td>( D_h ) hydraulic diameter</td>
<td>( 4A/P )</td>
<td>-</td>
</tr>
<tr>
<td>( h ) heat transfer coefficient</td>
<td>( \text{Nu} \cdot k/D_h )</td>
<td>-</td>
</tr>
<tr>
<td>( \dot{m} ) mass flow</td>
<td>( v \cdot A \cdot \rho )</td>
<td>-</td>
</tr>
</tbody>
</table>
Plotting this latter equation with $T_w = 94 \, ^\circ C$ and $T_{in} = 65 \, ^\circ C$ and variables as listed in Table 6, results in the blue dotted line in Figure 9. After 3.2 mm 99.9% of $T_w$ (in Kelvin) is reached. For 99.99% of $T_w$ the oil has to travel 4.8 mm. These same values hold for the case $T_w = 65 \, ^\circ C$ and $T_{in} = 94 \, ^\circ C$ (not shown).

When equation 6 is rewritten in

$$x = \ln \left( \frac{T_{in} - T_w}{T_{average} - T_w} \right) \frac{\dot{m} c_p}{h w}$$

(7)

it can be seen that the length needed to reach the desired temperature is proportional to $\dot{m}$ and thus to the velocity of the fluid (equation 8).

$$x \sim \frac{\dot{m}}{h w} = \frac{v \cdot A}{Nu \cdot k}$$

(8)

Thus the time needed to heat or cool is proportional to the channel cross section (when the height and width are equal):

$$t = \frac{x}{v} \sim \frac{A}{Nu \cdot k}$$

(9)

With all other values constant and as listed in Table 6, the heating and cooling time is 0.97 seconds. The average temperature rate is calculated by dividing $T_w - T_{in}$ by the time needed to reach 99.99% of $T_w$. For this approximation this results in a temperature gradient of 30 °C s$^{-1}$ for both cooling and heating.

Reducing the channel cross section will reduce the time (and length) needed to reach the set temperature, as can be seen from equation 9. When a channel width and height of 100 µm are used this results in a temperature gradient of four times that of a 200 x 200 µm channel: 120 °C s$^{-1}$. This is comparable to the high heating and cooling rates mentioned in section 2.2.1.1 for a chamber based chip.

![Figure 9 Plot of the analytically calculated $T_{average}$ along the channel with an inlet and wall temperature of 65 °C and 94 °C, respectively.](image)
3.2.3 Conclusions
From these analytical approximations it can be concluded that the temperature of the heating block should be only slightly higher than the desired temperature (for the middle of the channel) and the time needed to heat from 65 °C to 94 °C is proportional to the channel cross section.

3.3 Numerical calculations
To calculate the temperatures in the final chip more precisely, the chip geometry, as shown in Figure 6, has to be modelled numerically. The simulations have been done with finite element analysis (FEA) software. The influence of adding a cooling block to the chip is investigated and will be compared to the experimental results in section 0. Based on the simulations a chip design can be made with (near) optimal channel lengths to let the fluid just the desired denaturation temperature and keep it for sufficient time (two seconds as mentioned in 2.1.3.1) at the extension temperature and eventually make the PCR cycle as fast and efficient as possible.

3.3.1 Validation
To validate the results of the FEA simulations, four elements used in the simulation are separately compared to examples that can be analytically calculated, as can be seen in in appendix II.

1. Steady state conduction
2. Convective heating/cooling
3. Pressure drop
4. Symmetry boundary condition

From these validations can be concluded that the results of the FEA simulations are in close agreement with the analytical calculations. Therefore it is assumed a combination of these elements will also result in representative results.

3.3.2 Configuration and assumptions
The geometry used in the simulations is represented in Figure 10 and Figure 11. The dimensions of the chip are stated in Table 8 and are mainly chosen for ease of fabrication in the experimental section.

Table 7 Geometry dimensions used in the simulation

<table>
<thead>
<tr>
<th>Geometry</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aluminium height</td>
<td>5</td>
<td>mm</td>
</tr>
<tr>
<td>Annealing/extension zone width (a)</td>
<td>5.5 (2x)</td>
<td>mm</td>
</tr>
<tr>
<td>Cooler width (b)</td>
<td>2.5</td>
<td>mm</td>
</tr>
<tr>
<td>Denaturation zone width (c)</td>
<td>4.5</td>
<td>mm</td>
</tr>
<tr>
<td>Distance between aluminium blocks</td>
<td>0.5</td>
<td>mm</td>
</tr>
<tr>
<td>Glass height</td>
<td>0.5</td>
<td>mm</td>
</tr>
<tr>
<td>PDMS height</td>
<td>3</td>
<td>mm</td>
</tr>
<tr>
<td>Channel height</td>
<td>200</td>
<td>µm</td>
</tr>
<tr>
<td>Channel width</td>
<td>200</td>
<td>µm</td>
</tr>
</tbody>
</table>

To reduce the computational power needed for the simulation, several assumptions and simplifications were made. First of all only a single cycle in the middle of the chip, as indicated on the
right of Figure 10, is simulated and simplified to a straight channel, as can be seen on the left side of Figure 10.

The second simplification is the line symmetry with respect to the dotted lines in Figure 11 (one through the middle of the channel and one on the left side of the geometry). Because of these symmetries the temperature gradient at these boundaries is zero.

For the liquid flowing through the channel laminar flow was assumed, with no slip conditions at the channel boundaries as in previous simulations mentioned in literature [7, 26].

