Low-Latency GFSK Demodulation Architecture Comparison and Design for FPGA

Alexandre Lopez
IC-Design group
University of Twente
Enschede, The Netherlands

Abstract—Gaussian Frequency Shift Keying (GFSK) is a widely used type of continuous phase modulation (CPM), where a Gaussian pulse shaping filter is used before frequency modulation. Commercially available GFSK demodulators are mostly optimised to minimise power consumption or bit error rate (BER), but rarely consider the latency of demodulation. However, in situations where the output of the demodulator is used in a feedback loop, the demodulator’s latency is a crucial factor regarding stability of the system. In this paper, we primarily investigate which noncoherent GFSK demodulator architecture, suitable for implementation on a field-programmable gate array (FPGA), has the lowest latency of demodulated bits, while considering BER performance secondary. Three demodulation methods were modelled in Simulink: instantaneous frequency estimation using zero-crossing detection, a quadricorrelator, and matched filters with envelope detection. Simulation results show the quadricorrelator demodulator is most suitable, introducing a latency of 1µs and a BER of 0.1% at Eb/N0 = 13.2 dB. The realistic model of this demodulator for FPGA produces a BER of 0.1% with Eb/N0 = 14.6 dB.

Index Terms—Frequency shift keying, Low latency communication, Field programmable gate arrays, Simulink.

I. INTRODUCTION

Since the first digital communications between devices in the 20th century, countless wireless communication standards have been defined. One such standard is Bluetooth Low Energy (BLE), using the Gaussian Frequency Shift Keying (GFSK) modulation scheme [1]. GFSK is a modulation type that filters the baseband message with a Gaussian filter, after which it is frequency modulated with continuous phase (CPM). This results in less required transmission bandwidth compared to regular frequency shift keying (FSK). Other than in BLE, GFSK is also used in many other standards, including Improved Layer 2 Protocol [2], DECT [3] and IEEE 802.15.4 [4]. This research is done in accordance with the BLE 1M PHY standard.

Currently available GFSK demodulators are primarily concerned with reducing BER and power consumption, since these are the most important attributes of a demodulator in most contexts. Ongoing research in the field of BLE at the Integrated Circuit Design group at the University of Twente, however, makes use of the demodulated message in a control loop, meaning low latency of the demodulator is of high importance regarding stability of the system. In fact, any control system where the demodulated message is used to give feedback on a system, would benefit from low demodulation latency. This research concerns itself with designing such a demodulator for BLE of PHY type 1M. In Bluetooth, receivers are predominantly noncoherent because of the cost efficiency associated with them [5], which is why the focus of this research is only on noncoherent demodulators.

This paper is structured as follows: in Section II-A, the GFSK modulation scheme is explained and modelled, after which the three demodulation architectures are analysed and designed in Section II-B. Simulations are done for the demodulators and results are then compared in Section III using the self-defined metric. In Section IV, a test setup is suggested, as well as a realistic implementation for FPGA. For this realistic implementation, a model is made in Simulink, followed by simulation results of a representative Simulink model in Section IV-D. Finally, the research is concluded in Section V with the implications of the results, as well as areas for further research on the topic.

II. GAUSSIAN FREQUENCY SHIFT KEYING

A. Modulation

GFSK modulation is a modification of FSK, where the baseband message is first pulse-shaped (i.e. filtered) using a Gaussian filter before being frequency modulated (see Fig. 1). The filter removes sharp frequency transitions, significantly reducing spectral width of the transmitted signal, at the cost of ISI [5]. A comparison of their spectra is shown in Fig. 2.

The transmitted signal can be expressed as [6]:

\[ s(t) = A \cos(2\pi f_c t + \phi(t)), \]  

(1)

where

\[ \phi(t) = 2\pi \frac{h R_s}{2} \int_0^t m(\tau) \, d\tau. \]  

(2)

Parameter \( f_c \) is the carrier frequency, \( h \) is the modulation index, \( R_s \) is the symbol data rate and \( m(t) \) is the pulse shaped bit sequence. The remainder of this research assumes the following parameters based on the BLE 1M PHY specification [1]:

- \( R_s = 1 \text{ Mb/s}, \)
- \( h = 0.5, \)
- The Gaussian filter’s bandwidth-time product BT = 0.5. Furthermore, it is assumed \( s(t) \) is already down-mixed to \( f_c = 1 \text{ MHz} \) upon reception at the demodulator.
A model of a demodulator is made in Simulink R2022b by modulating a Bernoulli bit sequence with the CPM block from the Wireless Communication toolbox (see Fig. 3) with a pulse width of three symbols and oversampling rate $sps = 1000$. The output of the CPM block is complex baseband, so it is then converted to passband with carrier frequency $f_c$. Fig. 4 shows that the CPM block also introduces a delay of 1 symbol. This delay is caused by the Gaussian filtering prior to modulation.