Other boundary conditions include the temperature on the bottom of the aluminium blocks and the convective cooling at the sides of the aluminium blocks and the top of the PDMS layer (these values can be found in the next section; Table 9).

Figure 10 Left: Side view of the geometry used in the simulation representing one cycle as in the dotted area in the right figure. Right: top view of simplified chip. Arrows indication flow direction. Colours represent, denaturation zone (red), cooling element (yellow), annealing/extension zone (orange).

Figure 11 Cross section of the simulated geometry. The dotted line represents a line of symmetry. On the top and bottom the temperature boundary conditions are applied.
3.3.3 Methods

The FEA program used is called COMSOL Multiphysics® version 4.3.1.115. Two sets of so-called “physics” were used: the “Laminar flow” and “heat transfer” (in solids and fluids) physics. The results from the “Laminar flow” simulations were used in the heat transfer simulations. By keeping these physics separate, computational time was reduced dramatically compared to the combined physics called “Conjugate Heat Transfer”. Because of the assumption of constant fluid properties (independent of temperature), the results from the combined physics did not differ from the separated physics.

The mesh used for the simulations was a so called “extra fine physics-controlled mesh” with almost 38,000 elements, with a minimal element size of 29 µm. The plot of the mesh can be seen in Figure 12.

The simulations were made using the material properties listed in Table 8. The temperatures set as boundary conditions at the bottom of the aluminium blocks (for the annealing/extension, denaturation and cooling zones) are listed in Table 9. The temperature of the air is set to 25 °C with a heat transfer coefficient of 10 W m⁻² K⁻¹; the same as in the analytical calculations.

The droplets moving in the middle of the channel will have approximately the velocity of the fluid in the middle of the channel (v_{center}). The residence time of the droplets in the different temperature zones should be calculated using this center velocity. That is why v_{center} is given, instead of v_{average} (over the channel cross section) or the flow rate in µL min⁻¹ (as indicated on syringe pumps available in the MCS laboratory).

Table 8 Material properties [26, 29, 72-74] used in simulations

<table>
<thead>
<tr>
<th></th>
<th>Specific Heat (J kg⁻¹ K⁻¹)</th>
<th>Thermal conductivity (W m⁻¹ K⁻¹)</th>
<th>Density (kg m⁻³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PDMS</td>
<td>1500</td>
<td>0.21</td>
<td>970</td>
</tr>
<tr>
<td>Glass</td>
<td>835</td>
<td>0.75</td>
<td>2500</td>
</tr>
<tr>
<td>Mineral oil</td>
<td>2000</td>
<td>0.17</td>
<td>916</td>
</tr>
</tbody>
</table>
Table 9 Velocities and temperatures used in simulations

<table>
<thead>
<tr>
<th>( v_{\text{center}} ) (mm s(^{-1}))</th>
<th>( T_{\text{denaturation}} ) (°C)</th>
<th>( T_{\text{cool}} ) (°C)</th>
<th>( T_{\text{annealing/extension}} ) (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>97.0</td>
<td>60</td>
<td>65.5</td>
</tr>
<tr>
<td>13</td>
<td>97.8</td>
<td>60</td>
<td>65.6</td>
</tr>
<tr>
<td>23</td>
<td>99.7</td>
<td>58</td>
<td>65.6</td>
</tr>
</tbody>
</table>

3.3.4 Results and discussion

In Figure 13 the simulated temperatures in the middle of the channel are shown for a 200 x 200 µm channel for three different fluid velocities with and without a cooling element. The cooling rates of the cooled chip (solid lines) are higher than a chip without active cooling (dotted lines). If the temperature of the cooler is set at 60 °C \(^1\), the fluid “undershoots” the extension temperature at low velocities at both the transition from the extension to the denaturation zone (indicated with ① in Figure 13) and from the denaturation to the extension zone (indicated with ② in Figure 13). With increasing velocity this ‘dip’ reduces at ②, but still visible at ① even at higher velocities because of the smaller temperature difference between \( T_{\text{extension}} \) and \( T_{\text{cool}} \) than between \( T_{\text{denaturation}} \) and \( T_{\text{cool}} \).

For the lower flow speeds (\( v_{\text{center}} \) 5 and 13 mm s\(^{-1}\)) the \( T_{\text{cool}} \) has to be increased to reduce the “undershoot” of the extension temperature. In Figure 14 the temperature versus time is plotted with \( T_{\text{cool}} \) of 64, 62 and 58 °C for \( v_{\text{center}} \) of 5, 13 and 23 mm s\(^{-1}\), respectively.

The average heating (①) and cooling (②) rates for different velocities are listed in Table 10. These values differ quite a bit from the heating and cooling rate of 30 °C s\(^{-1}\) calculated in section 3.2.2. The difference can be explained by the fact that the transition from 94 °C to 65 °C (or the other way around) is not instantaneously (as assumed in the analytical calculation). The conductivity of the glass results in a gradual temperature gradient. At low velocities the liquid can adjust to this wall temperature, resulting in a lower heating (and cooling) rate.

Besides a more gradual change of wall temperature, the maximum wall temperature in the simulations is higher than 94 °C (as used in the analytical calculation) to ensure the temperature in the middle of the channel reaches 94 °C. This results in higher heating rates for higher velocities.

A final difference is that in the simulation the temperature in the middle of the channel is calculated instead of the average liquid temperature.

Table 10 Average heating and cooling rates for different fluid velocities in a 200 x 200 µm channel

<table>
<thead>
<tr>
<th>Active/passive cooling</th>
<th>( v_{\text{center}} ) (mm s(^{-1}))</th>
<th>Heating rate (°C s(^{-1}))</th>
<th>Cooling rate (°C s(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Active (64 °C)</td>
<td>5</td>
<td>22</td>
<td>29</td>
</tr>
<tr>
<td>Passive</td>
<td>5</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td>Active (62 °C)</td>
<td>13</td>
<td>48</td>
<td>72</td>
</tr>
<tr>
<td>Passive</td>
<td>13</td>
<td>46</td>
<td>46</td>
</tr>
<tr>
<td>Active (58 °C)</td>
<td>23</td>
<td>80</td>
<td>123</td>
</tr>
<tr>
<td>Passive</td>
<td>23</td>
<td>85</td>
<td>73</td>
</tr>
</tbody>
</table>

\(^1\) Simulations with the cooling elements passively cooled were made; the passively cooled elements reached a temperature of about 70 °C. So active cooling is needed to reach 60 °C.
Figure 13: Temperature of the middle of the channel versus distance. a, b, and c indicate the positions of the aluminium blocks at \( T_{\text{annealing/extension}}, T_{\text{cool}}, \) and \( T_{\text{denaturation}} \) (as listed in Table 9), respectively. The channel dimensions are 200 x 200 \( \mu \)m.

In Figure 15 a close up of Figure 14 is shown for \( v_{\text{center}} = 23 \text{ mm s}^{-1} \). As indicated by the black dotted lines the time at the extension temperature is different for a chip with or without active cooling. The addition of an active cooling element decreases the transition time from \( T_{\text{denaturation}} \) to \( T_{\text{extension}} \) by about 3x (x being 0.05 seconds), while at the heating side the residence time at \( T_{\text{extension}} \) is shortened by 1x. This gives a time reduction of about 2x = 0.1 seconds for one cycle.

For lower flow speeds this time reduction increases, as can be seen in Table 11. However, the relative time reduction, i.e. when expressed as percentage of the time that a droplet is not at the extension temperature (0.5, 1 and 2.5 seconds for 5, 13 and 23 mm s\(^{-1}\), respectively), is 20% for all simulated velocities.
Figure 14 Temperature versus time for a $v_{\text{center}}$ of 5, 13 and 23 mm s$^{-1}$ in a 200 x 200 µm channel. $T_{\text{cool}}$ is set at 64, 62 and 58 °C, respectively.

Figure 15 Close up of Figure 14 for a $v_{\text{center}}$ of 23 mm s$^{-1}$ in a 200 x 200 µm channel. The black dotted lines indicate the difference in time at the extension temperature.
Table 11 Time savings by addition of a cooling element for different fluid velocities in a 200 x 200 µm channel

<table>
<thead>
<tr>
<th>Active/passive cooling</th>
<th>( v_{\text{center}} ) (mm s(^{-1}))</th>
<th>Heating time (s)</th>
<th>Cooling time (s)</th>
<th>Time savings (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Active (64 °C)</td>
<td>5</td>
<td>1.3</td>
<td>1.0</td>
<td>0.7</td>
</tr>
<tr>
<td>Passive</td>
<td>5</td>
<td>1.5</td>
<td>1.5</td>
<td></td>
</tr>
<tr>
<td>Active (62 °C)</td>
<td>13</td>
<td>0.6</td>
<td>0.4</td>
<td>0.2</td>
</tr>
<tr>
<td>Passive</td>
<td>13</td>
<td>0.6</td>
<td>0.6</td>
<td></td>
</tr>
<tr>
<td>Active (58 °C)</td>
<td>23</td>
<td>0.4</td>
<td>0.2</td>
<td>0.1</td>
</tr>
<tr>
<td>Passive</td>
<td>23</td>
<td>0.3</td>
<td>0.4</td>
<td></td>
</tr>
</tbody>
</table>

The analytical calculations show that the transition times (from extension to denaturation and the other way around) are proportional to the channel cross section. Therefore simulations are made with a channel of 100 x 100 µm to compare this to the 200 x 200 µm channel. The results of both channel dimensions are plotted in Figure 16.

Because of the smaller dimensions and the lower thermal mass (smaller volume) in case of a 100 x 100 µm channel, the response of the channel temperature is faster to the changing wall temperature compared to the 200 x 200 µm channel. The transition times for both heating and cooling are shorter and (especially at higher velocities) the dip between \( T_{\text{extension}} \) and \( T_{\text{denaturation}} \) is reduced. This latter is possible because of the higher \( T_{\text{cool}} \) (64 °C for all velocities).

![Figure 16 Temperature versus time for a \( v_{\text{center}} \) of 5, 13 and 23 mm s\(^{-1}\) in a 100 x 100 µm (\( T_{\text{cool}} = 64 \) °C for all velocities) and 200 x 200 µm channel (\( T_{\text{cool}} \) is set at 64, 62 and 58 °C, respectively).](image)

Although the transition times are shorter for the 100 x 100 µm channel, they are not a quarter of the heating and cooling times of 200 x 200 µm channel (as expected from equation 9 in section 3.2.2). A
possible explanation for this is the gradual temperature gradient of the walls of the channel. To verify this, simulations with a smaller heater were made. The temperatures of a configuration with a smaller heater width (2.5 instead of 4.5 mm) for the denaturation zone are shown in Figure 17. The figure shows that time for denaturation can be (further) reduced by narrowing the heater.