Next, the signal is downsampled to the sample frequency $f_s$ of the demodulator, after which additive white Gaussian noise (AWGN) is added to the signal. This way, no additional decimation filter is needed before downsampling to prevent the noise from aliasing. This workaround is needed because of the use of $sps = 1000$ in the first place, which is necessary to accurately represent a signal coming from an ideal transmitter.

### B. Demodulation

For the demodulation of the passband modulated signal provided by the GFSK modulator, three noncoherent demodulator architectures are considered, after which their latencies and BER performances are then compared.

The total time between transmission of a bit and its receival consists of three parts: the 1 µs delay of the CPM block, the delay of the demodulator, and the delay from symbol slicing. The symbol slicer of all three approaches is done by sampling the output of the demodulator exactly in the middle of a symbol, adding a constant $1.5 \mu s$ delay. The interested reader is referred to Appendix A for implementation details.

In this paper, we define the latency $L$ of a demodulator as the time delay between the transmitted and detected bit, minus the constant 1.5 µs from the CPM block and symbol slicing. The presented demodulators all have at least one parameter that trade latency for AWGN resilience. Therefore, multiple BER against $E_b/N_0$ simulations are done for the demodulators, each with different parameters. Additionally, the BER against $E_b/N_0$ is plotted for an ideal noncoherent FSK demodulator with the same modulation index, henceforth referred to as the reference demodulator. We use FSK as a lower bound to the BER against $E_b/N_0$ performance of GFSK, since it does not consider the ISI [5].

The maximum acceptable BER for BLE is 0.1% [1], which is achieved with $E_b/N_0 = 11$ dB for the reference demodulator. As a metric of noise resilience, we define

$$\Delta E_b \equiv \left[ \frac{E_b}{N_0} \right]_{\text{BER}=0.1\%} - 11 \text{ dB}.$$  

(3)
This number represents how much less noise the demodulator under consideration can handle in the channel, compared to the reference demodulator. To compare the demodulators with their different parameters, we define a figure of merit as

$$FoM = \frac{1}{L^2 \cdot \Delta E_b},$$

representing a better demodulator when FoM is larger. For simplicity, $L$ is in symbol periods (equivalent to 1 µs for $R_s = 1$ MHz) and $\Delta E_b$ is in dB.

For fair comparison, each demodulator uses the same sample frequency $f_s = 20$ MHz.

It must be noted this research only makes use of symmetric finite impulse response (FIR) filters because of their ease of construction in Matlab and because they have a constant group delay (of half their order) [7]. Constant group delay, however, is not required in most cases presented here, making this a simplification, representing a better demodulator when $\Delta f_c > 0$.

The latency of this part of the demodulator is the time between two zero crossings, since this is how long the demodulator needs to conclude if a 0 or 1 was sent. Therefore, the average latency of this part is $\frac{1}{2} \tau$.

However, this method would be very sensitive to AWGN because this can introduce additional zero crossings, completely throwing off the counter. This is why a lowpass filter (LPF) precedes the zero-crossing detectors. The filter is of order $N$ and has a cutoff frequency of 2 MHz, based on the spectral width seen in Fig. 2. The consequence hereof is that an additional latency of $\frac{\tau}{N_T}$ samples is introduced [7], making the total latency of the demodulator $\frac{1}{2} \cdot \left( \frac{1}{\tau} + \frac{N}{N_T} \right)$.

2) Quadricorrelator: The second presented method is the discrete-time quadricorrelator shown in Fig. 6, where the conventional differentiation elements are replaced by delay elements [9].

First, the passband GFSK signal is split and down-mixed into its in-phase and quadrature components

$$s_1(t) = \text{LPF}(\cos(2\pi f_c t) \cdot s(t)) = \frac{A}{2} \cos(\phi(t))$$

and

$$s_Q(t) = \text{LPF}(-\sin(2\pi f_c t) \cdot s(t)) = \frac{A}{2} \sin(\phi(t)).$$

Next, these signals are delayed by $\Delta T$, cross multiplied and subtracted from each other to produce

$$y(t) = s_Q(t) s_1(t - \Delta T) - s_1(t) s_Q(t - \Delta T)$$

$$\quad = \frac{A^2}{4} \sin(\phi(t) - \phi(t - \Delta T)) \cdot \frac{\Delta \phi(t)}{\Delta \phi(t)}$$

The argument of the sine, denoted $\Delta \phi(t)$, can be expressed as

$$\Delta \phi(t) = 2\pi \frac{h R_s}{2} \left( \int_0^t m(\tau) \, d\tau - \int_0^{t-\Delta T} m(\tau) \, d\tau \right)$$

$$\quad = 2\pi h R_s \int_{t-\Delta T}^t m(\tau) \, d\tau.$$  

Ignoring the latency introduced by the image rejection filter of the mixers and scaling factors, this shows the output of the demodulator at time $t$ is the sine of the area under $m(t)$ from $t - \Delta T$ until $t$. Assuming $-\frac{\pi}{2} \leq \Delta \phi(t) \leq \frac{\pi}{2}$ (which we will soon make sure of), the sine in (8) is a strictly increasing function through 0, meaning the sign of $y(t)$ is the same as the sign of the mentioned area. See Fig. 7 for a graphical relationship between $m(t)$ and $y(t)$.

To ensure $-\frac{\pi}{2} \leq \Delta \phi(t) \leq \frac{\pi}{2}$ we look at the maximum value $\Delta \phi(t)$ can reach and solve for $\Delta T$ accordingly. Equation (8) shows the maximum $\Delta \phi$ is achieved when $m(t) = 1$, so

$$\frac{2\pi}{2} h R_s \int_{t-\Delta T}^t 1 \, d\tau \leq \frac{\pi}{2} \implies \Delta T \leq \frac{2h R_s}{2}.$$
When two unequal bits are transmitted, it takes approximately $\Delta T$ for the area under the new bit to make up for the area of opposite sign of the old bit due to the close symmetry around the zero crossings of $m(t)$ (see Fig. 7b). This means the latency of this part of the demodulator is $\Delta T$. It must be noted this is not exact; there is slight asymmetry around the zero crossing of $m(t)$ caused by the history of the preceding symbol. However, for a BT product of 0.5, this deviation is less than 3 ns, which is insignificant compared to the symbol time of 1 µs.

Another source of delay is due to the image rejection filter. In Fig. 8 we see the cutoff frequency of the filter must be at

$$f_c \pm \frac{\Delta f}{2}$$

Stopband frequencies can be set because the unwanted image can be rejected. The image rejection filter is used to discriminate the frequencies by bandpass filters centered at $f_c \pm \Delta f$, where $\Delta f = \frac{hR}{2}$ is the frequency deviation of modulation. The width of the passband is set to 1 MHz. The result is two signals, roughly centered at $f_c \pm \Delta f$.

After this, we use a square-law AM demodulator as an envelope detector. Squaring the signals results in two terms: the desired envelope, and an unwanted copy, centered at $2(f_c \pm \Delta f)$ [10]. Hence, the squaring blocks are followed by LPF's with cutoff frequencies $f_c \pm \Delta f$ and using a rectangular window for a sharper transition. The order of this filter shall be kept at 14, since results in Appendix B show the performance gets worse with both a higher order or a lower order.

The only parameter of the demodulator therefore is bandpass filter order $N$, resulting in a latency of $\frac{N+14}{2f_c}$.

### III. Simulation Results

A plot of BER against $E_b/N_0$ is shown in Appendix B, from which values for $\Delta E_b$ for each demodulator architecture are found and FoM is calculated. The resulting summary is given in Table I. The demodulator with the highest FoM is the quadricorrelator with a delay block of 1 µs and filter order $N = 20$, producing a latency of 1 µs, and requires 2.2 dB more $E_b/N_0$ than the reference demodulator at a BER of 0.1%.

The fastest demodulator is the zero crossing detector with a second order filter, and the best demodulator regarding BER vs $E_b/N_0$ performance is the matched filter kind with filters of order 80. We are, however, only interested in the demodulator with the highest FoM.