![Figure 17 Temperature versus time for a \( v_{\text{center}} \) of 5, 13 and 23 mm s\(^{-1}\) in a 100 x 100 µm (\( T_{\text{cool}} = 64 ^\circ\text{C} \) for all velocities) for a denaturation heating element size of 2.5 and 4.5 mm.]

Two final remarks about the temperature cycles simulated in this section: i) the \( T_{\text{extension}} \) used in the simulation is 65 °C while the optimal temperature for the Taq or KOD polymerase is higher (72 and 75 °C, respectively). However, the effect of the cooling element at higher temperatures (not shown) is the same. ii) The undershoot at ② in Figure 13, might (especially when a higher \( T_{\text{extension}} \) is used) increase the efficiency of the PCR cycle, because at lower temperature the annealing is favoured. By doing experiments with PCR samples the effect of this dip could be investigated: will it improve the annealing and efficiency or just increase the false annealing?

### 3.3.5 Conclusions

Adding a cooling element improves the thermal cycling. At the cost of a temperature dip at the end of the extension zone, the transition of denaturation to extension is faster. For all simulated velocities in a 200 x 200 µm channel, the cooling element ensures a 20% decrease of the combined heating and cooling time (per cycle). Furthermore, both smaller channels and the use of narrower denaturation heaters show possibilities of shorter cycling times.

In conclusion, the cycle time can be reduced by using smaller channels, with higher fluid velocities and a cooling element.
3.4 Experiments

3.4.1 Materials and Methods

3.4.1.1 The chip
The chip design can be seen in Figure 18. It is almost the same as described in section 3.1, except for the addition of three side channels of 100 x 100 µm. These channels are used as inserts for the thermocouples.

![Chip design made in CleWin. The green areas indicate the positions of the heating and cooling blocks. The three grey lines on the right indicate the channels for the thermocouples.](image)

3.4.1.2 PDMS and glass
The PDMS was with the PDMS base silicone (Dow Corning Sylgard® 184 Base silicone elastomer) and the curing agent (Dow Corning Sylgard® 184 curing agent silicone elastomer) in a 1:10 ratio. After mixing the two components and degassing the mixture in a vacuum chamber, the PDMS was poured over the SU-8 mold with the pattern as can be seen in Figure 18. The PDMS was cured at 80 °C for four hours. Finally the PDMS was cut out and paced on a glass slide and bonded at 40 °C overnight. The 0.5 mm glass slides were not available in time. Instead, a 1 mm thick microscope slide was used.

3.4.1.3 Heaters and cooler
The heaters for both the denaturation and extension zone were made by attaching thick film heaters (CGS MPC55R0J) to aluminium blocks (2.5 x 5 x 15 mm and 5 x 5 x 15 mm for denaturation and extension, respectively).

The cooling element was made of an aluminium block of 2.5 x 5 x 20 mm (somewhat larger than the heating blocks) to leave space for the Peltier elements (Global Component Sourcing ET-007-06-11) as can be seen in Figure 19. To improve the cooling capacity of the Peltier elements aluminium fins
(mounted on a copper block) were attached to the heat sink. The power supply for the Peltier elements was from Agilent (E3633A DC Power Supply).

All connections (between the aluminium, heaters, Peltier elements and fins) were made with (blue) thermally conductive adhesive (Fischer Elektronik WLK 5). The configuration was assembled on a microscope slide for stability (Figure 20). The heater for the extension zone was covered with a thin layer of the thermal conductive glue to ensure a flat surface for the chip.

![Figure 19 Close up of the Peltier elements attached to the aluminium cooling block](image1)

![Figure 20 Heating and cooling configuration.](image2)

### 3.4.2 Temperature control

To control the temperatures of the heating blocks, 1 mm thermocouples (Omega Pt 100) were inserted in the centre of both aluminium blocks. The thermocouples and the heating elements were
connected to two home built temperature controllers (Pinotech). These temperature controllers have an accuracy of about +/- 0.2 °C around the setpoint.

In the middle of the cooling block there was also a 1 mm thermocouple mounted. The read out of this thermocouple was done with a thermometer (Yu Ching Technology Co., Ltd. YCT-747D Data Logger Thermometer). The temperature could be adjusted manually by altering the current and/or voltage of the power supply.

3.4.3 Temperature measurements in chip

The channel width and height of 200 µm were chosen to be large enough to insert the thermocouples for temperature measurement in the channel. The inserts for the thermocouples (grey lines on the right of Figure 18), with a width and height of 100 µm, were made to locate thermocouples (with a wire diameter of 25 µm; OMEGA® fine-diameter thermocouple CHAL-001) in the channel. Such inserts were positioned in the denaturation zone, the middle of the cooling zone and the extension zone.

However, mounting the thermocouples in the channel was difficult. First of all the thermocouples were very fragile. During assembly of the chip they were easily destroyed. Secondly, the thermocouple did not fit in the 100 µm wide insert channel, because the tip spaced both 25 µm wires (Figure 21).

![Figure 21 Thermocouple (wire diameter of 25 µm) in the channel](image)

One chip (with a thermocouple inside the channel) suffered from leakage due to bonding problems of the PDMS to the glass with a thermocouple in between (Figure 22). Moreover, the thermocouple was broken while connecting it to the thermometer.
Because of these difficulties a new approach was chosen. Only one thermocouple was put on a blank glass slide (Figure 23) (thus, no PDMS fluidic structure on glass). Subsequently, the heating/cooling unit was moved with respect to the thermocouple in such way that the tip was positioned at each of the three locations, indicated in Figure 24. Measurements were taken approximately 50 µm above the glass, with the thermocouple surrounded by air, immersed in a droplet of water or a droplet of mineral oil (Sigma-Aldrich® M5904). A thermal conductive gel (Dow Corning DC4) was put between the heating and cooling element and the glass slide to ensure good thermal contact.
3.4.4 Results and discussion

The following temperatures (Table 12 and Table 13) were measured with the thermocouples at positions ①, ② and ③, with/without cooling and for various surrounding media (now flow/static).

Table 12 Measurements without active cooling (passive)

<table>
<thead>
<tr>
<th>Measurement I.D.</th>
<th>Setpoints [°C]</th>
<th>Position thermocouple</th>
<th>Medium on tip thermocouple</th>
<th>Measured temperature [°C]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$T_{\text{denat}} = 94.0 \pm 0.2$</td>
<td>①</td>
<td>Air</td>
<td>83.0 ± 0.3</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td></td>
<td>$H_2O$</td>
<td>71.5 ± 0.5</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 66.4 \pm 0.4$</td>
<td></td>
<td>Oil</td>
<td>87.1 ± 0.3</td>
</tr>
<tr>
<td>2</td>
<td>$T_{\text{denat}} = 102.0 \pm 0.2$</td>
<td>①</td>
<td>Air</td>
<td>88.2 ± 0.3</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td></td>
<td>$H_2O$</td>
<td>72.5 ± 0.5</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 68.7 \pm 0.2$</td>
<td></td>
<td>Oil</td>
<td>91.7 ± 0.5</td>
</tr>
<tr>
<td>3</td>
<td>$T_{\text{denat}} = 104.0 \pm 0.2$</td>
<td>①</td>
<td>Air</td>
<td>89.0 ± 0.3</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td></td>
<td>$H_2O$</td>
<td>81.3 ± 0.4</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 70.2 \pm 0.5$</td>
<td></td>
<td>Oil</td>
<td>94.3 ± 0.2</td>
</tr>
<tr>
<td>4</td>
<td>$T_{\text{denat}} = 94.0 \pm 0.2$</td>
<td>③</td>
<td>Air</td>
<td>64.5 ± 0.3</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td></td>
<td>$H_2O$</td>
<td>60.2 ± 0.4</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 66.0 \pm 0.3$</td>
<td></td>
<td>Oil</td>
<td>66.2 ± 0.4</td>
</tr>
<tr>
<td>5</td>
<td>$T_{\text{denat}} = 94.0 \pm 0.2$</td>
<td>③</td>
<td>Air</td>
<td>61.3 ± 0.5</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td></td>
<td>$H_2O$</td>
<td>55.5 ± 0.5</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 67.5 \pm 0.3$</td>
<td></td>
<td>Oil</td>
<td>63.2 ± 0.5</td>
</tr>
<tr>
<td>6</td>
<td>$T_{\text{denat}} = 94.0 \pm 0.2$</td>
<td>③</td>
<td>Air</td>
<td>62.8 ± 0.7</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 67.0 \pm 0.2$</td>
<td></td>
<td>$H_2O$</td>
<td>57.5 ± 0.5</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 67.3 \pm 0.3$</td>
<td></td>
<td>Oil</td>
<td>64.8 ± 0.5</td>
</tr>
</tbody>
</table>
Power to the Peltier elements: 0.13 W for all measurements below.

Table 13 Measurements with active cooling: 0.13 W

<table>
<thead>
<tr>
<th>Measurement I.D.</th>
<th>Setpoints [°C]</th>
<th>Position thermocouple</th>
<th>Medium on tip thermocouple</th>
<th>Measured temperature [°C]</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>$T_{\text{denat}} = 94.0 \pm 0.2$</td>
<td>☀️</td>
<td>Air</td>
<td>83.5 ± 0.9</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td>☀️</td>
<td>H$_2$O</td>
<td>55.5 ± 0.5</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 61.0 \pm 0.2$</td>
<td>☀️</td>
<td>Oil</td>
<td>63.2 ± 0.5</td>
</tr>
<tr>
<td>8</td>
<td>$T_{\text{denat}} = 104.0 \pm 0.2$</td>
<td>☀️</td>
<td>Air</td>
<td>85.8 ± 0.6</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td>☀️</td>
<td>H$_2$O</td>
<td>80.0 ± 1</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 65.2 \pm 0.1$</td>
<td>☀️</td>
<td>Oil</td>
<td>94.7 ± 0.8</td>
</tr>
<tr>
<td>9</td>
<td>$T_{\text{denat}} = 94.0 \pm 0.2$</td>
<td>☀️</td>
<td>Air</td>
<td>63.5 ± 0.5</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td>☀️</td>
<td>H$_2$O</td>
<td>57.0 ± 0.4</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 62.7 \pm 0.2$</td>
<td>☀️</td>
<td>Oil</td>
<td>63.9 ± 0.3</td>
</tr>
<tr>
<td>10</td>
<td>$T_{\text{denat}} = 94.0 \pm 0.2$</td>
<td>☀️</td>
<td>Air</td>
<td>60.5 ± 0.5</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{ext}} = 65.0 \pm 0.2$</td>
<td>☀️</td>
<td>H$_2$O</td>
<td>56.4 ± 0.4</td>
</tr>
<tr>
<td></td>
<td>$T_{\text{cool}} = 60.9 \pm 0.5$</td>
<td>☀️</td>
<td>Oil</td>
<td>61.5 ± 0.3</td>
</tr>
</tbody>
</table>

The temperatures measured for all positions show a better heat transfer (i.e. higher temperature) when mineral oil was added on the surface. The addition of water resulted in lower temperatures because of the evaporation of the water.