It must be noted that only a limited number of parameter combinations were simulated due to time constraints, making the optimal solution unlikely to be the one presented here. However, the square in (4) was mostly chosen arbitrarily in the first place anyway, so this is of no serious concern.

### IV. FPGA Implementation

This section covers the generation of the GFSK wave, followed by a realistic (quantised) Simulink model of the demodulator. Finally, VHDL suggestions are given for final implementation. The list of components used is given in Table II.
A. Signal Generation

In order to test the demodulator once implemented on FPGA, a GFSK wave must be generated with a known bit sequence, starting with a flag that the FPGA can easily recognise.

The signal generator can loop an arbitrary signal (from a file) of maximum length $4 \times 10^6$ samples and with maximum sample frequency $250 \text{MHz}$ [11]. The amplitude is restricted to $1.5V_{pp}$ because this is the input range of the analog to digital converter (ADC). Creating a GFSK wave with the aforementioned properties results in the signal shown in Fig. 10. The amplitude seems off by a factor 2, but this is because of the high Z of the oscilloscope; the signal generator accounts for the 50Ω input impedance of the ADC. The exact Matlab script to generate the .arb file is given in Appendix C.

Although not done in this research, if BER performance were to be simulated, care must be taken to ensure the AWGN is band-limited to $f_s/2$. The simplest way to ensure this is Matlab is to add the white Gaussian noise, and then filter the signal with a very high order LPF. Alternatively, an analog filter could also be used.

B. Optimisation for FPGA

A modification that simplifies implementation on FPGA is the reduction of the local oscillator (LO) to a 1 bit resolution instead of a full-scale sine wave. This way, a lookup table can be omitted, at the cost of harmonic distortion. The Fourier series of a 1 bit sine wave of frequency $f_c$ is

$$\sin_{sq}(t) = \frac{1}{n} \sum_{n=1}^{\infty} \sin(n \cdot 2\pi f_c t).$$

Using (12) and (1), the output of the mixer can be expressed as

$$s(t) \sin_{sq}(t) = \sum_{n=1}^{\infty} \frac{4A}{\pi n} \cdot \frac{1}{2} \sin((n+1) \cdot 2\pi f_c t + \phi(t)) + \sin((n-1) \cdot 2\pi f_c t - \phi(t)).$$

For $n = 1$, this is same as the output of a mixer using a full scale sine wave, scaled by a factor $4/\pi$. The rest of the terms are distortions, centered at frequencies $2f_c, 4f_c, 6f_c,$ etc. This is, however, insignificant, because the terms in the sum decay by themselves, as well as get filtered by the mixer’s image rejection LPF with cutoff frequency $f_c$.

The second simplification regards the LPFs. The Cyclone V on this FPGA board has a dedicated DSP chip which can only be configured to have at most two parallel 18 bit multipliers that run at a maximum frequency of 200 MHz [12]. Using a filter order 20 and a sample frequency of 20 MHz, neither a parallel nor a serial FIR filter can be implemented; a parallel implementation would require $2 \cdot 21 = 42$ multipliers and a serial implementation would require a speed of $21 \cdot 20 = 420 \text{MHz}$. Potential solutions include a reduction in sample frequency, as well as using a lower order filter.

However, a different approach is used in this case: all filter coefficients are changed to 1. The result is a scaled moving average filter, which is also a type of LPF. Fig. 12 shows the frequency responses of the original filter compared to the new moving average filter.

C. Implementation Suggestions

To simulate the performance of the realistic demodulator, these two modifications are made in Simulink and the receiving input is quantised. The realistic model of the realisable demodulator is shown in Fig. 11.

The ADC board used with the FPGA has a 14 bit offset binary output [13], so the model’s modulator output is mapped and rounded from 0 to $2^{14} - 1$ in the ADC block. For the multiplication and filtering to work, the DC offset is then removed by temporarily turning the bus into 15 bits, subtracting the constant $\left\lfloor \frac{2^{14}}{2} \right\rfloor$, and then truncation by 1 bit, while keeping the sign bit.