By comparing measurements 4 and 9 it can be seen that with this configuration it is possible to cool the glass slide between the denaturation and extension zone in static conditions. This (combined with the simulations) indicates the possibility of faster temperature transitions when a liquid flow is used.

From the results of measurements 3 and 8 it can be seen that in order to reach a temperature of 94 °C of mineral oil, the heating block needs to be set at 104 °C. This is quite higher than the 94.8 °C calculated in 3.2.1 and simulated in 3.3.4, which is explained by the thicker glass used in the experiments and the absence of insulating PDMS. However, when taken into account the thicker glass and the absence of PDMS, the analytical calculation gives 95.4 °C and the simulation 99.5 °C (not shown) as the temperature for the heating block. An explanation might be the non-perfect thermal contact between the heating block and the glass slide, as well as heat loss to the glass slide at the bottom of the heating/cooling configuration. The same arguments hold for the extension zone (measured 67 °C (measurement 6), calculated: 65.5 °C).

To improve the bonding between the glass and PDMS, larger inserts for the thermocouples could be used. After mounting the thermocouples in the correct position, some PDMS could be added from the outside of the chip to seal the insert channels. Another possibility is to fix the thermocouples to the glass and then spin coat a thin layer of PDMS before attaching the PDMS chip. The heat transfer to the fluidic channel is reduced because of the use of extra low conductive PDMS, but there will be less chance of leakage of fluids.

When thermocouples could be mounted in the PDMS chip, the heating and cooling elements could be attached directly to the glass slide, ensuring good thermal contact. With the configuration used, it is not easy to ensure a flat surface and good contact between the heating and cooling elements and
the glass slide. The electrical compound might have caused a direct thermal path between heating and cooling blocks (rather than via the glass slide) which makes the separation of the temperature zones less well defined.

Based on the difficulties with the small (25 µm) thermocouples, it seems reasonable to use larger thermocouples (and larger channels). However, larger thermocouples have a larger thermal mass that influences the measurements (less accurate).

Other temperature measurement techniques were considered. For example temperature measurements using a thermal camera (not available, or too low resolution at < 100 °C) or temperature dependent fluorescence of Rhodamine (or Rhodamine dextran), as investigated earlier in the MCS group [76]. However, this latter technique was not used, because initial tests showed that images (not shown) made through the PDMS (needed to estimate the temperature in the channel) were blurry. This could be solved by taking images through the glass with the heating/cooling configuration on the PDMS side. However, during the simulations there was also a design tested with a cooling element embedded in the PDMS instead of beneath the glass, but this did not (even close) work as efficient as a cooler on the glass side. PDMS has an even lower thermal conductivity than glass and the distance between the cooling element and the channel will be larger when PDMS instead of glass is used.

3.4.5 Conclusions
From the experiments it can be concluded that i) the setpoint temperature of the heating blocks should be higher than analytically and numerically calculated, ii) the temperature measurement technique and/or the fabrication process should be reconsidered to get temperature measurements inside a channel with flowing liquid, and most important, iii) the cooling element does reduce the temperature between the denaturation and extension zone, making faster temperature transitions possible.
4 Conclusions

4.1 Main conclusions

From the literature research a chip design is proposed for the fastest amplification time: a continuous droplet flow chip with an optimised length of the extension zone (i.e. adjusted to the velocity of the fluid, the cycle number, the speed of the polymerase and the length of the amplicon).

The materials of which this chip is composed should have low thermal conductivity, to make well separated temperature zones possible. As heating method thin element heaters in/near the fluid channel should be used, to localise the heat close to the fluid (for efficient heating with minimised losses).

Simulations showed that adding a cooling element between the denaturation and elongation zones improves the thermal cycling. For all simulated velocities in a channel with a cross section of 200 x 200 µm, the cooling element ensures a 20% decrease of the combined heating and cooling time (per cycle). Both smaller channels and the use of narrower denaturation heaters might be possibilities of further reducing the cycling time.

Experiments with PDMS/glass chips with external heating/cooling showed that the cooling element indeed reduces the temperature between the denaturation and extension zone. In combination with the simulations, it can be concluded that the temperature transition time between the denaturation and extension zone will be reduced by addition of a cooling element, thus making faster temperature transitions possible.

4.2 Recommendations

i) To verify the influence of the cooling element on the temperatures in flowing liquid, a chip design should be used with larger insertion channels for the thermocouples. Alternatively, a different temperature measurement technique could be used. For example, the fluorescence temperature measurement technique could be used when transparent ITO thin film heaters are implemented in the channel, instead of external aluminium heating blocks. The images can then be taken from the glass side. Another alternative is the use of the ITO thin films as thermocouple inside the channel.

ii) The experimental research shows that faster temperature transitions are possible by adding a cooling element. To investigate the effect of the faster transitions on the PCR reaction, experiments with a PCR mixture in droplets should be done. Does the cooling element indeed increase the efficiency and reduce the cycling time of the PCR?

iii) In section 2.2.4.2 it is mentioned that a direct IR heating technique has been used in continuous flow devices, but for lower temperatures than required for PCR. Further research into to the possibilities of this technique for PCR is recommended. It seems a promising technique when only the droplet could be heated by a laser and the oil is at a steady temperature of 65-70 °C. The droplets cool rapidly in the oil: no active cooler needed. Overall this might result in a fast and low power consuming device.
5 References