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**Table I**

<table>
<thead>
<tr>
<th>Architecture</th>
<th>Parameter(s)</th>
<th>$\Delta E_{th}$ [dB]</th>
<th>$L$ [µs]</th>
<th>FoM</th>
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<tr>
<td>Z.C. detector $(N)$</td>
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<td>0.295</td>
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<td></td>
<td>10</td>
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<td>0.317</td>
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<td></td>
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<td>2.00</td>
<td>0.052</td>
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<td>Quadrincorr. $(\Delta T, N)$</td>
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<td>50</td>
<td>5.8</td>
<td>1.30</td>
</tr>
<tr>
<td></td>
<td>0.5</td>
<td>50</td>
<td>4.2</td>
<td>1.50</td>
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<td></td>
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<td>50</td>
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<td>1.10</td>
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**Table II**

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<td>MY59003394</td>
</tr>
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<td>Terasic</td>
<td>SoCKit rev. C</td>
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<tr>
<td>Scope</td>
<td>Keysight</td>
<td>DSOX2002A</td>
<td>MY56273381</td>
</tr>
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</table>

Fig. 10. Oscilloscope acquisition of output from GFSK wave generation.
The 1 MHz LOs can be made by taking the existing 20 MHz clock used for the ADC, and connecting it to a counter that ranges from 0 to 19. From this, the $-\sin(2\pi f_c t)$ is created by creating a signal that becomes 1 when the counter hits 0, and becomes 0 when the counter hits 10. Similarly, the $\cos(2\pi f_c t)$ is created by creating a signal that becomes 1 when the counter hits 5, and becomes 0 when the counter hits 15.

Mixing the signal with the 1 bit LO is efficiently done by applying the appropriate bit operation rather than using a full multiplier. Signed data is stored in two’s complement by the IEEE.numeric_std library, so multiplication by $-1$ is done by inverting every bit and adding one. The operation of inverting the signal in case LO is 0 and leaving it unchanged if LO is 1, is equivalent to a XNOR gate. Next, 1 must be added to the signal in case LO is 0, and 0 must be added in case LO is 1. This is achieved by negating the LO and adding it to the output. The diagram of the multiplier is shown in Fig. 13.

Next, the LPF is made by placing 20 data flipflops in series with adders summing the individual stages. The corresponding block diagram is shown in Fig. 15. The additional bus width required is $\left\lceil \log_2(21) \right\rceil = 5$, making the output width of the filter 19 bits.

Next, the signals are delayed by 20 by putting 20 data flipflops in series. Multiplication is done with the dedicated 18 by 18 bit multipliers available. The result is 36 bits wide.

Subtraction can be achieved by constant multiplication by -1 and an adder. The output after this stage is 37 bits, from which only the MSB is used, since this is the sign bit. This bit is considered the output of the demodulator. The full model is shown in Fig. 11.

At this stage symbol slicing is performed. As can be seen in Fig. 10, the wave is generated such that the middle of the pulses fall on multiples of 1 µs since the starting flag. This starting flag can be turned into a signal by comparing the ADC output to $\frac{5}{6}(2^{14} - 1)$. If a data flipflop samples the output of the demodulator with period $\frac{1}{R_s} = 1$ µs, starting at the rising edge of the starting flag, then the output of the demodulator is sampled exactly in the middle of each symbol. This bit sequence can then be stored in random access memory (RAM), where also the known bit sequence is stored. A BER calculation can then be made and displayed using the LCD screen on the board.

Note it is very important for the clocks of the FPGA and the signal generator to be synchronised. This can be achieved by either providing the signal generator with a square wave generated from the FPGA by using the DAC, or by providing the FPGA with the clock from the signal generator using the second ADC channel.

D. Realistic Simulation

The transient analysis shown in Fig. 14 gives an overall idea of the stages of demodulation of the quadricorrelator. From it, we see the ripple from the intermediate signal due to the square local oscillator. In Fig. 16, the realistic demodulator does not perform much worse than the original model it was
Fig. 14. Simulation result of the Simulink model of the realistic quadricorrelator GFSK demodulator, simplified for implementation on FPGA.

Fig. 15. Scaled moving average filter of order 20.

Fig. 16. BER against $E_b/N_0$ for the realistic Simulink model of the quadricorrelator, compared to the model from which it descended and the reference FSK demodulator.

derived from. The latency remains 1 µs and $E_b/N_0 = 3.6$ dB, resulting in $\text{FoM} = 0.28$. This worsening is partially caused by quantisation (modeled by rounding of integers), the introduced harmonics from the square wave, as well as the simplified LPFs.

Although the FoM is lower than the original 0.44, this is still high in comparison to most demodulators listed in Table I.

V. CONCLUSION

This research presented three non-coherent demodulation architectures for GFSK with parameters in accordance with the BLE 1M PHY standard. The considered architectures were a zero crossing detector, a quadricorrelator and matched filters with envelope detection. Each demodulator was analysed, based on which multiple designs were made for every demodulator and the models were simulated for varying levels of AWGN.

With the primary objective of designing a low-latency demodulator, which still has a good AWGN resilience, a FoM was defined for comparison. Results show the quadricorrelator with a delay $\Delta T = 1$ µs and filter order $N = 20$ presents the highest FoM.

Next, a test setup, as well as specific FPGA implementation ideas were suggested, based on which a realistic version of the aforementioned best performing demodulator was made. Realistic implementation did reduce the FoM, but still remained amongst the best ones, suggesting it is a suitable demodulator.

However, further research should be done into the design of more appropriate filters, namely by considering IIR filters, or by constructing FIR filters differently. This research also only considered AWGN as a disturbance, but the demodulators might react differently to different disturbances, such as frequency drift, DC offset, jitter, etc. Additionally, changing the
sample frequency might also have effects not observed in this paper. This research also only investigated the architectures for GFSK parameters in accordance to the BLE 1M PHY standard. FoM results may vastly differ for GFSK with different parameters. Finally, only a few versions of each demodulator were simulated, meaning there might still be (combinations of) parameters that produce better results than seen here.

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REFERENCES


[13] Analog Devices, Dual AD converter AD9248, Rev. A.
## APPENDIX A
### SIMULINK MODELS

For every model it is required to run the following code to load the necessary variables into workspace:

```matlab
Rs = 1e6; % symbol rate (= bit rate)
BT = 0.5; % bandwidth-time product
Tw = 3; % FIR filter length/symbol length
h = 0.5; % modulation index
fc = 1e6; % carrier frequency
sps = 1000; % samples per symbol
fs = 20e6; % sample frequency of demodulators
```

A. Modulator

The exact parameters of the blocks used for modulation are listed below:

- Bernoulli Binary Generator
  - Pr(0): 0.5;
  - Initial seed: 0
  - Sample time: 1/Rs
  - Samples per frame: 1
  - Output data type: boolean
- CPM Modulator Baseband
  - M-ary number: 2
  - Input type: Bit
  - Symbol set ordering: Binary
  - Modulation index: h
  - Frequency pulse shape: Gaussian
  - BT product: BT
  - Pulse length: Tw
  - Symbol prehistory: 1
  - Phase offset: 0;
  - Samples per symbol: sps
  - Rate options: Allow multirate processing
  - Output data type: double
- cos and sin
  - Sine type: time based
  - Time (t): Use simulation time
  - Amplitude: 1
  - Bias: 0
  - Frequency (rad/sec): 2*pi*fc
  - Phase: 0 for cos, pi/2 for sin
  - Sample time: 1/(Rs*sps)
- Zero-Order Hold
  - Sample time: 1/fs
- AWGN Channel
  - Initial seed: 67
  - Mode: Signal to noise ratio (Eb/No)
  - Eb/No (dB): EbNo
  - Number of bits per symbol: 1
  - Input signal power: 1/2
  - Symbol period: 1/Rs

B. Zero-Crossing Demodulator

The following code needs to be run first, where the value for N is not strict.

```matlab
Cmid = fs/(2*fc);
N = 10;
filtZC = designfilt('lowpassfir', ...
  'FilterOrder',N, ...
  'CutoffFrequency',2e6/(fs/2));
```

The blocks in the Simulink model have the following parameters:

- Discrete FIR Filter
  - Coefficients: filtZC.Coefficients
- Pulse Generator:
  - Pulse type: Sample based
  - Time: Use simulation time
  - Amplitude: 1
  - Period: 2
  - Pulse width: 1
  - Phase delay: 0
  - Sample time: 1/fs
- Counter
  - Count direction: Up
  - Count even: Either edge
  - Counter size: User defined
  - Maximum count: Cmid*2
  - Initial count: 0
  - Output: Count and Hit
  - Hit values: Cmid + 1
  - Reset input: Check
  - Count data type: double
  - Hit data type: Logical

C. Quadricorrelator

The following code needs to be run first, where the values for DT and N are not strict.

```matlab
DT = 2;
N = 50;
filtDM = designfilt('lowpassfir', ...
  'FilterOrder',N, ...
  'CutoffFrequency',1e6/(fs/2));
```