Appendices

I. Analytical Calculations

Deriving $T_{\text{average}}$

$$ q = h \int \frac{w dx}{\dot{m} c_p} (T_w - T_{\text{average}}(x)) = \dot{m} c_p \frac{dT_{\text{average}}}{T_w - T_{\text{average}}} $$  

i.

$$ \frac{h \int \frac{w dx}{\dot{m} c_p}}{\dot{m} c_p} = \frac{dT_{\text{average}}}{T_w - T_{\text{average}}} $$  

ii. 

$$ \int_0^x \frac{h \int \frac{w dx}{\dot{m} c_p}}{\dot{m} c_p} = \int_{T_{\text{in}}}^{T_w} \frac{dT_{\text{average}}}{T_w - T_{\text{average}}} $$  

iii.

$$ \frac{h \int \frac{w x dx}{\dot{m} c_p}}{\dot{m} c_p} = \ln \left( \frac{T_w - T_{\text{in}}}{T_w - T_{\text{average}}(x)} \right) $$  

iv.

$$ T_{\text{average}}(x) = (T_w - T_{\text{in}}) \exp \left( - \frac{h \int \frac{w x dx}{\dot{m} c_p}}{\dot{m} c_p} + T_w \right) $$  

v.

Insulation assumption

To verify if the assumption of an insulated channel is justified, the heat transfer through the PDMS is now included. It adds a thermal resistance and a temperature difference to equation 5 on page 23:

$$ q = \left( \frac{1}{L} \left( \frac{T_w - T_{\text{average}}(x)}{k_{\text{PDMS}}} + \frac{T_{\text{average}}(x) - T_\infty}{R_{\text{air}}} \right) \right) \int \frac{w dx}{\dot{m} c_p} $$  

vi.

with $L$ being the height and $k_{\text{PDMS}}$ the thermal conductivity of the PDMS layer.

Solving this for $T_{\text{average}}(x)$ results in

$$ T_{\text{average}}(x) = R_{\text{tot}} \left( \frac{T_w}{R_{\text{oil}}} + \frac{T_{\text{in}}}{R_{\text{PDMS}}} \right) + \left( \frac{T_{\text{in}}}{R_{\text{tot}}} - \frac{T_w}{R_{\text{oil}}} - \frac{T_{\text{in}}}{R_{\text{PDMS}}} \right) \exp \left( - \frac{h \int \frac{w x dx}{\dot{m} c_p}}{\dot{m} c_p} \right) $$  

vii.

Using the values for the PDMS as can be found in Table 5, there is no significant difference compared to the insulation assumption, as can be seen in Figure 25.
II. Simulations

Validation of:

Steady state conduction
As mentioned in section 3.2.1, the temperatures in a composite wall for steady state conduction can be calculated using an equivalent thermal circuit. The analytical calculations exactly match (difference smaller than $1 \cdot 10^{-5}$ °C) the simulation results from the FEA software, as can be seen in Figure 26. Thus the steady state conduction of the simulation can be assumed to be correct.
Figure 26 verification steady state conduction through a composite wall. The coloured dot represent the analytically calculated temperatures on the boundaries of the different layers.

Convective heating/cooling

For the convection part of the simulation, the analytical result of section 3.2.2 can be used. The results of the simulation are shown in Figure 27. There is a slight difference between the analytical and the simulated values. With the values of the simulation it takes 1.55 mm instead of 1.2 mm to reach 99.999% of $T_w$ in a 100 x 100 µm channel.

Figure 27 Analytical calculation of temperature along a 100 x 100 µm channel
Pressure drop

The pressure drop is calculated with the Fanning friction factor and the derived Fanning pressure drop equation (equation 2) [75]

\[ \Delta p = p_1 - p_2 = 4 \cdot f \cdot \frac{L}{D_h} \cdot \frac{1}{2} \rho \langle v \rangle^2 \] \hspace{1cm} \text{viii.}\]

with \( p \) the pressure in Pa, \( f \) the Fanning friction factor, \( L \) the length of the channel in \( m \), \( D_h \) the hydraulic diameter of the channel in \( m \), \( \rho \) the density in \( \text{kg/m}^3 \) and \( \langle v \rangle \) the mean velocity of the liquid in \( \text{m/s} \).

The hydraulic diameter is defined [71, 75] as

\[ D_h \equiv \frac{4A}{S} \] \hspace{1cm} \text{ix.}\]

with \( A \) the cross sectional area of flow and \( S \) the wetted perimeter of the channel. For cylindrical channels \( D_h \) is equal to the diameter.

For laminar flow in a cylindrical channel \( f=16/\text{Re} \) in [75], with \( \text{Re} \) the Reynolds number

\[ \text{Re} = \frac{\rho \langle v \rangle D_h}{\mu} \] \hspace{1cm} \text{x.}\]

with \( \mu \) the dynamic viscosity in \( \text{kg/(m\cdot s)} \).

Combining equation viii, ix and x with the ‘\( f \)’ for laminar flow results in

\[ \Delta p = \frac{32L \langle v \rangle \mu}{D_h^2} \] \hspace{1cm} \text{xi.}\]

For a cylindrical channel with a diameter of 100 \( \mu \text{m} \) and a length of 1 cm with a flow of liquid with a viscosity of 1 mPa\( \cdot \text{s} \) and mean velocity of 5 mm/s the pressure drop is 160 Pa. This is within 1% of the pressure drop calculated with the FEA software.

Symmetry

The symmetry boundary for the flow is used in the simulation in the middle of the channel. This reduces the number of degrees of freedom and thus the computation time.

The symmetry boundary for the flow in the channel does not affect the outcome of the pressure drop calculation as given above. This was checked using a square channel with width and height 100 \( \mu \text{m} \) and a length of 1 cm and the same channel cut in half with added symmetry boundary as can be seen in Figure 28 Pressure drop symmetry geometries Figure 28. For square channels \( f=14.2/\text{Re} \) [77] resulting in a pressure drop of 142 Pa which is in agreement with the simulations.
Figure 28 Pressure drop symmetry geometries
III. Assignment

Assignment Lab-on-a-chip for forensics

Assignment E: Fast temperature cycling for PCR-based DNS amplification - Physics / Physical Chemistry

Introduction:

The number and variety of forensic traces found at a crime scene is enormous. The term forensic science is therefore very broad and can be divided in several expertise areas, such as DNA profiling, blood spatter analysis, explosives and illicit drugs. It is a clear desire of forensic investigators that analyses should be simple, fast, robust, cheap and have high sensitivity and selectivity. Devices with these specifications can be used directly at the crime scene and are especially useful as they can provide immediate information to the police investigators. Most ideal would be a mobile forensic lab for collecting, screening and analysis of the evidence. So-called 'lab-on-a-chip' (LOC) systems can speed up the analysis, are compact, can easily be integrated, limit the risk of contamination and can be used by people who are not technically trained.

However, micro-devices for forensic investigation hardly exist [1]. Experts in LOC technology and/or nanotechnology do not have experience and knowledge about forensic science. On the other hand, forensic experts are in general not familiar with LOC devices. The two disciplines have not yet been combined often in order to obtain an LOC device for forensic research. Combining both disciplines is a goal of this assignment.

Theory:

Several advantages of lab-on-a-chip devices are the fast analysis time, high throughput, minimal amount of analyte material needed, less waste and compactness [2]. Exactly these benefits are the desires of forensic scientists. Other advantages of LOC are limitation of (cross-) contamination, improved chain of custody and possibility of direct analysis at the crime scene, which are the most important issues within forensic science. Obtaining an on-chip DNA-profile is complex as DNA extraction, PCR amplification and STR fragment separation have to be integrated on chip, as can be seen in the figure below [3,4]. Moreover, the 12-72 hour analysis of conventional techniques has to be beaten [4,5]. Fast results are required as a suspect can be held in custody for only 6 hours [5]. For the analysis of human biological samples micro-devices are developed for extraction, purification, amplification, separation and detection.
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One of the aspects of DNA-analysis is PCR (Polymerase Chain Reaction). In this reaction, DNA is replicated by an enzyme, polymerase. The process consists of 3 main steps, denaturation, extension, and annealing (see Figure below), which are carried out at different temperatures in a cyclic process. Typically 30 or more cycles are needed to obtain enough DNA for further analysis.

![PCR reaction scheme](image)

PCR reaction scheme. Denaturation occurs at ca. 95°C, extension at ca. 70°C, and annealing at ca. 60°C. From [6].

For the forensic application, it is required to have an as fast as possible amplification of DNA, which means that the cycle time has to be made as short as possible. From literature it has become clear that the intrinsic kinetics of the chemical reactions and phase transformations involved in PCR are in the millisecond range, or faster. This implies that the rate limiting steps in the cyclic process most likely are mass and heat transport. Mass transport has to occur in the PCR solution in order to bring reactants together for the reaction, and by using microfluidics, this mass transport becomes fast, because of the shorter distances for diffusion. Furthermore, since the PCR reaction was chosen to be performed in micro-droplets in a microfluidic channel, in which internal flows are present which enhance diffusion, mass transport is not the limiting factor.

What is left is the heat transport: to cycle the temperature, heat has to be transported to and from the microfluidic droplets. Especially the cooling step is considered to be critical, because the heating step can typically be made faster by putting in more heating power (however, care has to be taken that no overshoot in temperature will occur, since this may decompose the DNA), while the cooling step normally will be performed by heat diffusion to a cold reservoir.

The aim of this assignment is to:

a. Estimate the theoretical limit for the thermal cycling time in PCR
b. Design a number of chips which apply an optimized thermal cycling concept
c. Experimentally test these chips (if time allows)
A literature study has to be carried out prior to design chips for forensic DNA-analysis.

- **Literature study**
  - **Thermal cycling for PCR in a microfluidic format:** Make an inventory of the existing microfluidics/lab-on-a-chip technology for thermal cycling of reactants, with a focus on PCR. Which chip designs and heating/cooling concepts have been used, which materials (e.g. glass, PDMS, plastics or silicon) are suitable?
  - **Estimations/calculations:** Based on literature, evaluate the critical phenomena involved in fast thermal cycling of PCR, and estimate/calculate the theoretical limits.

- **Experimental setup and experiments on chip**
  - **Chip design:** Based on the calculations and the literature study, propose a number of chip designs with optimized temperature cycling capabilities. Also, in close collaboration with group members, design a fabrication process for these chips and draw the photolithographic masks, and build a set-up for testing the chips.
  - **Experimental testing of chips:** If time allows, perform functional tests of the chips, using a fluorescent dye (which has a temperature-dependent fluorescence intensity) to monitor the temperature inside the microchannels, preferably also with a droplet which is present in a microchannel. This requires working with a microscope and a camera and with the software to evaluate the images.

- **Finishing of the report and preparations for the final presentation**

**References**