The blocks in the Simulink model have the following parameters:

- Sine Wave
  - Sine type: time based
  - Time (t): Use simulation time
  - Amplitude: 1
  - Bias: 0
  - Frequency (rad/sec): 2*pi*fc
  - Phase: pi/2
  - Sample time: 1/fs
- Discrete FIR Filter
  - Filter structure: Direct form,
  - Coefficients: filtDM.Coefficients
- Delay
  - Delay length: DT
D. Matched Filter

The following code needs to be run first, where the values for DT and N are not strict.

```matlab
N1 = 50;
N2 = 14;
hMF1 = designfilt('bandpassfir', ...
  'FilterOrder',N1, ...
  'CutoffFrequency1',(0.75-0.5)*1e6/(fs/2), ...
  'CutoffFrequency2',(0.75+0.5)*1e6/(fs/2));
hMF2 = designfilt('bandpassfir', ...
  'FilterOrder',N1, ...
  'CutoffFrequency1',(1.25-0.5)*1e6/(fs/2), ...
  'CutoffFrequency2',(1.25+0.5)*1e6/(fs/2));
hLP1 = designfilt('lowpassfir', ...
  'FilterOrder',N2, ...
  'CutoffFrequency',0.75e6/(fs/2), ...
  'Window','rectwin');
hLP2 = designfilt('lowpassfir', ...
  'FilterOrder',N2, ...
  'CutoffFrequency',1.25e6/(fs/2), ...
  'Window','rectwin');
```

The blocks in the Simulink model have the following parameters:

- **Discrete FIR Filter**
  - Coefficients: `<X>.Coefficients`, where `<X>` is hMF1 for the low bandpass filter, hMF2 for the high bandpass, hLP1 for the low lowpass, and hLP1 for the high lowpass.

E. Symbol slicing and BER computation

First, the transmitted bits are oversampled with $f_s$ and delayed by the exact amount of samples that correspond to the demodulator’s latency. Next, we need to resample exactly in the middle of the bits. This is done in Simulink by delaying the oversampled bitstream such that the middle of a bit falls exactly on an integer multiple of the sample time $\frac{1}{R_s}$. For $f_s = 20$ MHz and $R_s = 1$ MHz, the middle of a symbol is after 10 samples, and the entire symbol is 20 samples. So by adding a delay of

$$\text{mod}(10-<\text{latency in samples}>,20),$$ (14)the bit stream is delayed by the smallest amount such that the middle of the bits fall exactly on multiples of 1 $\mu$s. Then, a zero order hold block samples the bit stream at these instances and the signal is given to a BER calculation block.
**APPENDIX C**

**WAVEFORM GENERATION**

The following code was used to generate the ARB file that was manually transferred to storage of the wave generator through USB.

```matlab
% % generate GFSK for KEYSIGHT 33600A
% set params
fs = 250e6;  % max Sa/s for this device
length = 4e6;  % max Sa for this device
Rs = 1e6;  % symbol rate (= bit rate)
BT = 0.5;  % bandwidth-time product
Tw = 3;  % FIR filter length
fc = 1e6;  % Carrier frequency
Df = 250e3;  % frequency deviation

% therefore
sps = fs/Rs;  % samples per symbol
Nsys = length/sps - Tw;  % -Tw due to filtering

% generate bits
rng(0)
bits = (randi(2,[Nsys,1]) - 1)*2-1;
msg = repelem(bits,sps);

% GFSK
msg_filtered = conv(gaussdesign(BT,Tw,sps),msg);
y = fmmod(msg_filtered,fc,fs,2*Df);

% add beginning mark
y(1:50) = 1.5;
y(51:100) = -1.5;

% remove bleed from filters abruptly
y(101:sps*Tw/2) = 0;
y(end - sps*Tw/2:end) = 0;

% normalise
y = y/1.5;

% make ARB file
header = "File Format:1.10\n" + ...  % low level
"Channel Count:1\n" + ...  % sample rate
"Sample Rate:250E6\n" + ...  % high level
"High Level:0.75\n" + ...  % data type
"Low Level:-0.75\n" + ...  % data: \n"
dataspec = "%d\n";
fileID = fopen("GFSK.arb","w");
fprintf(fileID,header);
fprintf(fileID,dataspec,round(32767*y));
fclose(fileID);

%%% remove last \n manually using text editor, %
%%% else insufficient memory prompt!!!
```